

Imprints of massive inverse seesaw model neutrinos in lepton flavor violating Higgs boson decays

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In this paper we consider a Higgs boson with mass and other properties compatible with those of the recently discovered Higgs particle at the LHC, and explore the possibility of new Higgs leptonic decays, beyond the standard model, with the singular feature of being lepton flavor violating (LFV). We study these LFV Higgs decays, $H \rightarrow l_k \bar{l}_m$, within the context of the inverse seesaw model (ISS) and consider the most generic case where three additional pairs of massive right-handed singlet neutrinos are added to the standard model particle content. We require in addition that the input parameters of this ISS model are compatible with the present neutrino data and other constraints, like perturbativity of the neutrino Yukawa couplings. We present a full one-loop computation of the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates for the three possible channels, $l_k \bar{l}_m = \mu \bar{\tau}, e \bar{\tau}, e \bar{\mu}$, and analyze in full detail the predictions as functions of the various relevant ISS parameters. We study in parallel the correlated one-loop predictions for the radiative decays, $l_m \rightarrow l_k \gamma$, within this same ISS context, and require full compatibility of our predictions with the present experimental bounds for the three radiative decays, $\mu \rightarrow e \gamma$, $\tau \rightarrow \mu \gamma$, and $\tau \rightarrow e \gamma$. After exploring the ISS parameter space we conclude on the maximum allowed LFV Higgs decay rates within the ISS.

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I. INTRODUCTION

At present, there seems to be a broad consensus in the high energy physics community that the recently discovered scalar particle at the CERN-LHC [1,2] behaves as the Higgs particle of the standard model of particle physics (SM). The most recent measurements of this scalar particle mass by the ATLAS and CMS collaborations set $m_h^{\text{ATLAS}} = 125.5 \pm 0.6$ GeV [3] and $m_h^{\text{CMS}} = 125.7 \pm 0.4$ GeV [4], respectively. These experiments also show that the most probable J^P quantum numbers for this discovered Higgs boson are 0^+ , and conclude that the measured Higgs particle couplings to the other SM particles are in agreement so far, although yet with moderate precision, with the values predicted in the SM. Also, the scalar Higgs-like particle width Γ_h has been found to be $\Gamma_h < 17.4$ MeV, which is about 4.2 times the SM value [5].

On the other hand, there is also a major consensus that the SM must be modified in order to include the neutrino masses and oscillations in agreement with present data, which are nowadays quite impressive and urge of an explanation from a theoretical framework beyond the SM. Thus, in order to be compatible with the present neutrino data we choose here to go beyond the SM using one of its simplest and more

appealing extensions, the inverse seesaw model (ISS) [6–8]. This ISS extends the SM particle content by adding pairs of right-handed (RH) neutrinos with opposite lepton number whose masses and couplings can be properly chosen to produce the physical light neutrino masses and oscillations in good agreement with present data [9–11]. In contrast to the original seesaw type I model [12–16], the seesaw mechanism that produces the small light physical neutrino masses in the ISS is associated to the smallness of the Majorana mass model parameters, such that when these are set to zero lepton number conservation is restored, therefore increasing the symmetries of the model. Another appealing feature of the ISS is that it allows for large Yukawa neutrino couplings while having at the same time moderately heavy right-handed neutrino masses at the $\mathcal{O}(\text{TeV})$ energies that are reachable at the present colliders, like the LHC. In addition to the possibility of being directly produced at colliders, these right-handed neutrinos could also lead to a new rich phenomenology in connection with lepton flavor violating (LFV) Physics. This is because the ISS right-handed neutrinos can produce non-negligible contributions to LFV processes via radiative corrections that are mediated by the sizable neutrino Yukawa couplings, therefore leading to clear signals/imprints in these rare processes, which are totally absent in the SM. These LFV processes include the most frequently studied radiative decays, $\mu \rightarrow e \gamma$, $\tau \rightarrow \mu \gamma$, $\tau \rightarrow e \gamma$, others like $\mu \rightarrow 3e$, leptonic and semileptonic τ decays, $\mu - e$ conversion in heavy nuclei, and others (see [17] for a review). The ISS mechanism also has implications

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on deviations from lepton flavor universality [18,19] and from lepton number conservation [20–24]. Although quite promising future sensitivities for some of these LFV processes are expected, for instance, for $\mu - e$ conversion in heavy nuclei [25–28], at present the highest sensitivity to LFV signals is obtained in $\mu \rightarrow e\gamma$ where MEG has set an upper bound at branching ratio (BR), $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29].

In this paper, we study other LFV processes, the Higgs decays into lepton-antilepton pairs $H \rightarrow l_k \bar{l}_m$ with $k \neq m$, which are of obvious interest at present, given the recent discovery of the Higgs particle and the fact that these rare Higgs decays are also being presently explored at the LHC. The current direct search at the LHC for these LFV Higgs decays (LFVHD) has been recently reported in [30], where an upper limit of $\text{BR}(H \rightarrow \mu\tau) < 1.57\%$ at 95% C.L. has been set using 19.7 fb^{-1} of $\sqrt{s} = 8 \text{ TeV}$. This improves previous constraints from indirect measurements at LHC [31] by roughly one order of magnitude (see also [32]), and it is close to the previous estimates in [33] that predicted sensitivities of 4.5×10^{-3} (see also [34]). The future perspectives for LFVHD searches are encouraging due to the expected high statistics of Higgs events at future hadronic and leptonic colliders. Although, to our knowledge, there is no realistic study, including background estimates, of the expected future experimental sensitivities for these kinds of rare LFVHD events, a naive extrapolation from the present situation can be done. For instance, the future LHC runs with $\sqrt{s} = 14 \text{ TeV}$ and total integrated luminosity of first 300 fb^{-1} and later 3000 fb^{-1} expect the production of about 25 and 250 million Higgs events, respectively, to be compared with 1 million Higgs events that the LHC produced after the first run [35]. These large numbers suggest an improvement in the long-term sensitivities to $\text{BR}(H \rightarrow \mu\tau)$ of at least two orders of magnitude with respect to the present sensitivity. Similarly, at the planned lepton colliders, like the international linear collider (ILC) with¹ $\sqrt{s} = 1 \text{ TeV}$ and 2.5 ab^{-1} [36], and the future electron-positron circular collider (FCC-ee) as the TLEP with $\sqrt{s} = 350 \text{ GeV}$ and 10 ab^{-1} [37], the expectations are of about 1 and 2 million Higgs events, respectively, with much lower backgrounds due to the cleaner environment, which will also allow for a large improvement in LFV Higgs searches with respect to the current sensitivities.

We will present a full one-loop computation of the LFV partial decay widths, $\Gamma(H \rightarrow l_k \bar{l}_m)$, within the ISS context with three extra pairs of right-handed neutrinos, and will analyze in full detail the predictions for the LFVHD rates, $\text{BR}(H \rightarrow l_k \bar{l}_m)$, as functions of the various relevant ISS parameters. These LFV Higgs decays were analyzed in the context of the SM enlarged with three heavy Majorana neutrinos for the first time in [38]. Later, they were computed in the context of the seesaw I model in [39], and they were

found to lead to extremely small rates due to the strong suppression from the extremely heavy right-handed neutrino masses, at 10^{14-15} GeV , in that case. This motivates our study of the LFV Higgs decays in the ISS case with the right-handed neutrino masses lying in contrast at the $\mathcal{O}(\text{TeV})$ energy scale and therefore the rates are expected to be larger than in the seesaw I case. The interest of neutrino masses at this $\mathcal{O}(\text{TeV})$ energy scale is also because they can be directly produced at the LHC. Furthermore, we will also study in parallel the correlated one-loop predictions for the radiative decays, $\text{BR}(l_m \rightarrow l_k \gamma)$, within this same ISS context, and we will require full compatibility of our predictions with the present experimental upper bounds for the three relevant radiative decays, $\mu \rightarrow e\gamma$, $\tau \rightarrow \mu\gamma$, and $\tau \rightarrow e\gamma$, the first one being the most constraining one. We will require in addition that the input parameters of the ISS are compatible with the present neutrino data and other constraints, like perturbativity of the neutrino Yukawa couplings. After exploring the ISS parameter space we will conclude on the maximum allowed LFV Higgs decay rates within the ISS.

The paper is organized as follows: in Sec. II we summarize our theoretical framework and shortly review the main features of the ISS that are relevant for the present computation. In Sec. III we present our computation of the one-loop LFV Higgs decay widths within the ISS and include, for completeness and comparison, both the analytical formulas for the LFV Higgs decays and the LFV radiative decays. The full one-loop analytical formulas for the LFV Higgs form factors are collected in the Appendix. Section IV is devoted to the presentation of the numerical results of our computation and also includes the predictions for both kind of LFV processes, the branching ratios for the LFV Higgs decays, $H \rightarrow \mu\bar{\tau}$, $H \rightarrow e\bar{\tau}$, and $H \rightarrow e\bar{\mu}$ that we compare with the branching ratios for the radiative decays, $\tau \rightarrow \mu\gamma$, $\tau \rightarrow e\gamma$, and $\mu \rightarrow e\gamma$. Finally, we summarize our conclusions in Sec. V.

II. THEORETICAL FRAMEWORK

One of the simplest extensions of the SM leading to nonzero neutrino masses and mixing is the addition of fermionic gauge singlets. As mentioned above, a very attractive model is the ISS that supplements the SM with pairs of RH neutrinos, denoted here by ν_R and X , with opposite lepton number. While the minimal model that fits oscillation data requires only two generations of RH neutrinos [40], we consider here a more generic model containing three pairs of fermionic singlets. It extends the SM Lagrangian with the following neutrino Yukawa interactions and mass terms:

$$\mathcal{L}_{\text{ISS}} = -Y_{\nu}^{ij} \bar{L}_i \tilde{\Phi} \nu_{Rj} - M_R^{ij} \bar{\nu}_{Ri}^c X_j - \frac{1}{2} \mu_X^{ij} \bar{X}_i^c X_j + \text{H.c.}, \quad (1)$$

where L is the SM lepton doublet, Φ is the SM Higgs doublet, $\tilde{\Phi} = i\sigma_2 \Phi^*$, with σ_2 being the corresponding Pauli

¹We thank J. Fuster for private communication with the updated ILC perspectives.

matrix, Y_ν is the 3×3 neutrino Yukawa coupling matrix, M_R is a lepton number conserving complex 3×3 mass matrix, and μ_X is a Majorana complex 3×3 symmetric mass matrix that violates lepton number conservation by two units. Setting the latter to zero would restore the conservation of lepton number, thus increasing the symmetry of the model. This makes the smallness of μ_X natural since it could be seen as the remnant of a symmetry broken at a higher energy [41]. Since a Majorana mass term of the type $\overline{\nu_{Ri}}\nu_{Rj}^C$ would only give subleading corrections to the neutrino masses and the observables considered here, we have taken it to be zero, for simplicity.

After electroweak symmetry breaking, the 9×9 neutrino mass matrix reads, in the electroweak interaction basis (ν_L^C, ν_R, X) ,

$$M_{\text{ISS}} = \begin{pmatrix} 0 & m_D & 0 \\ m_D^T & 0 & M_R \\ 0 & M_R^T & \mu_X \end{pmatrix}, \quad (2)$$

with the 3×3 Dirac mass matrix given by $m_D = Y_\nu \langle \Phi \rangle$, and the Higgs vacuum expectation value is taken to be $\langle \Phi \rangle = v = 174$ GeV. Since this mass matrix is complex and symmetric, it can be diagonalized using a 9×9 unitary matrix U_ν according to

$$U_\nu^T M_{\text{ISS}} U_\nu = \text{diag}(m_{n_1}, \dots, m_{n_9}). \quad (3)$$

This gives three light mass eigenstates and six heavy mass eigenstates, and the electroweak eigenstates and the mass eigenstates are related through

$$\begin{pmatrix} \nu_L^C \\ \nu_R \\ X \end{pmatrix} = U_\nu P_R \begin{pmatrix} n_1 \\ \vdots \\ n_9 \end{pmatrix}, \quad \begin{pmatrix} \nu_L \\ \nu_R^C \\ X^C \end{pmatrix} = U_\nu^* P_L \begin{pmatrix} n_1 \\ \vdots \\ n_9 \end{pmatrix}. \quad (4)$$

In order to illustrate more simply the dependence on the seesaw parameters, let us first consider the one generation case and then we will come back to the three generation case. In this one generation case there are just three ISS model parameters, M_R , μ_X , and Y_ν , and there are just three physical eigenstates: one light ν and two heavy N_1 and N_2 . In the limit $\mu_X \ll m_D, M_R$, the mass eigenvalues are given by

$$m_\nu = \frac{m_D^2}{m_D^2 + M_R^2} \mu_X, \quad (5)$$

$$m_{N_1, N_2} = \pm \sqrt{M_R^2 + m_D^2} + \frac{M_R^2 \mu_X}{2(m_D^2 + M_R^2)}, \quad (6)$$

with the light neutrino mass m_ν being proportional to μ_X , thus making it naturally small, and the two heavy masses

m_{N_1, N_2} being close to each other. As a consequence in this $\mu_X \ll m_D, M_R$ limit, these two nearly degenerate heavy neutrinos combine to form pseudo-Dirac fermions.

A similar pattern of neutrino mass eigenvalues occurs in the three generation case, with one light and two nearly degenerate heavy neutrinos per generation. This can be illustrated clearly in the limit $\mu_X \ll m_D \ll M_R$, where the mass matrix M_{ISS} can be diagonalized by blocks [42], leading to the following 3×3 light neutrino mass matrix:

$$M_{\text{light}} \simeq m_D M_R^{T-1} \mu_X M_R^{-1} m_D^T, \quad (7)$$

which is then diagonalized using the unitary Pontecorvo–Maki–Nakagawa–Sakata (PMNS) matrix U_{PMNS} [43]:

$$U_{\text{PMNS}}^T M_{\text{light}} U_{\text{PMNS}} = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3}), \quad (8)$$

where m_{ν_1}, m_{ν_2} , and m_{ν_3} are the masses of the three lightest neutrinos.

Then, by defining a new 3×3 mass matrix by

$$M = M_R \mu_X^{-1} M_R^T, \quad (9)$$

the light neutrino mass matrix can be written similarly to the type I seesaw model as

$$M_{\text{light}} \simeq m_D M^{-1} m_D^T. \quad (10)$$

The mass pattern of the heavy neutrinos in the $\mu_X \ll m_D \ll M_R$ limit presents a similar behavior to the one generation case. The heavy neutrinos form quasidegenerate pairs with a mass approximately given by the eigenvalues of M_R , namely $M_{R_{1,2,3}}$ for the first, second, and third generation, respectively, and with a splitting of order $\mathcal{O}(\mu_X)$.

For our phenomenological purposes, and in order to implement easily the compatibility with present neutrino data, we will use here the useful Casas-Ibarra parametrization [44] that can be directly applied to the inverse seesaw model case, giving

$$m_D^T = V^\dagger \text{diag}(\sqrt{M_1}, \sqrt{M_2}, \sqrt{M_3}) \times R \text{diag}(\sqrt{m_{\nu_1}}, \sqrt{m_{\nu_2}}, \sqrt{m_{\nu_3}}) U_{\text{PMNS}}^\dagger, \quad (11)$$

where V is a unitary matrix that diagonalizes M according to $M = V^\dagger \text{diag}(M_1, M_2, M_3) V^*$ and R is a complex orthogonal matrix that can be written as

$$R = \begin{pmatrix} c_2 c_3 & -c_1 s_3 - s_1 s_2 c_3 & s_1 s_3 - c_1 s_2 c_3 \\ c_2 s_3 & c_1 c_3 - s_1 s_2 s_3 & -s_1 c_3 - c_1 s_2 s_3 \\ s_2 & s_1 c_2 & c_1 c_2 \end{pmatrix}, \quad (12)$$

where $c_i \equiv \cos \theta_i$, $s_i \equiv \sin \theta_i$ and θ_1, θ_2 , and θ_3 are arbitrary complex angles.

TABLE I. Examples of neutrino mass spectrum in the ISS for various input parameters. The relevant nondiagonal $|(Y_\nu Y_\nu^\dagger)_{km}|$ elements are also included.

ISS examples	A	B	C
M_{R_1} (GeV)	1.5×10^4	1.5×10^2	1.5×10^2
M_{R_2} (GeV)	1.5×10^4	1.5×10^3	1.5×10^3
M_{R_3} (GeV)	1.5×10^4	1.5×10^4	1.5×10^4
$\mu_{X_{1,2,3}}$ (GeV)	5×10^{-8}	5×10^{-8}	5×10^{-8}
m_{ν_1} (eV)	0.1	0.1	0.1
$\theta_{1,2,3}$ (rad)	0, 0, 0	0, 0, 0	$\pi/4, 0, 0$
m_{n_1} (eV)	0.0998	0.0998	0.0998
m_{n_2} (eV)	0.1002	0.1002	0.1002
m_{n_3} (eV)	0.1112	0.1112	0.1112
m_{n_4} (GeV)	15014.99250747	150.1499250500	150.1499250500
m_{n_5} (GeV)	15014.99250752	150.1499250999	150.1499250999
m_{n_6} (GeV)	15015.04822299	1501.504822277	1501.587676006
m_{n_7} (GeV)	15015.04822304	1501.504822327	1501.587676056
m_{n_8} (GeV)	15016.70543659	15016.70543659	15015.87685358
m_{n_9} (GeV)	15016.70543664	15016.70543664	15015.87685363
$ (Y_\nu Y_\nu^\dagger)_{23} $	0.8	8.0	1.4
$ (Y_\nu Y_\nu^\dagger)_{12} $	0.2	1.7	0.3
$ (Y_\nu Y_\nu^\dagger)_{13} $	0.2	1.8	4.0

In summary, assuming $\mu_X = \text{diag}(\mu_{X_1}, \mu_{X_2}, \mu_{X_3})$ and $M_R = \text{diag}(M_{R_1}, M_{R_2}, M_{R_3})$ (hence, diagonal M), the input ISS parameters that will have to be fixed for our forthcoming study of the LFV rates are the following: $m_{\nu_{1,2,3}}$, $\mu_{X_{1,2,3}}$, $M_{R_{1,2,3}}$, $\theta_{1,2,3}$, and the entries of the U_{PMNS} matrix. For all the numerical analysis in this work, and in order to keep agreement with the experimental neutrino data, we will choose the lightest neutrino mass, here assumed to be m_{ν_1} , as a free input parameter and the other two light masses will be obtained from the two experimentally measured mass differences:

$$m_{\nu_2} = \sqrt{m_{\nu_1}^2 + \Delta m_{21}^2}, \quad m_{\nu_3} = \sqrt{m_{\nu_1}^2 + \Delta m_{31}^2}. \quad (13)$$

Similarly, the three light neutrino mixing angles will also be set to their measured values. For simplicity, we will set to zero the CP-violating phase of the U_{PMNS} matrix. Specifically, we have used the results of the global fit [10] leading to

$$\begin{aligned} \sin^2 \theta_{12} &= 0.306_{-0.012}^{+0.012}, & \Delta m_{21}^2 &= 7.45_{-0.16}^{+0.19} \times 10^{-5} \text{ eV}^2, \\ \sin^2 \theta_{23} &= 0.446_{-0.008}^{+0.008}, & \Delta m_{31}^2 &= 2.417_{-0.014}^{+0.014} \times 10^{-3} \text{ eV}^2, \\ \sin^2 \theta_{13} &= 0.0231_{-0.0019}^{+0.0019}, \end{aligned} \quad (14)$$

where we have assumed a normal hierarchy. Regarding the input lightest neutrino mass, m_{ν_1} , we have chosen it so that the effective electron neutrino mass in β decay agrees with the upper limit from the Mainz and Troitsk experiments [45,46],

$$m_\beta < 2.05 \text{ eV} \quad \text{at 95\% C.L.} \quad (15)$$

For the final numerical evaluation of the eigenvalues and eigenstates of the full 9×9 neutrino matrix, we have used our private *Mathematica* code that solves this system numerically, using all the previously mentioned input parameters and experimental data; and besides it also computes the Yukawa coupling matrix entries by using Eq. (11).

In order to illustrate the kind of generic neutrino spectra that one obtains in the ISS and that indeed follow the previously commented pattern, we have chosen in this section to show three examples of spectra whose most relevant parameters for the present work are collected in Table I.

We see clearly in these three examples that one typically gets the announced pattern of neutrino masses: three light neutrinos compatible with data and six heavy ones, with their heavy masses being degenerate in pairs to values close to M_{R_1} , M_{R_2} , and M_{R_3} respectively, and their tiny mass differences given approximately by μ_{X_1} , μ_{X_2} , and μ_{X_3} . We also see in this table that one can get sizable Yukawa couplings, in particular leading to large nondiagonal entries in flavor space, which are the relevant ones for the present work on lepton flavor violation. It should also be noticed that the heavy masses that are governing the size of these off diagonal entries are not those of M_R but those of Eq. (9), which are largely heavier, therefore leading in general to larger LFV rates in the ISS than in the seesaw I. For instance, the chosen examples in this table lead to large $|(Y_\nu Y_\nu^\dagger)_{23}|$ and $|(Y_\nu Y_\nu^\dagger)_{13}|$ in the $\mathcal{O}(1-10)$ range. $|(Y_\nu Y_\nu^\dagger)_{12}|$ in these examples is slightly smaller, $\leq \mathcal{O}(1)$.

One way of checking the validity of the parametrization in Eq. (11) is by comparing the input light neutrino mass values in this equation with the lightest output mass values obtained as a solution of Eq. (3). We have checked that the error on the light neutrino masses estimated with this

parametrization, meaning the differences between the input $m_{\nu_{1,2,3}}$ and the output $m_{n_{1,2,3}}$ masses, is below 10% and that the rotation matrix U_ν exhibits the required unitarity property. Furthermore, since a given set of input parameters can generate arbitrarily large Yukawa couplings, we will enforce their perturbativity by setting an upper limit on the entries of the neutrino Yukawa coupling matrix, given by

$$\frac{|Y_{ij}|^2}{4\pi} < 1.5, \quad (16)$$

for $i, j = 1, 2, 3$. This particular perturbativity condition has been used in the literature (see, for instance, SPHENO VERSION 2.0 [47]) but others more conservative than this have also been used (see, for instance, SPHENO VERSION 3.1 [48]). In the absence of a concrete evaluation of the next order corrections to the observable of interest (two-loop contributions to the LFBVD rates in our present case, which are beyond the scope of this article), the perturbativity condition is not uniquely defined and the choice of a specific criterion is an open issue. For instance, the use of a more conservative condition like $|Y_{ij}|^2 < 4\pi$ instead of Eq. (16) will not qualitatively change our results and will just lead to a decrease on the maximum LFBVD rates allowed by perturbativity,² by roughly a factor of (1/5), as can be easily estimated with our approximate formulas that will be presented later.

Finally, to complete our setup of the theoretical framework for our study of LFBV, we also have to specify all the relevant interactions that will enter in the computation of the LFBVD rates. We focus here on the relevant interactions involving neutrinos, which are the only ones that are assumed here to differ from those of the SM. These include the neutrino Yukawa couplings, the gauge couplings of the charged gauge bosons W^\pm to the lepton-neutrino pairs and the corresponding couplings of the charged Goldstone bosons, denoted here by G^\pm , to the lepton-neutrino pairs. In our one-loop computation of the LFBV rates we will choose to work in the mass basis for all the particles involved, with diagonal charged leptons, and taking into account the contributions from all the nine physical neutrinos. As for the gauge choice, we will choose the Feynman-t'Hooft gauge. Following the notation and presentation in [39,49], the relevant interactions are given in the mass basis by the following terms of the Lagrangian:

$$\begin{aligned} \mathcal{L}_{\text{int}}^{W^\pm} &= \frac{-g}{\sqrt{2}} W^{\mu-} \bar{l}_i B_{l_i n_j} \gamma_\mu P_L n_j + \text{H.c.}, \\ \mathcal{L}_{\text{int}}^H &= \frac{-g}{2m_W} H \bar{n}_i C_{n_i n_j} [m_{n_i} P_L + m_{n_j} P_R] n_j, \\ \mathcal{L}_{\text{int}}^{G^\pm} &= \frac{-g}{\sqrt{2}m_W} G^- [\bar{l}_i B_{l_i n_j} (m_{l_i} P_L - m_{n_j} P_R) n_j] + \text{H.c.}, \end{aligned} \quad (17)$$

where P_L and P_R are respectively the left- and right-chirality projectors, given by $(1 - \gamma^5)/2$ and $(1 + \gamma^5)/2$, and the coupling factors $B_{l_i n_j}$ ($i = 1, 2, 3, j = 1, \dots, 9$) and $C_{n_i n_j}$ ($i, j = 1, \dots, 9$) are defined in terms of the U_ν matrix of Eq. (3) by

$$B_{l_i n_j} = U_{ij}^{\nu*}, \quad (18)$$

$$C_{n_i n_j} = \sum_{k=1}^3 U_{ki}^\nu U_{kj}^{\nu*}. \quad (19)$$

III. COMPUTATION OF THE LFBV DECAY WIDTHS

In the calculation of the LFBV Higgs decay rates, we consider the full set of contributing one-loop diagrams, drawn in Fig. 1, and adapt to our present ISS case the complete one-loop formulas for the $\Gamma(H \rightarrow l_k \bar{l}_m)$ partial decay width, taken from [39], which we include, for completeness, also here. The relation between the form factors F_L and F_R given in the Appendix and the decay amplitude F is given by

$$iF = -ig\bar{u}_{l_k}(-p_2)(F_L P_L + F_R P_R)v_{l_m}(p_3), \quad (20)$$

where

$$F_L = \sum_{i=1}^{10} F_L^{(i)}, \quad F_R = \sum_{i=1}^{10} F_R^{(i)}, \quad (21)$$

and $p_1 = p_3 - p_2$ is the ingoing Higgs boson momentum.

The width for the LFBV Higgs decays is obtained from these form factors by

$$\begin{aligned} \Gamma(H \rightarrow l_k \bar{l}_m) &= \frac{g^2}{16\pi m_H} \sqrt{\left(1 - \left(\frac{m_{l_k} + m_{l_m}}{m_H}\right)^2\right) \left(1 - \left(\frac{m_{l_k} - m_{l_m}}{m_H}\right)^2\right)} \\ &\quad \times ((m_H^2 - m_{l_k}^2 - m_{l_m}^2)(|F_L|^2 + |F_R|^2) - 4m_{l_k} m_{l_m} \text{Re}(F_L F_R^*)). \end{aligned} \quad (22)$$

In this work we focus on the decays $H \rightarrow \mu\bar{\tau}, e\bar{\tau}, e\bar{\mu}$ and do not consider their related CP conjugate decays $H \rightarrow \tau\bar{\mu}, \tau\bar{e}, \mu\bar{e}$, which, in the presence of complex phases, could lead to different rates.

²We thank the referee for suggesting this other possible choice.

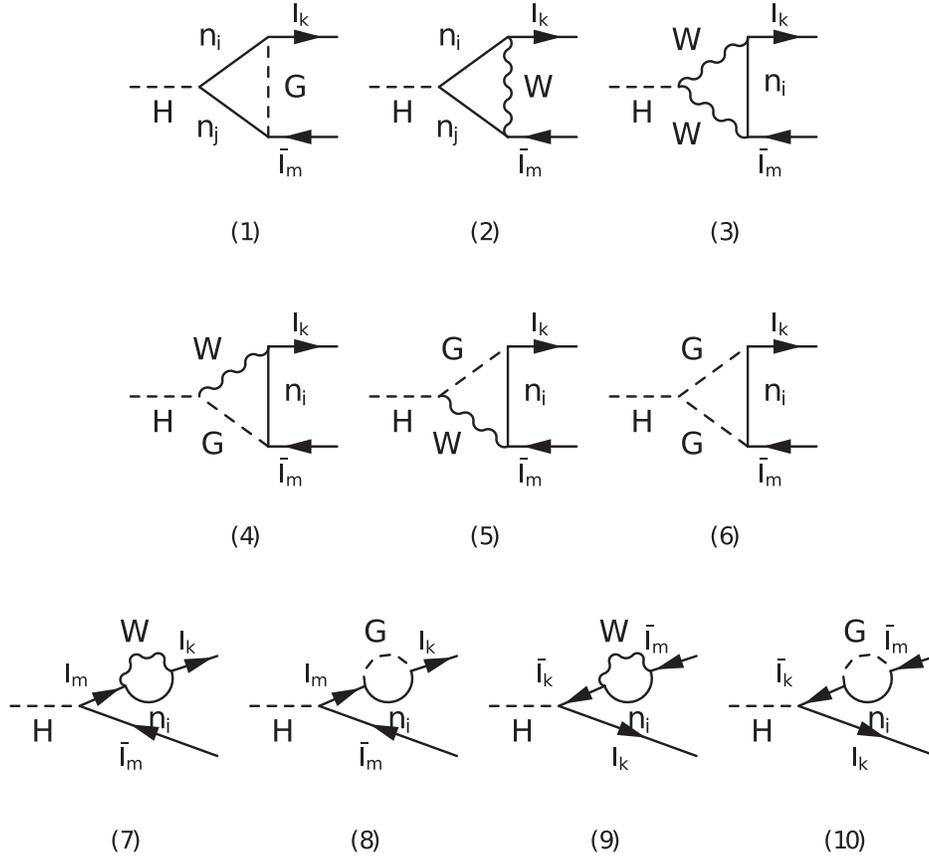


FIG. 1. One-loop contributing diagrams to the LFV Higgs decays $H \rightarrow l_k \bar{l}_m$ in the ISS with massive neutrinos $n_i (i = 1, \dots, 9)$.

We have explicitly checked that the only divergent contributions to the LFV Higgs decays arise from the diagrams (1), (8), and (10), and that they cancel among each other, in agreement with [39], giving rise to a total finite result. All these formulas for the LFV Higgs form factors and the LFV Higgs partial decay widths have been implemented into our private *Mathematica* code. In order to get numerical predictions for the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates we use $m_H = 126$ GeV and its corresponding SM total width is computed with FEYNHIGGS [50–52] including two-loop corrections.

At the same time that we analyze the LFV Higgs decays, we also compute the one-loop $l_m \rightarrow l_k \gamma$ decay rates within this same ISS framework and for the same input parameters, and check that these radiative decay rates are compatible with their present experimental 90% C.L. upper bounds [29,53]:

$$\text{BR}(\mu \rightarrow e \gamma) \leq 5.7 \times 10^{-13}, \quad (23)$$

$$\text{BR}(\tau \rightarrow e \gamma) \leq 3.3 \times 10^{-8}, \quad (24)$$

$$\text{BR}(\tau \rightarrow \mu \gamma) \leq 4.4 \times 10^{-8}. \quad (25)$$

In order to calculate these LFV radiative decay rates, which have been first computed in [54], we use the analytical

formulas appearing in [49] and [55] that have also been implemented in our code:

$$\text{BR}(l_m \rightarrow l_k \gamma) = \frac{\alpha_W^3 s_W^2}{256 \pi^2} \left(\frac{m_{l_m}}{M_W} \right)^4 \frac{m_{l_m}}{\Gamma_{l_m}} |G_{mk}|^2, \quad (26)$$

where Γ_{l_m} is the total decay width of the lepton l_m , and

$$G_{mk} = \sum_{i=1}^6 B_{mi}^* B_{ki} G_\gamma \left(\frac{m_{N_i}^2}{M_W^2} \right),$$

$$G_\gamma(x) = -\frac{2x^3 + 5x^2 - x}{4(1-x)^3} - \frac{3x^3}{2(1-x)^4} \log x, \quad (27)$$

where the sum above extends over the six heavy neutrinos, $N_{1,\dots,6} = n_{4,\dots,9}$. Notice that in the above formulas (26)–(27) the mass of the final lepton l_k has been neglected.

Finally, we offer a few words summarizing the various constraints that we have also implemented in our code. As we have already said, we have imposed the perturbativity constraint on the neutrino Yukawa couplings given in Eq. (16). Regarding the Higgs total width, it could be modified by the presence of sterile neutrinos with a mass below the Higgs boson mass that could open new invisible decays, as was studied in [56,57]. However, in this work,

we focus on the scenario where the new fermionic singlets have a mass above 200 GeV, thus escaping these constraints. If the right-handed neutrinos provide a sizable contribution to LFV processes, a non-negligible contribution to the lepton electric dipole moments (EDMs) could also be expected in the general case with complex phases. Thus, to avoid potential constraints from EDMs, we assume in most of this work that all mass matrices are real, as well as the PMNS matrix. The case of complex R matrix has also been considered in this work, but as it will be shown later (see Fig. 8) it is highly constrained by $\mu \rightarrow e\gamma$. Additional constraints might also arise from lepton universality tests. However, in the scenario that we consider where the sterile neutrinos are heavier than the Higgs boson, points that would be excluded by lepton universality tests are already excluded by $\mu \rightarrow e\gamma$, as can be seen in Fig. 8 of [19]. In the end, we found that the most constraining observable for our study is by far $\mu \rightarrow e\gamma$.

IV. NUMERICAL RESULTS FOR THE LFV RATES

In this section we present our numerical results for the LFV Higgs decay rates, $\text{BR}(H \rightarrow \mu\bar{\tau})$, $\text{BR}(H \rightarrow e\bar{\tau})$, and $\text{BR}(H \rightarrow e\bar{\mu})$, and we also compare them with the numerical results for the related radiative decay rates, $\text{BR}(\mu \rightarrow e\gamma)$, $\text{BR}(\tau \rightarrow e\gamma)$, and $\text{BR}(\tau \rightarrow \mu\gamma)$. First, we consider the simplest case of diagonal M_R and μ_X matrices and study all these LFV rates as functions of the more relevant ISS parameters, namely, M_R , μ_X , m_{ν_1} , and the R matrix angles, θ_i , trying to localize the areas of the parameter space where the LFV Higgs decays can be both large and respect the constraints on the radiative decays. The results of this first case will be presented in two generically different scenarios for the heavy neutrinos: (1) the case of (nearly) degenerate heavy neutrinos (first

subsection), and (2) the case of hierarchical heavy neutrinos (second subsection). In the last subsection, we then consider the most general case of nondiagonal μ_X and look for solutions within the ISS that lead to the largest and allowed LFVHD rates. We will then present our predictions for the maximal allowed $\text{BR}(H \rightarrow \mu\bar{\tau})$ and $\text{BR}(H \rightarrow e\bar{\tau})$ rates and will provide some specific examples for this kind of ISS scenario.

A. Degenerate heavy neutrinos

The case of (nearly) degenerate heavy neutrinos is implemented here by choosing degenerate entries in $M_R = \text{diag}(M_{R_1}, M_{R_2}, M_{R_3})$ and in $\mu_X = \text{diag}(\mu_{X_1}, \mu_{X_2}, \mu_{X_3})$, i.e., by setting $M_{R_i} = M_R$ and $\mu_{X_i} = \mu_X$ ($i = 1, 2, 3$).

First, we show in Fig. 2 the results for all the LFV rates as functions of the common right-handed neutrino mass parameter M_R for all the LFV Higgs decay channels (left panel) and for all the LFV radiative decay channels (right panel). Here we have fixed the other input parameters to $\mu_X = 10^{-7}$ GeV, $m_{\nu_1} = 0.1$ eV, and $R = I$. As expected, we find that the largest LFV Higgs decay rates are for $\text{BR}(H \rightarrow \mu\bar{\tau})$ and the largest radiative decay rates are for $\text{BR}(\tau \rightarrow \mu\gamma)$. We also see that, for this particular choice of input parameters, all the predictions for the LFV Higgs decays are allowed by the present experimental upper bounds on the three radiative decays (dashed horizontal lines in all our plots for the radiative decays) for all explored values of M_R in the interval $(200, 10^7)$ GeV. Besides, it shows clearly that the most constraining radiative decay at present is by far the $\mu \rightarrow e\gamma$ radiative decay. This is so in all the cases explored in this work, so whenever we wish to conclude on the allowed LFVHD rates we will focus mainly on this radiative channel.

Regarding the M_R dependence shown in Fig. 2, we clearly see that the LFVHD rates grow faster with M_R than

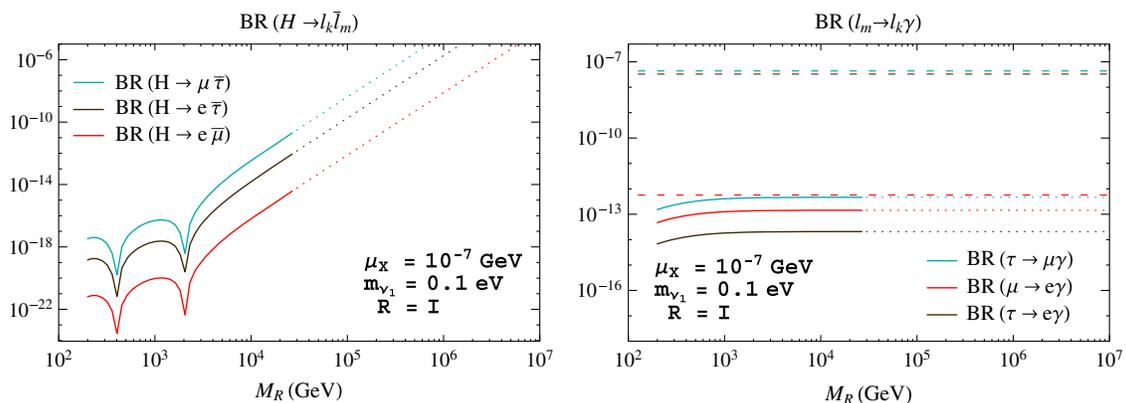


FIG. 2 (color online). Predictions for the LFV decay rates as functions of M_R in the degenerate heavy neutrinos case. Left panel: $\text{BR}(H \rightarrow \mu\bar{\tau})$ (upper blue line), $\text{BR}(H \rightarrow e\bar{\tau})$ (middle dark brown line), $\text{BR}(H \rightarrow e\bar{\mu})$ (lower red line). Right panel: $\text{BR}(\tau \rightarrow \mu\gamma)$ (upper blue line), $\text{BR}(\mu \rightarrow e\gamma)$ (middle red line), $\text{BR}(\tau \rightarrow e\gamma)$ (lower dark brown line). The other input parameters are set to $\mu_X = 10^{-7}$ GeV, $m_{\nu_1} = 0.1$ eV, $R = I$. The dotted lines in both panels indicate nonperturbative neutrino Yukawa couplings. The horizontal dashed lines in the right panel are the present (90% C.L.) upper bounds on the radiative decays: $\text{BR}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$ [53] (blue line), $\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$ [53] (dark brown line), $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29] (red line).

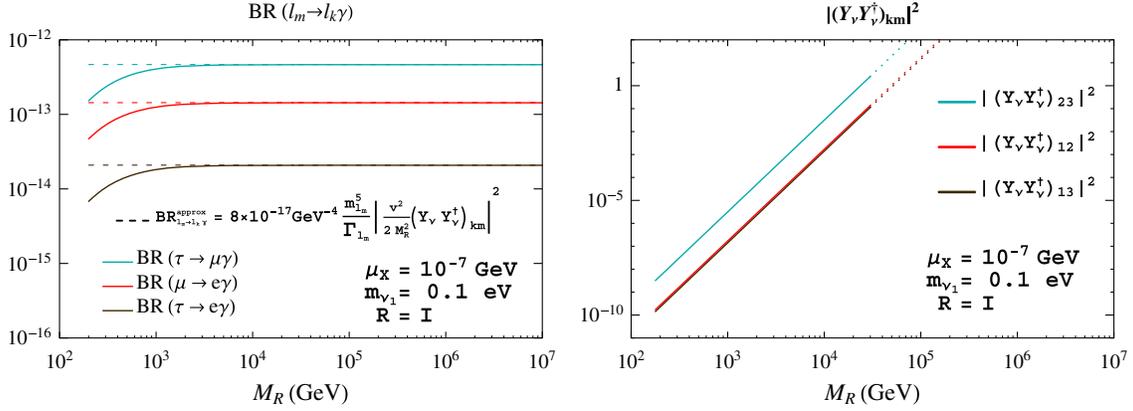


FIG. 3 (color online). Comparison of the full one-loop and approximate rates for the radiative decays $l_m \rightarrow l_k \gamma$ and their relation with the $(Y_\nu Y_\nu^\dagger)_{km}$ nondiagonal matrix elements in the degenerate heavy neutrinos case. Left panel: full one-loop rates (solid lines) and approximate rates (dashed lines) as functions of M_R . Right panel: $|(Y_\nu Y_\nu^\dagger)_{km}|^2$ versus M_R for $km = 23$ (blue line), $km = 12$ (red line), and $km = 13$ (dark brown line). Dotted lines indicate nonperturbative neutrino Yukawa couplings. The other input parameters are set to $\mu_X = 10^{-7}$ GeV, $m_{\nu_1} = 0.1$ eV, and $R = I$.

the radiative decays, which indeed tend to a constant value for M_R above $\sim 10^3$ GeV. In fact, the LFBVD rates can reach quite sizable values at the large M_R region of these plots, yet are allowed by the constraints on the radiative decays. For instance, we obtain $\text{BR}(H \rightarrow \mu \bar{\tau}) \sim 10^{-6}$ for $M_R = 4 \times 10^5$ GeV. However, our requirement of perturbativity for the neutrino Yukawa coupling entries, see Eq. (16), does not allow for such large M_R values leading to too-large Y_ν values in the framework of our parametrization of Eq. (11). Indeed, the exclusion region for M_R from perturbativity of Y_ν (given by the dotted lines in these plots), forbids these large M_R values. For the specific input parameter values of this Fig. 2, the forbidden values are for M_R above 3×10^4 GeV, and this leads to maximum allowed values of $\text{BR}(H \rightarrow \mu \bar{\tau}) \sim 2 \times 10^{-11}$, $\text{BR}(H \rightarrow e \bar{\tau}) \sim 10^{-12}$, and $\text{BR}(H \rightarrow e \bar{\mu}) \sim 5 \times 10^{-15}$.

The qualitatively different functional behavior with M_R of the LFBVD and the radiative rates shown by Fig. 2 is an interesting feature that we wish to explore further. Whereas the $\text{BR}(l_m \rightarrow l_k \gamma)$ rates follow the expected behavior with M_R as derived from their dependence with the relevant $(Y_\nu Y_\nu^\dagger)_{km}$ element, the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates do not follow this same pattern. As it is clearly illustrated in Fig. 3, the radiative decay rates can be well approximated for large M_R by a simple function of $|(Y_\nu Y_\nu^\dagger)_{km}|^2$ given by

$$\text{BR}_{l_m \rightarrow l_k \gamma}^{\text{approx}} = 8 \times 10^{-17} \frac{m_{l_m}^5 (\text{GeV}^5)}{\Gamma_{l_m} (\text{GeV})} \left| \frac{v^2}{2M_R^2} (Y_\nu Y_\nu^\dagger)_{km} \right|^2, \quad (28)$$

which provides predictions very close to the exact rates (given by the solid lines) for $M_R > 10^3$ GeV. Then we can understand the final constant behavior of all the radiative decay rates with M_R , since the $|(Y_\nu Y_\nu^\dagger)_{km}|^2$ elements grow with M_R approximately as M_R^4 in the parametrization here

used of Eq. (11), as can be seen in the plot on the right in Fig. 3. This simple behavior with M_R is certainly not the case of the LFBVD rates, and we conclude that these do not follow this same behavior with $|(Y_\nu Y_\nu^\dagger)_{km}|^2$. This different functional behavior of $\text{BR}(H \rightarrow l_k \bar{l}_m)$ with M_R will be further explored and clarified later.

Next we study the sensitivity in the LFBVD rates to other choices of μ_X . For this study we focus on the largest LFBVD rates, $\text{BR}(H \rightarrow \mu \bar{\tau})$, and on the most constraining $\text{BR}(\mu \rightarrow e \gamma)$ rates. In Fig. 4 we show the predictions for the LFBVD rates for different values of $\mu_X = (10^{-8}, 10^{-6}, 10^{-4}, 10^{-2})$ GeV. The other input parameters have been fixed here to $m_{\nu_1} = 0.1$ eV and $R = I$. On the left panel of Fig. 4 we see again the increase of $\text{BR}(H \rightarrow \mu \bar{\tau})$ as M_R grows, which is more pronounced in the region where M_R is large and μ_X is low, and, therefore, where the Yukawa couplings are large [see Eq. (11)]. We have checked that, in that region, the dominant diagrams are by far the divergent diagrams (1), (8), and (10), and that the $\text{BR}(H \rightarrow \mu \bar{\tau})$ rates grow as M_R^4 . In this plot, as well as in the previous plot of $\text{BR}(H \rightarrow l_k \bar{l}_m)$ in Fig. 2, we can also identify the appearance of different dips, which we have understood as destructive interferences among the various contributing diagrams. More precisely, we have checked that the dips that appear at large M_R and just before the M_R^4 growing region are due to partial cancellations between diagrams (1), (8), and (10), while the other dips that appear at lower M_R happen among diagrams (2)–(6) [(7) and (9) are subleading]. These last diagrams have relevant contributions to $\text{BR}(H \rightarrow \mu \bar{\tau})$ only for low values of the Yukawa couplings. We also observe a fast growth of the LFBVD Higgs rates as μ_X decreases from 10^{-2} GeV to 10^{-8} GeV. However, not all the values of M_R and μ_X are allowed, because they may generate nonperturbative Yukawa entries, expressed again in this figure by dotted lines. Therefore, the largest LFBVD Higgs rates permitted

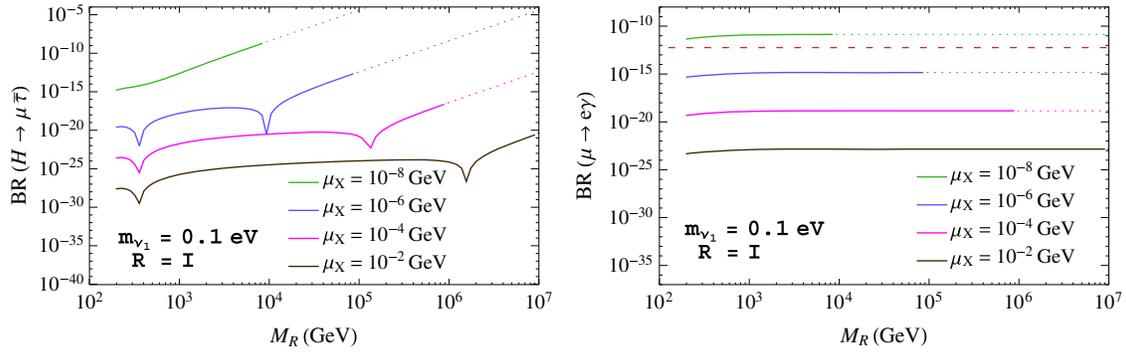


FIG. 4 (color online). Branching ratios of $H \rightarrow \mu\bar{\tau}$ (left panel) and $\mu \rightarrow e\gamma$ (right panel) as functions of M_R for different values of $\mu_X = (10^{-8}, 10^{-6}, 10^{-4}, 10^{-2})$ GeV from top to bottom. In both panels, $m_{\nu_1} = 0.1$ eV and $R = I$. The horizontal red dashed line denotes the current experimental upper bound for $\mu \rightarrow e\gamma$, $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29]. Dotted lines represent nonperturbative neutrino Yukawa couplings.

by our perturbativity requirements [Eq. (16)] are approximately $\text{BR}(H \rightarrow \mu\bar{\tau}) \sim 10^{-9}$, obtained for $\mu_X = 10^{-8}$ GeV and $M_R \simeq 10^4$ GeV. Larger values of M_R , for this choice of μ_X , would produce Yukawa couplings that are not perturbative.

Nevertheless, we must pay attention to the predictions of $\text{BR}(\mu \rightarrow e\gamma)$ for this choice of parameters, because they can be excluded by its quite restrictive present experimental upper bound, as shown on the right panel of Fig. 4. In this plot, the dependence of $\text{BR}(\mu \rightarrow e\gamma)$ on M_R is depicted, for the same choices of μ_X , m_{ν_1} , and R as in the left panel. The horizontal red dashed line denotes again its current upper bound; see Eq. (23). In addition to what we have already learned about the approximate behavior of the $\text{BR}(\mu \rightarrow e\gamma)$ rates going as $|(Y_\nu Y_\nu^\dagger)_{12}/M_R^2|^2$, which explains the constant behavior with M_R , we also learn from this figure about the generic behavior with μ_X , which leads to increasing LFV rates for decreasing μ_X values, for both LFNVD and radiative processes. In particular, we see that small values of $\mu_X \leq \mathcal{O}(10^{-8})$ GeV lead to $\text{BR}(\mu \rightarrow e\gamma)$ rates that are excluded by the present experimental upper bound. Taking this into account, the largest value of $\text{BR}(H \rightarrow \mu\bar{\tau})$, for the

choice of parameters fixed in Fig. 4, that is allowed by the $\text{BR}(\mu \rightarrow e\gamma)$ upper bound (this being more restrictive than the perturbativity requirement in this case) is $\sim 10^{-12}$, which is obtained for $M_R = 10^5$ GeV and $\mu_X = 10^{-6}$ GeV.

The behavior of $\text{BR}(H \rightarrow \mu\bar{\tau})$ and $\text{BR}(\mu \rightarrow e\gamma)$ as functions of μ_X , for several values of M_R , $m_{\nu_1} = 0.1$ eV, and $R = I$, is displayed in Fig. 5. As already seen in Fig. 4, both LFV rates decrease as μ_X grows; however, the functional dependence is not the same. The LFV radiative decay rates decrease as μ_X^{-2} , in agreement with the approximate expression (28), while the LFNVD rates go as μ_X^{-4} when the Yukawa couplings are large. For a fixed value of μ_X , the larger M_R is, the larger $\text{BR}(H \rightarrow \mu\bar{\tau})$ can be, while the prediction for $\text{BR}(\mu \rightarrow e\gamma)$ is the same for any value of M_R . We have already learned this independence of the LFV radiative decays on M_R from the previous figure, which can be easily confirmed on the right panel of Fig. 5, where all the lines for different values of M_R are superimposed. We observe again the existence of dips in the left panel of Fig. 5. We also see in this figure that the smallest value of μ_X allowed by the $\text{BR}(\mu \rightarrow e\gamma)$ upper bound is $\mu_X \sim 5 \times 10^{-8}$ GeV, which is directly translated to a

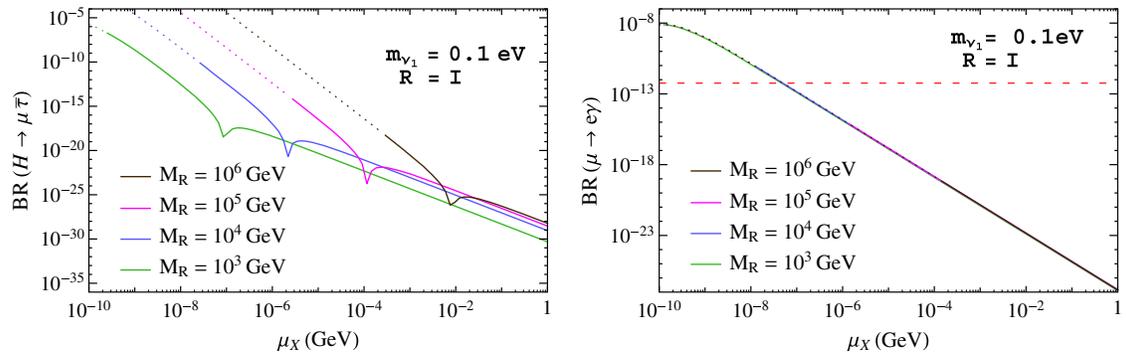


FIG. 5 (color online). Branching ratios of $H \rightarrow \mu\bar{\tau}$ (left panel) and $\mu \rightarrow e\gamma$ (right panel) as functions of μ_X for different values of $M_R = (10^6, 10^5, 10^4, 10^3)$ GeV from top to bottom. In both panels, $m_{\nu_1} = 0.1$ eV and $R = I$. The horizontal red dashed line denotes the current experimental upper bound for $\mu \rightarrow e\gamma$, $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29]. Dotted lines represent nonperturbative neutrino Yukawa couplings.

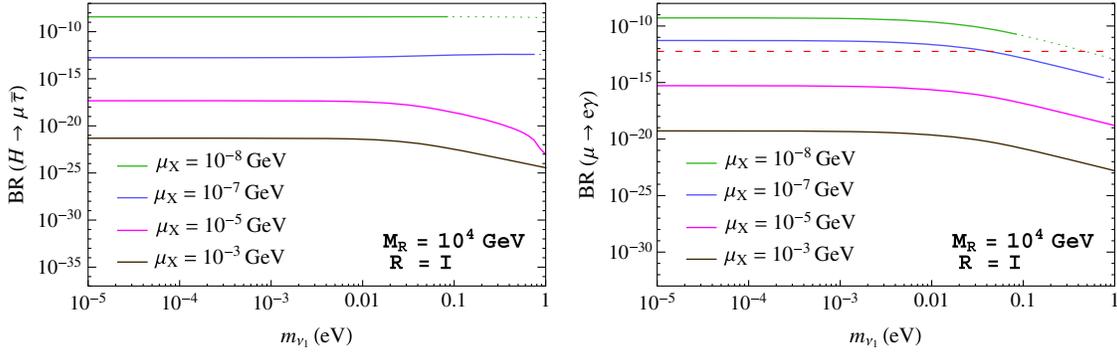


FIG. 6 (color online). Branching ratios of $H \rightarrow \mu\bar{\tau}$ (left panel) and $\mu \rightarrow e\gamma$ (right panel) as functions of m_{ν_1} for different values of $\mu_X = (10^{-8}, 10^{-7}, 10^{-5}, 10^{-3})$ GeV from top to bottom. In both panels, $M_R = 10^4$ GeV and $R = I$. The horizontal red dashed line denotes the current experimental upper bound for $\mu \rightarrow e\gamma$, $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29]. Dotted lines represent nonperturbative neutrino Yukawa couplings [see Eq. (16)].

maximum allowed value of $\text{BR}(H \rightarrow \mu\bar{\tau}) \sim 10^{-11}$, for $M_R = 10^4$ GeV.

The dependence of $\text{BR}(H \rightarrow \mu\bar{\tau})$ and $\text{BR}(\mu \rightarrow e\gamma)$ on the lightest neutrino mass m_{ν_1} is studied in Fig. 6, for several values of μ_X with $M_R = 10^4$ GeV and $R = I$. For the chosen parameters in this figure, a similar dependence on m_{ν_1} is observed in both observables, in which there is a flat behavior with m_{ν_1} except for values

of $m_{\nu_1} \gtrsim 0.01$ eV. For these values, the LFV rates decrease as m_{ν_1} grows.

The behavior of $\text{BR}(l_m \rightarrow l_k\gamma)$ with m_{ν_1} can be understood from the fact that the flavor violation arises from the nondiagonal terms of $(Y_\nu Y_\nu^\dagger)_{km}$. In the simplified case of real R and U_{PMNS} matrices, for diagonal and degenerate M_R and μ_X , and by using Eqs. (11) and (9), we find the following simple expression for the nondiagonal km elements:

$$\frac{v^2(Y_\nu Y_\nu^\dagger)_{km}}{M_R^2} \approx \begin{cases} \frac{1}{\mu_X} (U_{\text{PMNS}} \sqrt{\Delta m^2} U_{\text{PMNS}}^T)_{km}, & \text{for } m_{\nu_1}^2 \ll |\Delta m_{ij}^2|, \\ \frac{1}{\mu_X} \frac{(U_{\text{PMNS}} \Delta m^2 U_{\text{PMNS}}^T)_{km}}{2m_{\nu_1}}, & \text{for } m_{\nu_1}^2 \gg |\Delta m_{ij}^2|, \end{cases} \quad (29)$$

where we have defined

$$\Delta m^2 \equiv \text{diag}(0, \Delta m_{21}^2, \Delta m_{31}^2), \quad (30)$$

and we have expanded properly m_{ν_2} and m_{ν_3} in Eq. (13) in terms of m_{ν_1} and Δm_{ij}^2 . Therefore, using Eqs. (28)–(30), we conclude that the $\text{BR}(\mu \rightarrow e\gamma)$ rates have a flat behavior with m_{ν_1} for low values of $m_{\nu_1} \lesssim 0.01$ eV, but they decrease with m_{ν_1} for larger values, explaining the observed behavior in Fig. 6.

By taking into account all the behaviors learned above, we have tried to find an approximate simple formula that could explain the main features of the $\text{BR}(H \rightarrow \mu\bar{\tau})$ rates. As we have already said, in contrast to what we have seen for the LFV radiative decays in Eq. (28), a simple functional dependence being proportional to $|(Y_\nu Y_\nu^\dagger)_{23}|^2$ is not enough to describe our results for the $\text{BR}(H \rightarrow \mu\bar{\tau})$ rates. Considering that, in the region where the Yukawa couplings are large, the LFVHD rates are dominated by diagrams (1), (8), and (10), we have looked for a simple expression that could properly fit the contributions from these dominant diagrams. From this fit we have found the following approximate formula:

$$\text{BR}_{H \rightarrow \mu\bar{\tau}}^{\text{approx}} = 10^{-7} \frac{v^4}{M_R^4} |(Y_\nu Y_\nu^\dagger)_{23} - 5.7(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{23}|^2, \quad (31)$$

which turns out to work reasonably well. In Fig. 7 we show the predicted rates of $\text{BR}(H \rightarrow \mu\bar{\tau})$ with (1) the full one-loop formulas (dashed lines); (2) taking just the contributions from diagrams (1), (8), and (10) of Fig. 1 (solid lines); and (3) using Eq. (31) (dotted lines). We see clearly that this Eq. (31) reproduces extremely well the contributions from diagrams (1), (8), and (10) and approximates reasonably well the full rates. The approximation is pretty good indeed for the M_R region above the dips. The change of functional behavior with M_R in the two different M_R regions, from nearly flat with M_R in the approximate result to fast growing as $\sim M_R^4$, also gives a reasonable approach to the full result, as well as the appearance of dips. The location of the dips is however not so accurately described by the approximate formula, since in the region where the cancellation among the diagrams (1), (8), and (10) takes place the other diagrams (not considered in the fit) also contribute. Overall, we find the approximate formula given

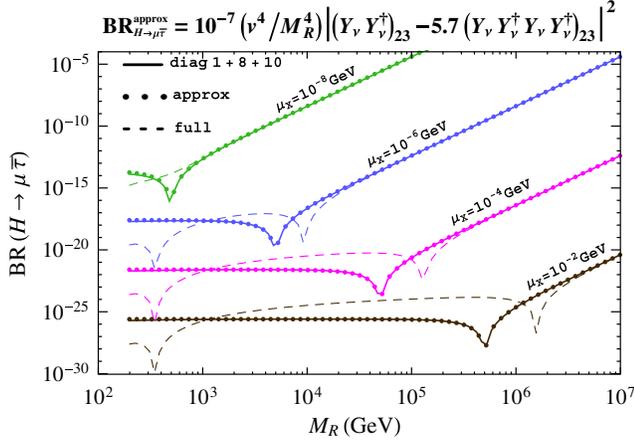


FIG. 7 (color online). Comparison between the predicted rates for $\text{BR}(H \rightarrow \mu\bar{\tau})$ taking (1) the full one-loop formulas (dashed lines); (2) just the contributions from diagrams (1), (8), and (10) of Fig. 1 (solid lines); and (3) the approximate formula of Eq. (31) (dotted lines).

by Eq. (31) very useful for generic estimates in the ISS, which could also be applied to other parametrizations of the neutrino Yukawa couplings.

This particular choice for the fitting function can be easily understood using the electroweak interaction basis of Eq. (1) and applying the mass insertion approximation (MIA). Looking at the finite contribution coming from diagrams (1), (8), and (10), we can see that, at the lowest order in the MIA, the Higgs decay amplitude has a similar behavior to the dimension-six operator that governs the LFV radiative decays, which is proportional to

$$\frac{v^2 (Y_\nu Y_\nu^\dagger)_{km}}{M_R^2}. \quad (32)$$

However, there are other contributions to the Higgs decays that are not present in the case of the radiative decays,

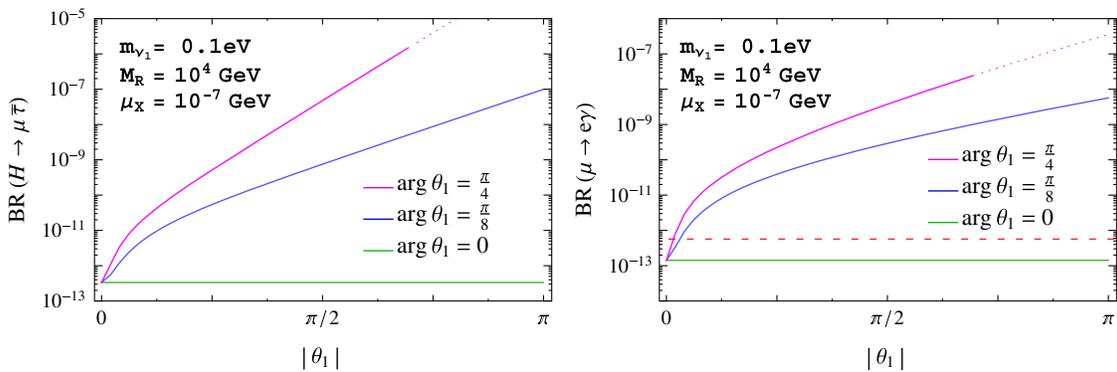


FIG. 8 (color online). Branching ratios of $H \rightarrow \mu\bar{\tau}$ (left panel) and $\mu \rightarrow e\gamma$ (right panel) as functions of $|\theta_1|$ for different values of $\arg\theta_1$. In both panels, $M_R = 10^4$ GeV, $\mu_X = 10^{-7}$ GeV, and $m_{\nu_1} = 0.1$ eV. The horizontal red dashed line denotes the current experimental upper bound for $\mu \rightarrow e\gamma$, $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29]. Dotted lines represent nonperturbative neutrino Yukawa couplings [see Eq. (16)].

owing to the different chiral structure of the lepton flavor violating operators. For example, having two mass insertions of LR type, one in each internal neutrino line of a loop like that of diagram 1, will give a contribution to the amplitude proportional to

$$\frac{v^2 (Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{km}}{M_R^2}. \quad (33)$$

Then, using again Eqs. (11) and (9), we find the following simple expression:

$$\frac{v^2 (Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{km}}{M_R^2} = \frac{M_R^2}{v^2 \mu_X^2} (U_{\text{PMNS}} \Delta m^2 U_{\text{PMNS}}^T)_{km}. \quad (34)$$

Thus, we can clearly see from the above result that the second contribution in Eq. (31) is the one that dominates at large M_R and low μ_X , i.e., at large Yukawa couplings, and, indeed, it reproduces properly the behavior of $\text{BR}(H \rightarrow \mu\bar{\tau})$ in this limit, with $\text{BR} \propto M_R^4 / \mu_X^4$. It is also independent of m_{ν_1} , explaining the flat behavior in Fig. 6 for low values of μ_X . Moreover, if the two contributions in Eq. (31) have opposite signs, they will interfere destructively, leading to a dip in the decay rate when both contributions are of the same size. From Eqs. (29) and (34), we can deduce that the position of the dip should verify $M_R^{-2} \mu_X \sim \text{constant}$, which is the behavior observed at large M_R in Figs. 4–5. The other dips, which appear for $M_R \simeq 300$ GeV in Fig. 4, come from a destructive interference between the other diagrams, as we have said.

Next, we display in Fig. 8 the dependence of the $H \rightarrow \mu\bar{\tau}$ and $\mu \rightarrow e\gamma$ decay rates on $|\theta_1|$ for different values of $\arg\theta_1 = 0, \pi/8, \pi/4$, with $M_R = 10^4$ GeV, $\mu_X = 10^{-7}$ GeV, and $m_{\nu_1} = 0.1$ eV. First of all, we highlight the flat behavior of both LFV rates with $|\theta_1|$ for real R matrix ($\arg\theta_1 = 0$), which is a direct consequence of the degeneracy of M_R and μ_X . In other words, the LFV rates for the degenerate heavy neutrinos case are independent of R if it is

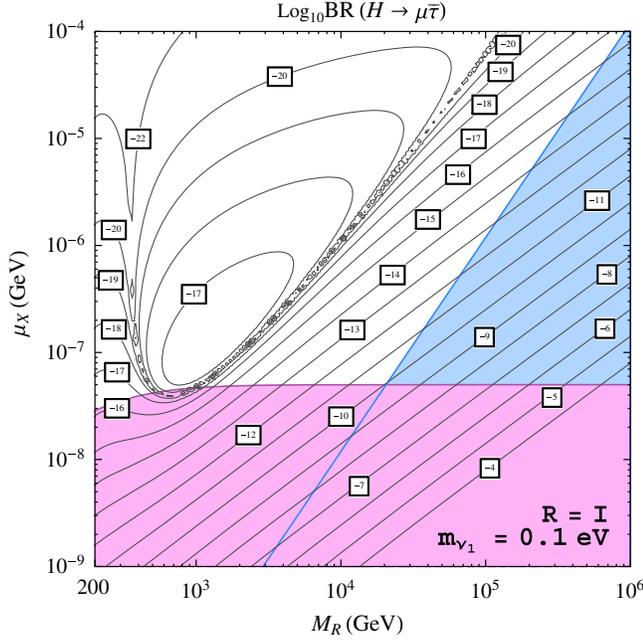


FIG. 9 (color online). Contour lines of $\text{BR}(H \rightarrow \mu\bar{\tau})$ in the (M_R, μ_X) plane for $R = I$ and $m_{\nu_1} = 0.1$ eV. The horizontal area in pink is excluded by the upper bound on $\text{BR}(\mu \rightarrow e\gamma)$. The oblique area in blue is excluded by the perturbativity requirement of the neutrino Yukawa couplings.

real. Once we abandon the real case and consider values of $\arg\theta_1$ different from zero, a strong dependence on $|\theta_1|$ appears. The larger $|\theta_1|$ and/or $\arg\theta_1$ are, the larger the LFV rates become. On the other hand, only values of $|\theta_1|$ lower than $\pi/32$ with $\arg\theta_1 = \pi/8$ in this figure are allowed by the $\mu \rightarrow e\gamma$ constraint, which allows us to reach values of $\text{BR}(H \rightarrow \mu\bar{\tau}) \sim 10^{-12}$ at the most. We have also explored the LFV rates as functions of complex θ_2 and

θ_3 and we have reached similar conclusions as for θ_1 . Therefore, by choosing complex $\theta_{1,2,3}$ the LFV Higgs decay rates that are allowed by the upper bounds on the radiative decays do not increase with respect to the real case, which is equal to the previous $R = I$ reference case, due to the independence on real R , as we have already said.

Once we have studied the behavior of all the LFV observables considered here with the most relevant parameters, we next present the results for the maximum allowed LFV Higgs decay rates in the case of heavy degenerate neutrinos. The plot in Fig. 9 shows the contour lines of $\text{BR}(H \rightarrow \mu\bar{\tau})$ in the (M_R, μ_X) plane for $R = I$ and $m_{\nu_1} = 0.1$ eV. The horizontal area in pink is excluded by not respecting the present upper bound on $\text{BR}(\mu \rightarrow e\gamma)$. The oblique area in blue is excluded by not respecting the perturbativity of the neutrino Yukawa couplings. These contour lines summarize the previously learned behavior with M_R and μ_X , which lead to the largest values for the LFVHD rates in the bottom right-hand corner of the plot, i.e., at large M_R and small μ_X . We also notice the appearance of dips in the (M_R, μ_X) plane that correspond to the previously commented dips in the previous figures. The most important conclusion from this contour plot is that the maximum allowed LFVHD rate is approximately $\text{BR}(H \rightarrow \mu\bar{\tau}) \sim 10^{-10}$ and it is found for $M_R \sim 2 \times 10^4$ GeV and $\mu_X \sim 5 \times 10^{-8}$ GeV. We have found similar conclusions for $\text{BR}(H \rightarrow e\bar{\tau})$.

B. Hierarchical heavy neutrinos

The case of hierarchical heavy neutrinos refers here to hierarchical masses among generations and it is implemented by choosing hierarchical entries in the $M_R = \text{diag}(M_{R_1}, M_{R_2}, M_{R_3})$ matrix. As for the $\mu_X = \text{diag}(\mu_{X_1}, \mu_{X_2}, \mu_{X_3})$ matrix that introduces the tiny splitting within the heavy masses in the same generation we choose

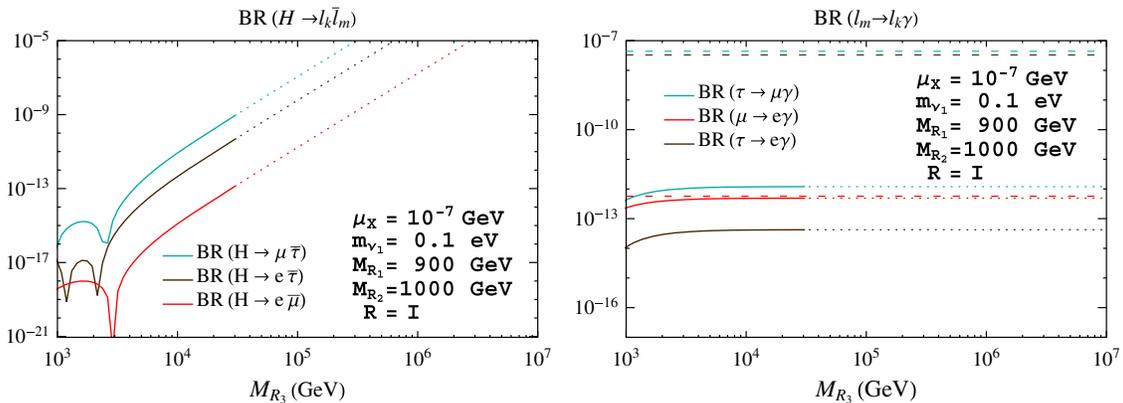


FIG. 10 (color online). Predictions for the LFV decay rates as functions of M_{R_3} in the hierarchical heavy neutrinos case with $M_{R_1} < M_{R_2} < M_{R_3}$. Left panel: $\text{BR}(H \rightarrow \mu\bar{\tau})$ (upper blue line), $\text{BR}(H \rightarrow e\bar{\tau})$ (middle dark brown line), $\text{BR}(H \rightarrow e\bar{\mu})$ (lower red line). Right panel: $\text{BR}(\tau \rightarrow \mu\gamma)$ (upper blue line), $\text{BR}(\mu \rightarrow e\gamma)$ (middle red line), $\text{BR}(\tau \rightarrow e\gamma)$ (lower dark brown line). The other input parameters are set to $\mu_X = 10^{-7}$ GeV, $m_{\nu_1} = 0.1$ eV, $M_{R_1} = 900$ GeV, $M_{R_2} = 1000$ GeV, and $R = I$. The dotted lines in both panels indicate nonperturbative neutrino Yukawa couplings. The horizontal dashed lines in the right panel are the present (90% C.L.) upper bounds on the radiative decays: $\text{BR}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$ [53] (blue line), $\text{BR}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$ [53] (dark brown line), and $\text{BR}(\mu \rightarrow e\gamma) < 5.7 \times 10^{-13}$ [29] (red line).

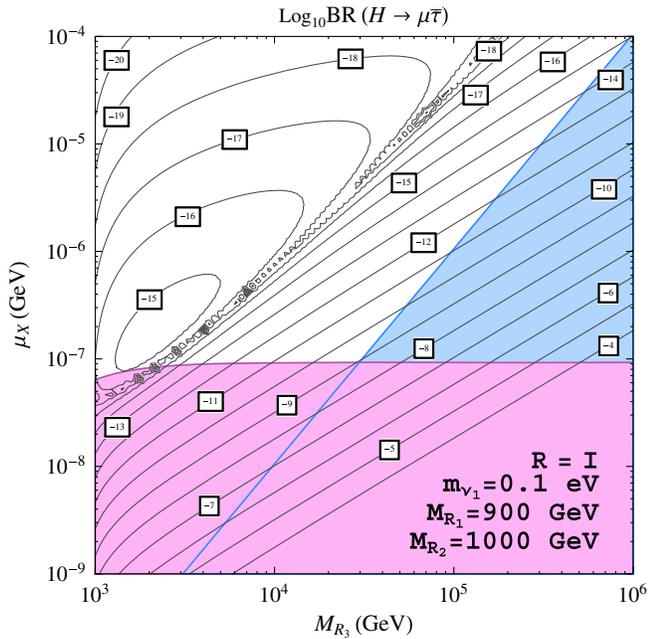


FIG. 11 (color online). Contour lines of $\text{BR}(H \rightarrow \mu\bar{\tau})$ in the (M_{R_3}, μ_X) plane for $R = I$, $m_{\nu_1} = 0.1$ eV, $M_{R_1} = 900$ GeV, and $M_{R_2} = 1000$ GeV. The horizontal area in pink is disallowed by the upper bound on $\text{BR}(\mu \rightarrow e\gamma)$. The oblique area in blue is disallowed by the perturbativity requirement of the neutrino Yukawa couplings.

it here to be degenerate, $\mu_{X_{1,2,3}} = \mu_X$. We focus on the normal hierarchy $M_{R_1} < M_{R_2} < M_{R_3}$, since we have found similar conclusions for other hierarchies.

The results for the LFV rates in the $M_{R_1} < M_{R_2} < M_{R_3}$ hierarchical case are shown in Fig. 10. This figure shows that the behavior of the LFV rates in the hierarchical case with respect to the heaviest neutrino mass M_{R_3} is very similar to the one found previously for the degenerate case with respect to the common M_R . The $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates

grow fast with M_{R_3} at large $M_{R_3} > 3000$ GeV, whereas the $\text{BR}(l_m \rightarrow l_k \gamma)$ rates stay flat with M_{R_3} . Again, there are dips in the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates due to the destructive interferences among the contributing diagrams. We also observe in this plot that, for the chosen parameters, the size that the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates can reach in this hierarchical scenario is larger than in the previous degenerate case. For instance, $\text{BR}(H \rightarrow \mu\bar{\tau})$ reaches 10^{-9} at $M_{R_3} = 3 \times 10^4$ GeV, to be compared with 10^{-10} at $M_R = 3 \times 10^4$ GeV that we got in Fig. 2 for the degenerate case. We have found this same behavior of enhanced LFVHD rates by approximately one order of magnitude in the hierarchical case as compared to the degenerate case in most of the explored parameter space regions.

This same enhancement can also be seen in the contour plot in Fig. 11 where the maximum allowed $\text{BR}(H \rightarrow \mu\bar{\tau})$ rates reach values up to about 10^{-9} for $M_{R_1} = 900$ GeV, $M_{R_2} = 1000$ GeV, $M_{R_3} = 3 \times 10^4$ GeV, $\mu_X = 10^{-7}$ GeV, and $R = I$. Finally, since in the hierarchical case, in contrast to the degenerate case, there is a dependence on the R matrix even if it is real, we have also explored the behavior with the real $\theta_{1,2,3}$ angles. We have found that for this particular hierarchy, $M_{R_1} < M_{R_2} < M_{R_3}$, there is near independence with θ_3 but there is a clear dependence with θ_1 and θ_2 , as it is illustrated in Fig. 12. These plots show that the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates for $\theta_{1,2} \neq 0$ can indeed increase or decrease with respect to the reference $R = I$ case. In particular, for $0 < \theta_1 < \pi$ we find that $\text{BR}(H \rightarrow \mu\bar{\tau})$ is always lower than for $R = I$, whereas $\text{BR}(H \rightarrow e\bar{\tau})$ can be one order of magnitude larger than for $R = I$ if θ_1 is near $\pi/2$. For the case of $0 < \theta_2 < \pi$, we find again that $\text{BR}(H \rightarrow \mu\bar{\tau})$ is always lower than for $R = I$, and $\text{BR}(H \rightarrow e\bar{\tau})$ can be one order of magnitude larger than for $R = I$ if θ_2 is near $\pi/4$. In this latter case, it is interesting to notice that the region of θ_2 close to $\pi/4$ where $\text{BR}(H \rightarrow e\bar{\tau})$ reaches the maximum value close to 10^{-9}

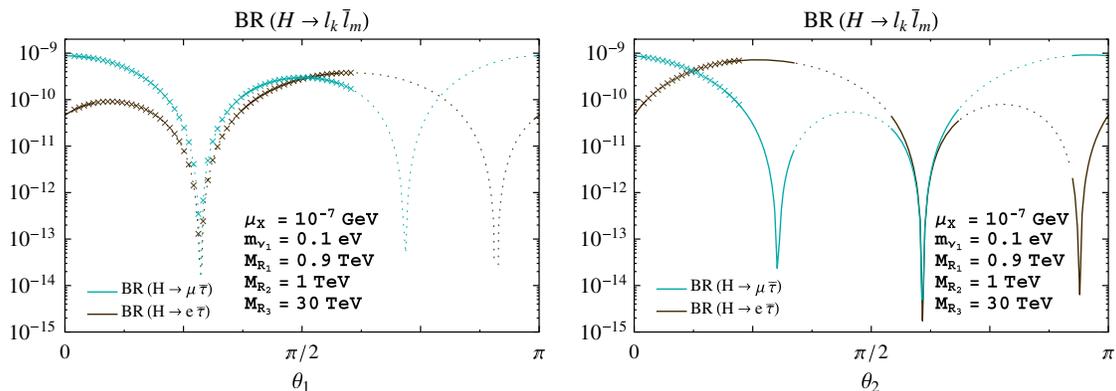


FIG. 12 (color online). Predictions for $\text{BR}(H \rightarrow \mu\bar{\tau})$ (blue lines) and $\text{BR}(H \rightarrow e\bar{\tau})$ (dark brown lines) rates as a function of real θ_1 (left panel) and θ_2 (right panel). The other input parameters are set to $\mu_X = 10^{-7}$ GeV, $m_{\nu_1} = 0.1$ eV, $M_{R_1} = 0.9$ TeV, $M_{R_2} = 1$ TeV, $M_{R_3} = 30$ TeV, $\theta_2 = \theta_3 = 0$ in the left panel and $\theta_1 = \theta_3 = 0$ in the right panel. The dotted lines indicate nonperturbative neutrino Yukawa couplings and the crossed lines are excluded by the present upper bound on $\text{BR}(\mu \rightarrow e\gamma)$. The solid lines are allowed by all the constraints.

is allowed by all the constraints. The results for the other decay $\text{BR}(H \rightarrow e\bar{\mu})$ are not shown here because they again give much smaller rates, as in the degenerate case. We have also tried other choices for the hierarchies among the three heavy masses $M_{R_{1,2,3}}$ and we have found similar conclusions.

C. ISS scenarios with large LFV Higgs decay rates

In this section we explore the implications on LFV Higgs decays of going beyond the simplest previous hypothesis of diagonal μ_X and M_R mass matrices in the ISS model. In particular, given the interesting possibility of decoupling the low energy neutrino physics from the LFV physics in this ISS model, by the proper choice of the input parameters, we will look for specific ISS scenarios with non-diagonal μ_X while keeping diagonal M_R that can provide the largest LFV Higgs decay rates and at the same time be compatible with the neutrino data and the present experimental upper bounds on the radiative decays. Here, we will focus on the case of degenerate M_R and will explore only the LFV Higgs decay channels with the largest rates, namely, $H \rightarrow \mu\bar{\tau}$ and $H \rightarrow e\bar{\tau}$.

In order to localize the class of scenarios leading to large and allowed LFVHD rates, we first make a rough estimate of the expected maximal rates for the $H \rightarrow \mu\bar{\tau}$ channel by using our approximate formula of Eq. (31), which is given just in terms of the neutrino Yukawa coupling matrix Y_ν and M_R . On the other hand, in order to keep the predictions for the radiative decays below their corresponding experimental upper bounds, we need to require a maximum value for the nondiagonal $(Y_\nu Y_\nu^\dagger)_{ij}$ entries. By using our approximate formula of Eq. (28) and the present bounds in Eqs. (23)–(25), we get

$$v^2(Y_\nu Y_\nu^\dagger)_{12}^{\max}/M_R^2 \sim 2.5 \times 10^{-5}, \quad (35)$$

$$v^2(Y_\nu Y_\nu^\dagger)_{13}^{\max}/M_R^2 \sim 0.015, \quad (36)$$

$$v^2(Y_\nu Y_\nu^\dagger)_{23}^{\max}/M_R^2 \sim 0.017. \quad (37)$$

Then, in order to simplify our search, and given the above relative strong suppression of the 12 element, it seems reasonable to neglect it against the other off diagonal elements. In that case, by assuming $(Y_\nu Y_\nu^\dagger)_{12} \approx 0$ we get

$$(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{23} \approx (Y_\nu Y_\nu^\dagger)_{22}(Y_\nu Y_\nu^\dagger)_{23} + (Y_\nu Y_\nu^\dagger)_{23}(Y_\nu Y_\nu^\dagger)_{33}, \quad (38)$$

and the approximate formula of Eq. (31) can then be rewritten as follows:

$$\text{BR}_{H \rightarrow \mu\bar{\tau}}^{\text{approx}} = 10^{-7} \left| \frac{v^2}{M_R^2} (Y_\nu Y_\nu^\dagger)_{23} \right|^2 \times |1 - 5.7((Y_\nu Y_\nu^\dagger)_{22} + (Y_\nu Y_\nu^\dagger)_{33})|^2. \quad (39)$$

This equation clearly shows that the maximal $\text{BR}(H \rightarrow \mu\bar{\tau})$ rates are obtained for the maximum allowed values of $(Y_\nu Y_\nu^\dagger)_{23}$, $(Y_\nu Y_\nu^\dagger)_{22}$, and $(Y_\nu Y_\nu^\dagger)_{33}$. Thus, before going to any specific assumption for the Y_ν texture we can already conclude on these maximal rates, by setting the maximum allowed value for $v^2(Y_\nu Y_\nu^\dagger)_{23}^{\max}/M_R^2$ to that given in Eq. (37) and fixing the values of $(Y_\nu Y_\nu^\dagger)_{22}$ and $(Y_\nu Y_\nu^\dagger)_{33}$ to their maximum allowed values that are implied by our perturbativity condition in Eq. (16),

$$(Y_\nu Y_\nu^\dagger)_{33}^{\max} = (Y_\nu Y_\nu^\dagger)_{22}^{\max} = (Y_\nu Y_\nu^\dagger)_{11}^{\max} = 18\pi. \quad (40)$$

This leads to our approximate prediction for the maximal rates:

$$\text{BR}_{H \rightarrow \mu\bar{\tau}}^{\max} \approx 10^{-5}. \quad (41)$$

We obtain similar conclusions for the $H \rightarrow e\bar{\tau}$ channel. This can be easily derived from the corresponding approximate formula that we have also checked to work quite well in this case:

$$\text{BR}_{H \rightarrow e\bar{\tau}}^{\text{approx}} = 10^{-7} \frac{v^4}{M_R^4} |(Y_\nu Y_\nu^\dagger)_{13} - 5.7(Y_\nu Y_\nu^\dagger Y_\nu Y_\nu^\dagger)_{13}|^2, \quad (42)$$

leading for $(Y_\nu Y_\nu^\dagger)_{12} \approx 0$ to

$$\text{BR}_{H \rightarrow e\bar{\tau}}^{\text{approx}} = 10^{-7} \left| \frac{v^2}{M_R^2} (Y_\nu Y_\nu^\dagger)_{13} \right|^2 \times |1 - 5.7((Y_\nu Y_\nu^\dagger)_{11} + (Y_\nu Y_\nu^\dagger)_{33})|^2, \quad (43)$$

and, therefore, by using Eqs. (36) and (40) we also obtain

$$\text{BR}_{H \rightarrow e\bar{\tau}}^{\max} \approx 10^{-5}. \quad (44)$$

Having such large and allowed by data LFVHD rates of the order of 10^{-5} for either $H \rightarrow \mu\bar{\tau}$ or $H \rightarrow e\bar{\tau}$ is clearly of great interest if the high number of Higgs events mentioned in the introduction is finally achieved.

In the rest of this section we will look for specific examples where the above settings can be reached. In particular, we will devote our attention to the search of particular choices of Y_ν that fulfill all the above requirements. Once some specific inputs are provided for Y_ν and M_R , the proper μ_X matrix that ensures the agreement between low energy neutrino predictions and data can be easily obtained by solving Eqs. (7)–(8), which leads to

$$\mu_X = M_R^T m_D^{-1} U_{\text{PMNS}}^* m_\nu U_{\text{PMNS}}^T m_D^{-1} M_R \quad (45)$$

with $m_D = vY_\nu$ and $m_\nu = \text{diag}(m_{\nu_1}, m_{\nu_2}, m_{\nu_3})$. It should be noted that for a generic Y_ν texture this μ_X will be in general nondiagonal, as announced at the beginning of this section.

For our purpose of looking for specific examples of Y_ν maximizing the LFVHD rates and for simplicity in that search, we focus next on the case of real Y_ν where

$(Y_\nu Y_\nu^\dagger) = (Y_\nu Y_\nu^T)$, and we use a geometrical picture where the elements of the Yukawa matrix can be interpreted as the components of three vectors that we call here \mathbf{e} , $\boldsymbol{\mu}$, and $\boldsymbol{\tau}$:

$$Y_\nu = \begin{pmatrix} Y_{\nu 11} & Y_{\nu 12} & Y_{\nu 13} \\ Y_{\nu 21} & Y_{\nu 22} & Y_{\nu 23} \\ Y_{\nu 31} & Y_{\nu 32} & Y_{\nu 33} \end{pmatrix} \equiv \begin{pmatrix} \mathbf{e} \\ \boldsymbol{\mu} \\ \boldsymbol{\tau} \end{pmatrix}. \quad (46)$$

Then the relevant matrix for our LFV observables can be written as

$$YY^T = \begin{pmatrix} |\mathbf{e}|^2 & \mathbf{e} \cdot \boldsymbol{\mu} & \mathbf{e} \cdot \boldsymbol{\tau} \\ \boldsymbol{\mu} \cdot \mathbf{e} & |\boldsymbol{\mu}|^2 & \boldsymbol{\mu} \cdot \boldsymbol{\tau} \\ \boldsymbol{\tau} \cdot \mathbf{e} & \boldsymbol{\tau} \cdot \boldsymbol{\mu} & |\boldsymbol{\tau}|^2 \end{pmatrix}, \quad (47)$$

and consequently it can be completely determined by setting six parameters: the modulus of the three vectors ($|\mathbf{e}|, |\boldsymbol{\mu}|, |\boldsymbol{\tau}|$) and the three angles ($\theta_{\mu e}, \theta_{\tau e}, \theta_{\tau \mu}$) defining their relative orientations. It should be noticed, however, that a real 3×3 Yukawa matrix should contain nine parameters. The missing three parameters can be understood in terms of an additional rotation O of the 3 vectors, which does not change their relative angles, and therefore it has no physical consequences for our observables. Thus, one can write, generically, the neutrino Yukawa matrix as a product of two matrices A and O , with $OO^T = O^T O = 1$:

$$Y_\nu \equiv A \cdot O, \quad (48)$$

$$Y_\nu Y_\nu^T = AA^T. \quad (49)$$

We can use then this freedom to choose the two orthogonal vectors ($\mathbf{e}, \boldsymbol{\mu}$) in two of the axes, for instance \mathbf{e} in the X axis and $\boldsymbol{\mu}$ in the Y axis, so that we can write

$$A = \begin{pmatrix} e & 0 & 0 \\ 0 & \mu & 0 \\ \tau c_{\tau e} & \tau c_{\tau \mu} & \tau \sqrt{1 - c_{\tau e}^2 - c_{\tau \mu}^2} \end{pmatrix}, \quad (50)$$

with $|\mathbf{e}| \equiv e$, $|\boldsymbol{\mu}| \equiv \mu$, $|\boldsymbol{\tau}| \equiv \tau$, $c_{\tau e} \equiv \cos \theta_{\tau e}$, and $c_{\tau \mu} \equiv \cos \theta_{\tau \mu}$. Then in our simple geometrical parametrization of the Yukawa matrix we get

$$Y_\nu Y_\nu^T = AA^T = \begin{pmatrix} e^2 & 0 & e\tau c_{\tau e} \\ 0 & \mu^2 & \mu\tau c_{\tau \mu} \\ e\tau c_{\tau e} & \mu\tau c_{\tau \mu} & \tau^2 \end{pmatrix}, \quad (51)$$

which shows explicitly our requirement of $(Y_\nu Y_\nu^T)_{12} = 0$ and whose simple form helps in the choice of the textures maximizing the LFVHD rates. For instance, it is obvious that by choosing parallel or antiparallel $\boldsymbol{\tau}$ and $\boldsymbol{\mu}$ vectors, i.e., $c_{\tau \mu} = \pm 1$ we will get maximal $\text{BR}(H \rightarrow \mu \bar{\tau})$, whereas, by choosing parallel or antiparallel $\boldsymbol{\tau}$ and \mathbf{e} vectors, i.e., $c_{\tau e} = \pm 1$ we will get maximal $\text{BR}(H \rightarrow e \bar{\tau})$. We also see that we will not be able to get maximal rates for both channels simultaneously, since the imposed orthogonality of \mathbf{e} and $\boldsymbol{\mu}$ implies some correlations among the LFV in the $e - \tau$ and $\mu - \tau$ channels. Thus, for a given input $\theta_{\tau \mu}$, the maximum LFV rates in the $e - \tau$ channel will occur at the correlated value $\theta_{\tau e} = \pi/2 - \theta_{\tau \mu}$, and vice versa. As a consequence, the maximum in $\text{BR}(H \rightarrow \mu \bar{\tau})$ implies a minimum in $\text{BR}(H \rightarrow e \bar{\tau})$, and a maximum in $\text{BR}(H \rightarrow e \bar{\tau})$ implies a minimum in $\text{BR}(H \rightarrow \mu \bar{\tau})$. We find this result an interesting feature of this kind of texture.

Finally, we provide some illustrative examples with large LFVHD rates. All of them fulfil $(Y_\nu Y_\nu^T)_{12} = 0$ and $(Y_\nu Y_\nu^T Y_\nu Y_\nu^T)_{12} = 0$, therefore ensuring the practically vanishing LFV in the $\mu - e$ sector, i.e., leading all to $\text{BR}(\mu \rightarrow e \gamma) \sim 0$ and $\text{BR}(H \rightarrow e \bar{\mu}) \sim 0$.

(1) Examples with large LFV $\mu - \tau$.

The following three textures, $Y_{\tau \mu}^{(1)}$, $Y_{\tau \mu}^{(2)}$, and $Y_{\tau \mu}^{(3)}$, provide large LFV in the $\mu - \tau$ sector, and practically vanishing LFV in the $e - \tau$ sector, since they all have $\mathbf{e} \cdot \boldsymbol{\tau} = 0$:

$$Y_{\tau \mu}^{(1)} = \sqrt{6\pi} \begin{pmatrix} 0 & 1 & -1 \\ 0.9 & 1 & 1 \\ 1 & 1 & 1 \end{pmatrix}, \quad Y_{\tau \mu}^{(2)} = \sqrt{6\pi} \begin{pmatrix} 0 & 1 & 1 \\ 1 & 1 & -1 \\ -1 & 1 & -1 \end{pmatrix}, \quad Y_{\tau \mu}^{(3)} = \sqrt{6\pi} \begin{pmatrix} 0 & -1 & 1 \\ -1 & 1 & 1 \\ 0.8 & 0.5 & 0.5 \end{pmatrix}. \quad (52)$$

These textures $Y_{\tau \mu}^{(1,2,3)}$ can be obtained by choosing $A_{\tau \mu}^{(1,2,3)}$ matrices like the A matrix in Eq. (50) with $e^{(1,2,3)} = (\sqrt{12\pi}, \sqrt{12\pi}, \sqrt{12\pi})$, $\mu^{(1,2,3)} = (\sqrt{17.4\pi}, \sqrt{18\pi}, \sqrt{18\pi})$, $\tau^{(1,2,3)} = (\sqrt{18\pi}, \sqrt{18\pi}, \sqrt{6.4\pi})$, and $c_{\tau \mu}^{(1,2,3)} = (0.98, 0.33, 0.025)$, respectively; and then applying the corresponding rotation $O_{\tau \mu} = (A_{\tau \mu}^{-1})Y_{\tau \mu}$.

(2) Examples with large LFV $e - \tau$.

The following three textures, $Y_{\tau e}^{(1)}$, $Y_{\tau e}^{(2)}$, and $Y_{\tau e}^{(3)}$, provide large LFV in the $e - \tau$ sector, and practically vanishing LFV in the $\mu - \tau$ sector, since they all have $\boldsymbol{\tau} \cdot \boldsymbol{\mu} = 0$:

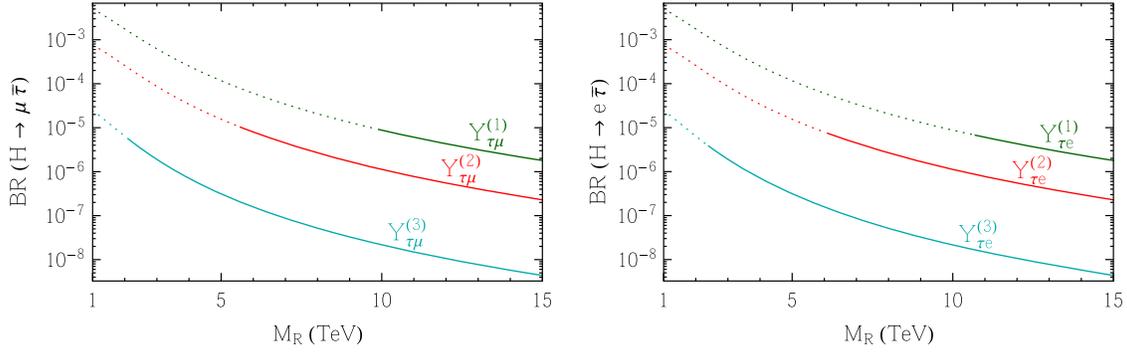


FIG. 13 (color online). Examples in the ISS with large LFBVD rates obtained using the full one-loop formulas. Left panel: $\text{BR}(H \rightarrow \mu\bar{\tau})$ versus M_R for $Y_{\tau\mu}^{(1)}$ (upper green line), $Y_{\tau\mu}^{(2)}$ (middle red line) and $Y_{\tau\mu}^{(3)}$ (lower blue line) given in Eq. (52). Dotted lines indicate disallowed input values leading to $\text{BR}(\tau \rightarrow \mu\gamma)$ above the present experimental bound in Eq. (25). Right panel: $\text{BR}(H \rightarrow e\bar{\tau})$ versus M_R for $Y_{\tau e}^{(1)}$ (upper green line), $Y_{\tau e}^{(2)}$ (middle red line), and $Y_{\tau e}^{(3)}$ (lower blue line) given in Eq. (53). Dotted lines indicate disallowed input values leading to $\text{BR}(\tau \rightarrow e\gamma)$ above the present experimental bound in Eq. (24). Solid lines indicate predictions allowed by all the constraints.

$$Y_{\tau e}^{(1)} = \sqrt{6\pi} \begin{pmatrix} 0.9 & 1 & 1 \\ 0 & 1 & -1 \\ 1 & 1 & 1 \end{pmatrix}, \quad Y_{\tau e}^{(2)} = \sqrt{6\pi} \begin{pmatrix} 1 & 1 & -1 \\ 0 & 1 & 1 \\ -1 & 1 & -1 \end{pmatrix}, \quad Y_{\tau e}^{(3)} = \sqrt{6\pi} \begin{pmatrix} -1 & 1 & 1 \\ 0 & -1 & 1 \\ 0.8 & 0.5 & 0.5 \end{pmatrix}. \quad (53)$$

These textures $Y_{\tau e}^{(1,2,3)}$ can be obtained by choosing $A_{\tau e}^{(1,2,3)}$ matrices like the A matrix in Eq. (50) with $e^{(1,2,3)} = (\sqrt{17.4\pi}, \sqrt{18\pi}, \sqrt{18\pi})$, $\mu^{(1,2,3)} = (\sqrt{12\pi}, \sqrt{12\pi}, \sqrt{12\pi})$, $\tau^{(1,2,3)} = (\sqrt{18\pi}, \sqrt{18\pi}, \sqrt{6.4\pi})$, and $c_{\tau e}^{(1,2,3)} = (0.98, 0.33, 0.025)$, respectively; and then applying the corresponding rotation $O_{\tau e} = A_{\tau e}^{-1} Y_{\tau e}$.

We present our predictions for the LFBVD rates in our above selected examples in Fig. 13 as a function of the degenerate right-handed neutrino mass M_R . For these predictions we have used the full one-loop formulas. We have also checked that the approximate formulas in Eqs. (31) and (42) give a quite good estimate of these BRs in the large M_R region, with deviations with respect to the full result smaller than 10% for $M_R > 6$ TeV. The main conclusion from these plots is that with these specific Yukawa textures one can indeed reach large LFBVD rates of the order of 10^{-5} and still be compatible with all the bounds from radiative decays. The textures $Y_{\tau\mu}$ ($Y_{\tau e}$) corresponding to lower $c_{\tau\mu}$ ($c_{\tau e}$) allow for lower M_R values and vice versa. Thus, $Y_{\tau\mu}^{(1)}$ ($Y_{\tau e}^{(1)}$) leads the maximum allowed $\text{BR}(H \rightarrow \mu\bar{\tau})$ ($\text{BR}(H \rightarrow e\bar{\tau})$) rates for M_R around 10 TeV (11 TeV), $Y_{\tau\mu}^{(2)}$ ($Y_{\tau e}^{(2)}$) around 5.5 TeV (6 TeV), and $Y_{\tau\mu}^{(3)}$ ($Y_{\tau e}^{(3)}$) around 2 TeV (2.5 TeV).

The above textures are just some selected examples, among many possibilities, but the important feature is that they will all provide maximum allowed rates of around 10^{-5} . We have also checked that by selecting examples with hierarchical $M_{R_1}, M_{R_2}, M_{R_3}$ masses we do not obtain larger maximum allowed rates. Thus, our conclusion is quite generic for the maximum allowed LFBVD rates in the

ISS models. The other generic feature that is worth mentioning is that, given the correlated rates found between $\text{BR}_{\max}(H \rightarrow \mu\bar{\tau})$ and $\text{BR}_{\max}(\tau \rightarrow \mu\gamma)$ [similarly, between $\text{BR}_{\max}(H \rightarrow e\bar{\tau})$ and $\text{BR}_{\max}(\tau \rightarrow e\gamma)$], if an improved future upper experimental bound on $\text{BR}(\tau \rightarrow \mu\gamma)$ [similarly, on $\text{BR}(\tau \rightarrow e\gamma)$] is provided, this will be intermediately translated into a smaller maximal allowed value for $\text{BR}(H \rightarrow \mu\bar{\tau})$ [similarly, for $\text{BR}(H \rightarrow e\bar{\tau})$].

V. CONCLUSIONS

In this paper we have studied the LFV Higgs decays $H \rightarrow l_k \bar{l}_m$ within the context of the inverse seesaw model where three additional pairs (one pair per generation) of massive right-handed singlet neutrinos are added to the standard model particle content. We have presented a full one-loop computation of the $\text{BR}(H \rightarrow l_k \bar{l}_m)$ rates for the three possible channels, $l_k \bar{l}_m = \mu\bar{\tau}, e\bar{\tau}, e\bar{\mu}$, and have analyzed in full detail the predictions as functions of the various relevant ISS parameters. The most relevant parameters for LFV have been found to be M_R and Y_ν . In addition, we have required that the input parameters of this ISS model be compatible with the present neutrino data and other constraints, like perturbativity of the neutrino Yukawa couplings and the present bounds for the three radiative decays $\mu \rightarrow e\gamma$, $\tau \rightarrow e\gamma$, and $\tau \rightarrow \mu\gamma$. To take control on this last requirement, we have studied along this paper in parallel to the LFV Higgs decays the correlated one-loop predictions for the radiative decays, $l_m \rightarrow l_k \gamma$, within this same ISS context. We have explored the ISS parameter space and consider both kinds of scenarios for the right-handed neutrinos, with either degenerate or hierarchical masses. First, we have considered the

simplest case of diagonal M_R and μ_X matrices. In this case, we conclude that the largest maximum LFV Higgs decay rates within the ISS that are allowed by all the constraints are for $\text{BR}(H \rightarrow e\bar{\tau})$ and $\text{BR}(H \rightarrow \mu\bar{\tau})$ and reach at most 10^{-10} for the degenerate heavy neutrino case and 10^{-9} for the hierarchical case. Second, we have explored more general ISS scenarios with nondiagonal μ_X matrices that we have found more promising for LFVHD searches. These can also accommodate successfully the low energy neutrino data, and be compatible with the present bounds on the radiative decays and with the perturbativity bounds on the neutrino Yukawa couplings. We have demonstrated that in this kind of ISS scenarios there are solutions with much larger allowed LFVHD rates than in the previous cases, leading to maximal allowed rates of around 10^{-5} for either $\text{BR}(H \rightarrow \mu\bar{\tau})$ or $\text{BR}(H \rightarrow e\bar{\tau})$. Assuming in addition CP conservation in these scenarios, the final LFVHD rates should be multiplied by a factor of 2 if the CP conjugate channels $\text{BR}(H \rightarrow \tau\bar{\mu})$ and $\text{BR}(H \rightarrow \tau\bar{e})$ are also considered. Finally, we have also provided a few particular examples where the predicted rates with the full one-loop formulas indeed give such a large LFVHD rate of $\sim 10^{-5}$, for values of M_R in the interval (1 TeV, 10 TeV). We certainly find these LFVHD rates and M_R values interesting, given the expected extremely high statistics of up to hundreds of millions of Higgs bosons that

will be produced at the future colliders, allowing for searches of rare Higgs decays, and the potential of LHC to explore new particles at the TeV region.

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APPENDIX ANALYTICAL EXPRESSIONS OF THE FORM FACTORS

For completeness, we collect here the analytical results for the LFV Higgs decay form factors in the Feynman 't Hooft gauge and expressed in the physical basis. These formulas are taken from Ref. [39].

$$\begin{aligned}
 F_L^{(1)} &= \frac{g^2}{4m_W^3 16\pi^2} B_{l_k n_i} B_{l_m n_j}^* \{m_{l_k} m_{n_j} [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) + i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j})] \tilde{C}_0 \\
 &\quad + (C_{12} - C_{11}) [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) (-m_{l_k}^3 m_{n_j} - m_{n_i} m_{l_k} m_{l_m}^2 + m_{n_i} m_{n_j}^2 m_{l_k} + m_{n_i}^2 m_{n_j} m_{l_k}) \\
 &\quad + i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j}) (-m_{l_k}^3 m_{n_j} + m_{n_i} m_{l_k} m_{l_m}^2 - m_{n_i} m_{n_j}^2 m_{l_k} + m_{n_i}^2 m_{n_j} m_{l_k})\}, \\
 F_R^{(1)} &= \frac{g^2}{4m_W^3 16\pi^2} B_{l_k n_i} B_{l_m n_j}^* \{m_{n_i} m_{l_m} [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) - i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j})] \tilde{C}_0 \\
 &\quad + C_{12} [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) (m_{l_m}^3 m_{n_i} - m_{n_i} m_{n_j}^2 m_{l_m} - m_{n_i}^2 m_{n_j} m_{l_m} + m_{n_j} m_{l_k}^2 m_{l_m}) \\
 &\quad + i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j}) (-m_{l_m}^3 m_{n_i} + m_{n_i} m_{n_j}^2 m_{l_m} - m_{n_i}^2 m_{n_j} m_{l_m} + m_{n_j} m_{l_k}^2 m_{l_m})\},
 \end{aligned}$$

where $C_{11,12} = C_{11,12}(m_{l_k}^2, m_H^2, m_W^2, m_{n_i}^2, m_{n_j}^2)$ and $\tilde{C}_0 = \tilde{C}_0(m_{l_k}^2, m_H^2, m_W^2, m_{n_i}^2, m_{n_j}^2)$.

$$\begin{aligned}
 F_L^{(2)} &= \frac{g^2}{2m_W 16\pi^2} B_{l_k n_i} B_{l_m n_j}^* m_{l_k} \{-m_{n_j} [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) + i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j})] C_0 \\
 &\quad + (C_{12} - C_{11}) [(m_{n_i} + m_{n_j})^2 \text{Re}(C_{n_i n_j}) + i(m_{n_j} - m_{n_i})^2 \text{Im}(C_{n_i n_j})]\}, \\
 F_R^{(2)} &= -\frac{g^2}{2m_W 16\pi^2} B_{l_k n_i} B_{l_m n_j}^* m_{l_m} \{m_{n_i} [(m_{n_i} + m_{n_j}) \text{Re}(C_{n_i n_j}) - i(m_{n_j} - m_{n_i}) \text{Im}(C_{n_i n_j})] C_0 \\
 &\quad + C_{12} [(m_{n_i} + m_{n_j})^2 \text{Re}(C_{n_i n_j}) + i(m_{n_j} - m_{n_i})^2 \text{Im}(C_{n_i n_j})]\},
 \end{aligned}$$

where $C_{0,11,12} = C_{0,11,12}(m_{l_k}^2, m_H^2, m_W^2, m_{n_i}^2, m_{n_j}^2)$.

$$\begin{aligned}
 F_L^{(3)} &= \frac{g^2}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_k} m_W (C_{11} - C_{12}), \\
 F_R^{(3)} &= \frac{g^2}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_m} m_W C_{12},
 \end{aligned}$$

where $C_{11,12} = C_{11,12}(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$.

$$F_L^{(4)} = -\frac{g^2}{4m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_k} \{m_{l_m}^2 (C_{12} - 2C_{11}) + m_{n_i}^2 (C_{11} - C_{12}) - m_{n_i}^2 C_0\},$$

$$F_R^{(4)} = -\frac{g^2}{4m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_m} \{\tilde{C}_0 + 2m_{l_m}^2 C_{11} + m_{n_i}^2 C_{12} + (m_{l_k}^2 - 2m_H^2)(C_{11} - C_{12}) + 2m_{n_i}^2 C_0\},$$

where $C_{0,11,12} = C_{0,11,12}(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$ and $\tilde{C}_0 = \tilde{C}_0(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$.

$$F_L^{(5)} = -\frac{g^2}{4m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_k} \{\tilde{C}_0 + 2m_{n_i}^2 C_0 + (m_{n_i}^2 + 2m_{l_k}^2)C_{11} + (m_{l_m}^2 - m_{n_i}^2 - 2m_H^2)C_{12}\},$$

$$F_R^{(5)} = \frac{g^2}{4m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_m} \{m_{n_i}^2 C_0 + m_{l_k}^2 C_{11} + (m_{l_k}^2 - m_{n_i}^2)C_{12}\},$$

where $C_{0,11,12} = C_{0,11,12}(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$ and $\tilde{C}_0 = \tilde{C}_0(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$.

$$F_L^{(6)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_k} m_H^2 \{m_{n_i}^2 (C_0 + C_{11}) + (m_{l_m}^2 - m_{n_i}^2)C_{12}\},$$

$$F_R^{(6)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* m_{l_m} m_H^2 \{m_{n_i}^2 (C_0 + C_{12}) + m_{l_k}^2 (C_{11} - C_{12})\},$$

where $C_{0,11,12} = C_{0,11,12}(m_{l_k}^2, m_H^2, m_{n_i}^2, m_W^2, m_W^2)$.

$$F_L^{(7)} = \frac{g^2}{2m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_m}^2 m_{l_k}}{m_{l_k}^2 - m_{l_m}^2} B_1,$$

$$F_R^{(7)} = \frac{g^2}{2m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_k}^2 m_{l_m}}{m_{l_k}^2 - m_{l_m}^2} B_1,$$

$$F_L^{(8)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_k}}{m_{l_k}^2 - m_{l_m}^2} \{m_{l_m}^2 (m_{l_k}^2 + m_{n_i}^2) B_1 + 2m_{n_i}^2 m_{l_m}^2 B_0\},$$

$$F_R^{(8)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_m}}{m_{l_k}^2 - m_{l_m}^2} \{m_{l_k}^2 (m_{l_m}^2 + m_{n_i}^2) B_1 + m_{n_i}^2 (m_{l_k}^2 + m_{l_m}^2) B_0\},$$

where $B_{0,1} = B_{0,1}(m_{l_k}^2, m_{n_i}^2, m_W^2)$.

$$F_L^{(9)} = \frac{g^2}{2m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_m}^2 m_{l_k}}{m_{l_m}^2 - m_{l_k}^2} B_1,$$

$$F_R^{(9)} = \frac{g^2}{2m_W} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_k}^2 m_{l_m}}{m_{l_m}^2 - m_{l_k}^2} B_1,$$

$$F_L^{(10)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_k}}{m_{l_m}^2 - m_{l_k}^2} \{m_{l_m}^2 (m_{l_k}^2 + m_{n_i}^2) B_1 + m_{n_i}^2 (m_{l_k}^2 + m_{l_m}^2) B_0\},$$

$$F_R^{(10)} = \frac{g^2}{4m_W^3} \frac{1}{16\pi^2} B_{l_k n_i} B_{l_m n_i}^* \frac{m_{l_m}}{m_{l_m}^2 - m_{l_k}^2} \{m_{l_k}^2 (m_{l_m}^2 + m_{n_i}^2) B_1 + 2m_{n_i}^2 m_{l_k}^2 B_0\},$$

where $B_{0,1} = B_{0,1}(m_{l_m}^2, m_{n_i}^2, m_W^2)$.

$$\tilde{C}_0(p_2^2, p_1^2, m_1^2, m_2^2, m_3^2) \equiv B_0(p_1^2, m_2^2, m_3^2) + m_1^2 C_0(p_2^2, p_1^2, m_1^2, m_2^2, m_3^2).$$

Notice that we have corrected the global sign of $F_L^{(1)}$, which was a typo in [39].

In all the previous formulas, summation over neutrino indices is understood. These run as $i, j = 1, \dots, 9$ for neutrinos, and $k, m = 1, \dots, 3$ for charged leptons. The loop function conventions are as in [58–60].

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