I. INTRODUCTION

Double-walled carbon nanotubes (DWNTs), consisting of two coaxial and weakly van der Waals coupled single-walled carbon nanotubes (SWNTs), are one of the most ideal and fundamental systems to study the effects of interwall coupling on the physical properties in one-dimensional structures. The properties of DWNTs are related to (i) the individual nature of the constituent SWNTs, which can be either metallic (M) or semiconductor (SC), (ii) the van der Waals interactions, depending on the wall-to-wall distance, typically ranging from 0.3 to 0.4 nm [1–6], and (iii) the matching of the atomic lattices of inner and outer tubes (moire patterns), which plays a decisive role in determining the electronic structure of DWNTs even without any commensurability [7,8]. It has even been shown recently that the mechanical interlayer coupling steers their structural properties and favors certain configurations [9].

Regarding potential applications, e.g., in photonics or biology, a key property is inner semiconducting tube (ISCT) photoluminescence (PL) from measurements performed on four individual freestanding index-identified double-walled carbon nanotubes (DWNTs). Based on thorough Rayleigh scattering, Raman scattering, and PL experiments, we are able to demonstrate that the ISCT PL is observed with a quantum yield estimated to be a few 10−6 independent of the semiconducting or metallic nature of the outer tube. This result is mainly attributed to ultrafast exciton transfer from the inner to outer tube. Furthermore, by carrying out PL excitation experiments on the (14,1)@(15,12) DWNT, we show that the ISCT PL can be detected through the optical excitation of the outer tube, indicating that the exciton transfer can also occur in the opposite way.

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across open-slit structures (50 × 1000 μm²) fabricated on silicon substrates. The details of the synthesis of individual DWNTs are given in the Supplemental Material [36].

The DWNTs were characterized by high resolution transmission electron microscopy (HRTEM) and ED and investigated using Raman, Rayleigh and PL measurements [36]. A DWNT structure is uniquely defined by the chiral indices (n_i, m_i) and (n_o, m_o) of its constituent inner and outer layers, respectively [37]. Such DWNT is denoted as (n_i, m_i)@(n_o, m_o). Here, the structure identification procedure follows the one described in Ref. [38] and is detailed in [36].

HRTEM images and ED patterns were recorded in a FEI Titan Cube microscope (equipped with a spherical aberration corrector) operating at 80 kV and within short acquisition times (less than 5 s for ED) to reduce damage induced by electron diffraction.

Rayleigh spectra of individual freestanding DWNTs were measured in a backscattering geometry using a cross-polarization scheme with a Fianium supercontinuum laser as a light source and a fiber-fitted QE-Pro Ocean Optics spectrometer for detection. Resonant Raman scattering measurements were carried out using an iHR550 Jobin-Yvon spectrometer (1800 gratings or 1200 grooves/mm) equipped with a liquid-nitrogen-cooled, back-illuminated silicon charge-coupled device detector in a micro-Raman backscattering configuration. The home-made microscope is equipped with a 100 × objective lens (numerical aperture of 0.95). The samples were mounted on a three-axis piezo-electric stage (PIMars P-563, Physik Instrumente) to ensure precise positioning and focusing of the laser spot. Incident excitations from various continuous-wave lasers were used: HeNe at 632.8 nm (1.96 eV), diode-pumped solid-state lasers at 457 nm (2.71 eV), 532 nm (2.33 eV), and 561 nm (2.21 eV), and a Ti:sapphire laser filtered using a tunable laser line filter [39] in the near infrared. To avoid heating effects, the laser intensity impinging the tube was kept below 100 kW/cm². Photoluminescence measurements were performed on the same setup but using a liquid-nitrogen-cooled InGaAs detector and a grating blazed at 1 μm with 300 grooves/mm. In all the Raman and PL measurements, the incident light polarization is along the nanotube axis.

III. RESULTS

The first investigated SC@SC DWNT is unambiguously identified as (8,4)@(18,2) from its ED pattern [Fig. 1(a)] and its Raman spectrum measured at 2.21 eV [561 nm; Fig. 1(b)]. The PL emission spectrum obtained by exciting this DWNT at 2.21 eV is shown in Fig. 1(c). The PL peak is centered at 1.128 eV (1099 nm). Its linewidth (FWHM) is ≈27 meV, and its maximum intensity is around 0.6 counts/s for a laser power of 60 μW. The observed PL peak is attributed to the emission from the first excitonic transition of the ISCT (S1), i.e., since its position is close to the one expected around 1.15 eV [40] for a (8,4) SWNT. Regarding the excitation, the energy used (2.21 eV) is close to both the ISCT second transition (S2) and the outer tube third transition (S3), predicted at 2.13 and 2.14 eV for the (8,4) and (18,2) SWNTs [33], respectively. This closeness is supported by the presence of both inner- and outer-tube signatures in the Raman spectrum excited at 2.21 eV. Moreover, the observed low intensity of the high-frequency radial breathinglike mode [4,34,41] (RBLM) at 288 cm⁻¹, dominated by the radial vibration of the (8,4) ISCT, is in agreement with the theoretically predicted vanishing of the radial breathing mode (RBM) of the (8,4) SWNT excited around its S2 transition [42,43].

However, it has recently been demonstrated that the optical transitions can be significantly shifted in DWNTs compared to their SWNT constituent counterparts [7]. Hence, a clear determination of the excited optical transitions requires an independent measurement of their energies. This has been achieved by measuring the Rayleigh spectra of two other individual SC@SC DWNTs, identified as (7,6)@(16,6) and (10,6)@(14,13) [36], which are shown in Figs. 2(a) and 2(d), respectively. By analyzing RBLM and G-mode resonance conditions at each excitation energy and comparing Rayleigh optical resonances to those of the constituent SWNTs [33], we have been able to assign unambiguously the resonance peaks in Rayleigh spectra to particular excitonic transitions of either inner layers [Sjj], in Figs. 2(a) and 2(d)] or outer layers [Sjj] in Figs. 2(a) and 2(d); see [36]).

The PL response of the (7,6)@(16,6) DWNT, excited at 1.78 eV (close to S22 located at 1.82 eV in the Rayleigh
The bright spot in the PLE map is attributed to the emission and the corresponding Raman spectrum in Fig. 2(b). The PL is centered at 1.058 eV (1172 nm), its FWHM is 36 meV, is shown in Fig. 2(c) [the resonance with this transition is shown in Fig. 2(f) [the combination mode [36]]. In the 1.4–1.8 eV range, two transitions are observed at 1.44 and 1.55 eV by Rayleigh scattering [Fig. 4(c), middle panel] which are assigned to $M_{11}^-$ and a superposition of $S_{22}^i$ and $S_{22}^{-}$, respectively, based on the resonant Raman excitation profiles (REPs) of RBLMs [Fig. 4(b)] and $G$ modes and $M_{11}^0$ electronic Raman scattering [36]. The PLE and REP maps of RBLMs of the (14,1)@(15,12) DWNT in the range 1.4–1.77 eV are presented in Figs. 4(a) and 4(b), respectively. The presence of two bright spots in the REP map [Fig. 4(b)], namely, 144 and 211 cm$^{-1}$ at an excitation energy close to 1.550 eV, indicates that, as expected, both in-phase and out-of-phase RBLMs are in resonance when $S_{22}^i$ and $M_{11}^0$, excited simultaneously [Fig. 4(b)]. The PLE map displays a bright spot located at 0.793 eV in emission and 1.540 eV in excitation [Fig. 4(a)]. The emission at 0.793 eV is assigned to the luminescence of the inner (14,1) layer ($S_{22}^i$). Its maximum intensity is around 2 counts/s ($P_{\text{laser}} \approx 70 \mu W$). As expected, when exciting the $M_{11}^0$ = 1.44 eV transition of the (15,12) outer tube, we observe exclusively the in-phase RBLM in the Raman spectrum [single bright spot at 144 cm$^{-1}$ for an excitation at 1.44 eV in Fig. 4(b)]. Surprisingly, a slightly weaker PL signal is also detected around 0.793–1.420 eV, as shown in the PLE map in Fig. 4(a). Surprisingly, a slightly weaker PL signal is also detected around 0.793–1.420 eV, as shown in the PLE map in Fig. 4(a) (see also [36]). This shows that it is possible to measure the PL signal of the ISCT through the excitation of an optical transition of the outer tube and suggests that an exciton transfer occurs from the metallic outer tube to the ISCT.

A fourth SC@M DWNT was unambiguously indexed from ED as (14,1)@(15,12) (see [36] for a detailed characterization). The outer-tube metallic character is also clearly evidenced by the broad component in the $G$ band and the presence of electronic Raman signatures in the Raman spectra [36]. In the 1.4–1.8 eV range, two transitions are observed at 1.44 and 1.55 eV by Rayleigh scattering [Fig. 4(c), middle panel] which are assigned to $M_{11}^-$ and a superposition of $S_{22}^i$ and $S_{22}^{-}$, respectively, based on the resonant Raman excitation profiles (REPs) of RBLMs [Fig. 4(b)] and $G$ modes and $M_{11}^0$ electronic Raman scattering [36]. The PLE and REP maps of RBLMs of the (14,1)@(15,12) DWNT in the range 1.4–1.77 eV are presented in Figs. 4(a) and 4(b), respectively. The presence of two bright spots in the REP map [Fig. 4(b)], namely, 144 and 211 cm$^{-1}$ at an excitation energy close to 1.550 eV, indicates that, as expected, both in-phase and out-of-phase RBLMs are in resonance when $S_{22}^i$ and $M_{11}^0$, excited simultaneously [Fig. 4(b)]. The PLE map displays a bright spot located at 0.793 eV in emission and 1.540 eV in excitation [Fig. 4(a)]. The emission at 0.793 eV is assigned to the luminescence of the inner (14,1) layer ($S_{22}^i$). Its maximum intensity is around 2 counts/s ($P_{\text{laser}} \approx 70 \mu W$). As expected, when exciting the $M_{11}^0$ = 1.44 eV transition of the (15,12) outer tube, we observe exclusively the in-phase RBLM in the Raman spectrum [single bright spot at 144 cm$^{-1}$ for an excitation at 1.44 eV in Fig. 4(b)]. Surprisingly, a slightly weaker PL signal is also detected around 0.793–1.420 eV, as shown in the PLE map in Fig. 4(a). Surprisingly, a slightly weaker PL signal is also detected around 0.793–1.420 eV, as shown in the PLE map in Fig. 4(a) (see also [36]). This shows that it is possible to measure the PL signal of the ISCT through the excitation of an optical transition of the outer tube and suggests that an exciton transfer occurs from the metallic outer tube to the ISCT.

FIG. 2. The (7,6)@(16,6) and (10,6)@(14,13) DWNTs. (a) The (7,6)@(16,6) and (d) (10, 6)@(14, 13) Rayleigh spectra; optical transitions associated with inner (i) and outer (o) tubes are labeled on the graph as $S_{jj}^i$ and $S_{jj}^o$, respectively, where $j$ is the optical transition index. (b) The (7,6)@(16,6) and (e) (10, 6)@(14, 13) RBLM (inset) and $G$-mode ranges of Raman spectra excited at (b) 1.78 and (e) 1.6 eV close to the $S_{jj}^o$ optical resonances observed by Rayleigh. (c) The (7,6)@(16,6) and (f) (10, 6)@(14, 13) corresponding PL emission spectra excited at (c) 1.77 and (f) 1.57 eV corresponding to $S_{jj}^i$. Blue lines show experimental data; black lines show Lorentzian fits. The additional narrow component in the PL spectrum in (c), marked with an asterisk, is attributed to the 2G + 2D Raman peak.

The spectrum, with a FWHM of 36 meV, is shown in Fig. 2(c) and the corresponding Raman spectrum in Fig. 2(b). The PL is centered at 1.058 eV (1172 nm), its FWHM is $\approx 28$ meV, and its maximum intensity is around 0.7 counts/s ($P_{\text{laser}} \approx 60 \mu W$). For comparison, $S_{11}^i$ of the (7,6) SWNT is expected at 1.13 eV [40]. The additional narrow line in the PL spectrum [marked with an asterisk in Fig. 2(c)] is attributed to the 2G + 2D combination mode [36].

For the third DWNT, (10,6)@(14,13), $S_{22}^i$ is located at 1.6 eV (FWHM = 22 meV). The PL spectrum excited in resonance with this transition is shown in Fig. 2(f) [the corresponding Raman spectrum is presented in Fig. 2(e)]. In this case, the PL is centered at 0.828 eV (1498 nm), its FWHM is $\approx 24$ meV, and its maximum intensity is around 1 counts/s ($P_{\text{laser}} \approx 70 \mu W$). For comparison, $S_{11}^i$ of the (10,6) SWNT is expected at 0.926 eV [40].

Since $S_{22}^i$ of the (10,6)@(14,13) DWNT falls in the excitation wavelength range available in our experimental setup, we carried out the measurement of the detailed PLE map in the excitation range from 1.49 up to 1.77 eV [Fig. 3(a)]. The bright spot in the PLE map is attributed to the emission involving $S_{11}^i$ of the (10,6) ISCT excited at its $S_{22}^i$.

FIG. 3. The (10, 6)@(14, 13) DWNT. (a) PLE map. Gray zones are artifacts mainly from the second order of the laser excitation line. (b) Top: PLE spectrum, integrated PL intensity as a function of laser excitation energy; black dots show experimental data, and the blue line shows the Lorentzian fit. Middle: Rayleigh spectrum; black dots show experimental data, and the red line shows the fit using an excitonic model [52]. Bottom: REPs of RBLMs, both in phase (blue open circles) and out of phase (black open diamonds), and corresponding fits using an excitonic model [52] (blue and black lines, respectively). The PLE profile fit gives a maximum of emission at an excitation energy of 1.573 eV, corresponding to $S_{22}^i$. The fits of the Rayleigh spectrum and REPs give the energies of this transition at 1.599 and 1.585 eV, respectively.
IV. DISCUSSION

We first discuss the shifts of the transition energies compared to that of SWNTs. As summarized in Table I, the $S_{11}'$ measured here are redshifted compared to the $S_{11}$ of the corresponding SWNTs [40] by an amplitude varying from $-20$ to $-100$ meV. Such shifts were already observed for higher-order transitions [6,7,35] by experiments performed on individual index-identified DWNTs. These shifts were mainly attributed to the electronic coupling between the incommensurate inner and outer tubes [7,8] and to the effect of the interlayer dielectric screening of Coulomb interactions on the optical transitions in DWNTs [7,22]. The magnitudes of the energy shifts have been shown to depend sensitively on the specific optical transition and on the inner- and outer-tube species [7], which explains the tube-to-tube variations reported here. Furthermore, the changes in the exciton binding energy could have an additional impact on the lowest transition energies [22], but they still need to be evaluated.

Direct comparisons of the extracted PLE spectra, Rayleigh spectra, and RBLM REPs for the (10,6)@(14,13) and (14,1)@(15,12) DWNTs are displayed in Figs. 3(b) and 4(c), respectively. Small redshifts ($-5$ to $-20$ meV) are observed in the PLE spectra compared to RBLM REPs and Rayleigh spectra. Such shifts have already been observed in SWNTs and were attributed to the energy difference between the localized exciton dominating the PLE spectrum and the free exciton giving rise to the REP [44].

For all four investigated DWNTs, the ISCT PL signal is low, as highlighted, for example, by the comparison with the $2G + 2D$ combination mode intensity in Fig. 2(c). Our results

<table>
<thead>
<tr>
<th>DWNT</th>
<th>(8,4)@18(2)</th>
<th>(7,6)@16(6)</th>
<th>(10,6)@14(13)</th>
<th>(14,1)@15(12)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$S_{11}'$ (eV)</td>
<td>1.128</td>
<td>1.058</td>
<td>0.828</td>
<td>0.792</td>
</tr>
<tr>
<td>$S_{11}$ (eV)</td>
<td>1.150</td>
<td>1.130</td>
<td>0.926</td>
<td>0.869</td>
</tr>
<tr>
<td>Difference (meV)</td>
<td>$-22$</td>
<td>$-72$</td>
<td>$-98$</td>
<td>$-78$</td>
</tr>
</tbody>
</table>

TABLE I. Comparison of first excitonic transition energies of the measured DWNTs ($S_{11}'$) and of corresponding SWNTs ($S_{11}$, from [40]).
suggest that the strong PL signal measured in different investigations performed on ensembles of DWNTs may clearly originate from SWNTs present in the samples [14,15,17–19,45]. In the perspective of possible optoelectronics developments, the PL QY, which is defined as the ratio of the number of photons emitted to the number of photons absorbed, appears to be a key parameter. In order to estimate the quantum yield of the studied DWNTs, we first performed a calibration of our experimental setup to determine the number of photons corresponding to one count detected. To do so, we first placed a silicon wafer under the microscope, focused on it with a laser with a wavelength of 950 nm, and measured the reflected power at the exit of the microscope using a power meter. We then inserted into the laser path at the entrance of the microscope a series of calibrated neutral density filters in order to attenuate the laser sufficiently enough to record its signal with the InGaAs detector without saturating it. We thus determined, that 320 ± 30 photons exiting the microscope are required to accumulate 1 count on the detector. This number compares reasonably well with a simple estimate based on the manufacturers’ specifications of the different elements of the setup, which gives 200 photons per count. By taking into account the transmissions of different elements of the microscope and the difference of the reflection efficiency of the spectrometer grating, we end up with 520 and 880 photons/count at 1.3 eV (1100 nm) and 0.8 eV (1550 nm), respectively. The detector quantum efficiency can be considered constant in this range. Taking the solid angle of the collection of the microscope objective (numerical aperture (0.95) into account as well, we can extract from the recorded PL spectra the number of emitted photons by summing the signal on all detector pixels.

In order to estimate the number of absorbed photons, (i) the absolute absorption cross section is taken as 0.6 nm² per excited transition as measured on SWNTs [46] and on DWNTs [47], (ii) the laser spot size is measured by Raman mapping across a nanotube, and (iii) the impinging laser power is measured under the microscope objective. This procedure gives values of the QY of 5 × 10⁻⁶ for the (10, 6)@(14, 13) DWNT excited at S₂,⁰ and 3 × 10⁻⁶ (2 × 10⁻⁶) for the (14,1)@(15,12) DWNT excited at S₂,⁰ + Mₘₑₐ₂ + Mₘₑₐ₃ + Mₘₑₐ₄. Additionally, for the (8,4)@(18,2) DWNT, we measured directly its extinction at 2.21 eV (561 nm), which is 4.9(±0.5) × 10⁻⁴ (Fig. 5). The extinction and the measurement of the impinging laser power give direct access to the number of photons absorbed by the DWNT during the measurement of its PL spectrum. Thus, we can estimate, with a direct measurement of its optical absorption, the QY of the (8,4)@(18,2) DWNT excited at 2.21 eV as 3.3(±0.9) × 10⁻⁶.

The value of the QY of the ISCT PL is thus found for the three investigated DWNTs, independent of the outer-tube SC or M nature, to be of the order of 10⁻⁶, i.e., four orders of magnitude lower than in SWNTs [48], in agreement with the conclusion of Ref. [20]. This weak QY can be understood in terms of (i) ultrafast exciton transfer from the inner to outer tube as suggested by femtosecond time-resolved luminescence measurements [21] and time-domain ab initio simulations [25] and (ii) charge transfer from outer to inner tubes [26,27]. Regarding the second effect, the observation of a rather strong electronic Raman scattering signal and broad component in the G band in the (14,1)@(15,12) DWNT [36] indicates that the doping level of this tube is, at most, of the order of 0.001 charge/atom [49,50]. Even if we cannot evaluate more precisely this doping, a recent study on DWNTs filled by linear carbon chains [27] has shown that balancing the intrinsic charge transfer between the outer tube and ISCT leads to a maximum increase of one order of magnitude of the PL signal. We thus infer that the main source of quenching would be the decay of the exciton through the lower-energy states of the outer tube compared to S₁₁ [25]. As discussed in Ref. [25], the detailed dynamics of exciton transfer in DWNTs is a complex and intricate process. Indeed, Postupna et al. [25] have shown that the exciton relaxation pathways are different for different DWNTs and that their dynamics can depend significantly on the initial system configuration. Furthermore, their work revealed that the detailed mechanism appears to go beyond the level alignment picture and involve geometry fluctuations and optically dark states. Nevertheless, simulated intertube transfer [25] and time-resolved luminescence experiments [21] agree for a transfer time of the order of 100 fs, which is in agreement with the low QY reported here. Regarding the observed (14,1) ISCT PL upon excitation of the (15,12) metallic outer tube, this transfer time has to be compared with the dynamics of photocarriers in metallic nanotubes. Hertel et al. [51] have shown that, for an excitation in the near infrared, the carriers in metallic tubes relax to the Fermi energy by electron-electron scattering within ≈50 fs. The two phenomena (intertube exciton transfer and photocarrier relaxation in metallic tubes) then appear to occur on very close time scales, which can explain our observation. Another possibility would be a significant mixing of energy levels with some delocalization between the tubes that could occur due to atomic motions at room temperature, as suggested by Postupna et al. [25]. We believe, however, that the first explanation is the most reasonable one given the magnitude of the effect and the fact that the Raman signatures remain unaffected.
V. CONCLUSION

In conclusion, our results derived from combined TEM, Rayleigh spectroscopy, Raman spectroscopy, and PL experiments performed on individual freestanding DWNTs give unambiguous evidence of ISCT PL, which is independent of the SC or M nature of the outer tubes. Our results definitively close the debate about the existence of ISCT luminescence in DWNTs. The PL QY of ISCT in DWNTs is found to be low. It was estimated for three DWNTs as a few \(10^{-6}\), i.e., four orders of magnitude lower than in freestanding SWNTs. This result is mainly attributed to ultrafast exciton transfer from the inner to outer tube. The investigation of outer-tube PL upon ISCT excitation could be a way to fully address this point. Furthermore, we have shown that it was possible to measure the PL signal of the \((14,1)\) ISCT through the excitation of the \(M_{11}\) optical transition of the \((15,12)\) outer tube. Moreover, the ISCT PL QY is found in this case to be comparable to the one estimated upon excitation of the ISCT \(S_{21}\). More generally, this opens the question of the possibility of an exciton transfer occurring from the outer tube to the ISCT, i.e., in the opposite way to that usually observed.

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[36] See Supplemental Material at http://link.aps.org/supplemental/10.1103/PhysRevB.96.195410, which includes Refs. [53–55], for details of the sample fabrication method and experimental measurement procedures; a detailed characterization and indexation of all four individual DWNTs, based on ED, HRTEM, and Rayleigh and Raman spectroscopies; PL spectra of the (7,6)@(16,6) DWNT measured at 693 nm (1.79 eV) and 700 nm (1.77 eV) and plotted as a function of Raman shift (with the $2G + 2D$ Raman peak indicated in the figure); PL spectra of (14,1)@(15,12) DWNT; Raman spectra of individual SC@M (14,1)@(15,12) DWNTs, measured at 776 nm (1.60 eV), 850 nm (1.46 eV), and 457 nm (2.71 eV), showing electronic Raman peaks; and a resonant Raman excitation map and resonant Raman excitation profiles of the (14,1)@(15,12) DWNT in the G-mode range.
