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ANEXOS

**Análisis y puesta en marcha de una
plataforma triaxial como demostrador
tecnológico**

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ANEXO 1. (CÓDIGO)

1.1. PYTHON

A través de este código se realiza la detección y el control de la pelota.

```
import cv2
import numpy as np
import time
import imutils
import tkinter as tk
import tkinter.messagebox
from PIL import Image, ImageTk
import serial
import serial.tools.list_ports
from math import *
x_a = np.zeros((12000, 1))
y_a = np.zeros((12000, 1))
Ix_a = np.zeros((12000, 1))
Iy_a = np.zeros((12000, 1))
consigneX_a = np.zeros((12000, 1))
consigneY_a = np.zeros((12000, 1))
alpha_a = np.zeros((12000, 1))
beta_m_a = np.zeros((12000, 1))
errorX_a = np.zeros((12000, 1))
errorY_a = np.zeros((12000, 1))
preX_a = np.zeros((12000, 1))
preY_a = np.zeros((12000, 1))
time_a = np.zeros((12000, 1))
```

(Código)

```
f = 0
c = 0
write_index=0
lines = open("/Users/rlopez/Desktop/Codigo/data.txt").read().splitlines()
lines = lines[:-11]    #enlève les 11 dernières lignes du fichier
lines = lines[1:]     #enlève la première ligne du fichier
dataDict = {}
camHeight =480
camWidth = 640
cam = cv2.VideoCapture(0)
cam.set(3,camWidth)
cam.set(4,camHeight)
getPixelColor = True #False
H,S,V = 16,131,229
mouseX,mouseY = 0,0
for i in range(0,len(lines)):
    key, value = lines[i].split("#")
    alpha, beta = key.split("|")
    angleA, angleB, angleC = value.split("|")
    dataDict[(float(alpha),float(beta))] = (float(angleA), float(angleB),
float(angleC))
controllerWindow = tk.Tk()
controllerWindow.title("fenêtre de contrôle")
controllerWindow.geometry("820x500")
controllerWindow["bg"]="white"
controllerWindow.resizable(0, 0)
videoWindow = tk.Toplevel(controllerWindow)
videoWindow.title("retour caméra")
videoWindow.resizable(0, 0) #empêche de modifier les dimensions de la fenêtre
```

```
lmain = tk.Label(videoWindow)
lmain.pack()
videoWindow.withdraw()
graphWindow = tk.Toplevel(controllerWindow)
graphWindow.title("Position en fonction du temps")
graphWindow.resizable(0, 0)
graphCanvas = tk.Canvas(graphWindow,width=camHeight+210,height=camHeight)
graphCanvas.pack()
graphWindow.withdraw()
pointsListCircle = []
def createPointsListCircle(rayon): global pointsListCircle
    for angle in range(0,360):
        angle=angle-90
    pointsListCircle.append([rayon*cos(radians(angle))+240,rayon*sin(radians(angle))+2
40])
createPointsListCircle(50)
pointsListEight = []
def createPointsListEight(rayon):
    global pointsListEight
    for angle in range(270,270+360):
        pointsListEight.append([rayon*cos(radians(angle))+240,rayon*sin(radians(angle))+2
40+rayon])
        for angle in range(360,0,-1):
            angle=angle+90
        pointsListEight.append([rayon*cos(radians(angle))+240,rayon*sin(radians(angle))+2
40-rayon])
createPointsListEight(80)
drawCircleBool = False
```

```
def startDrawCircle():
    global drawCircleBool, drawEightBool, consigneX, consigneY
    if drawCircleBool == False:
        drawCircleBool = True
        BballDrawCircle["text"] = "Centrer la bille"
    else:
        drawCircleBool = False
        consigneX, consigneY = 240, 240
        sliderCoefP.set(sliderCoefPDefault)
        BballDrawCircle["text"] = "Faire tourner la bille en cercle"

drawEightBool = False
def startDrawEight():
    global drawEightBool, drawCircleBool, consigneX, consigneY
    if drawEightBool == False:
        drawEightBool = True
        BballDrawEight["text"] = "Centrer la bille"
    else:
        drawEightBool = False
        consigneX, consigneY = 240, 240
        sliderCoefP.set(sliderCoefPDefault)
        BballDrawEight["text"] = "Faire tourner la bille en huit"

pointCounter = 0
def drawWithBall():
    global pointCounter, consigneX, consigneY
    if drawCircleBool == True:
        #sliderCoefP.set(15)
```



```
    if pointCounter >= len(pointsListCircle):
        pointCounter = 0

        point = pointsListCircle[pointCounter]
        consigneX, consigneY = point[0], point[1]
        pointCounter += 7

    if drawEightBool == True:
        #sliderCoefP.set(15)

        if pointCounter >= len(pointsListEight):
            pointCounter = 0

            point = pointsListEight[pointCounter]
            consigneX, consigneY = point[0], point[1]
            pointCounter += 7

def setConsigneWithMouse(mousePosition):
    global consigneX, consigneY

    if mousePosition.y > 10:
        refreshGraph()

        consigneX, consigneY = mousePosition.x, mousePosition.y

def getMouseClickedPosition(mousePosition):
    global mouseX, mouseY

    global getPixelColor

    mouseX, mouseY = mousePosition.x, mousePosition.y

    getPixelColor = True

    showVideoWindow = False

    def showCameraFrameWindow():
        global showVideoWindow, showGraph

        global BRetourVideoTxt

        if showVideoWindow == False:

            if showGraph == True:
```

(Código)

```
graphWindow.withdraw()
showGraph = False
BafficherGraph["text"] = "Afficher graphique"
videoWindow.deiconify()
showVideoWindow = True
BRetourVideo["text"] = "Cacher le retour vidéo "
else:
    videoWindow.withdraw()
    showVideoWindow = False
    BRetourVideo["text"] = "Afficher le retour vidéo"
showCalqueCalibrationBool = False
def showCalqueCalibration():
    global showCalqueCalibrationBool
    showCalqueCalibrationBool = not showCalqueCalibrationBool
    showGraph = False
    def showGraphWindow():
        global showGraph, showVideoWindow
        global BafficherGraphif showGraph == False:
            if showVideoWindow == True:
                videoWindow.withdraw()
                showVideoWindow = False
                BRetourVideo["text"] = "Afficher le retour vidéo"
            showGraph = True
            BafficherGraph["text"] = "Cacher graphique "
        else:
            showGraph = False
            BafficherGraph["text"] = "Afficher graphique"
```

t = 480

consigneY = 240

consigneX = 240

x=0

y=0

def paintGraph():

 global t,consigneY,x,y,prevX,prevY,alpha,prevAlpha

 global showGraphPositionX,showGraphPositionY, showGraphAlpha,
 showGraphBeta_m

 if showGraph == True:

 graphWindow.deiconify()

 if showGraphPositionX.get() == 1:

 graphCanvas.create_line(t-3,prevX,t,x, fill="#b20000", width=2)

 if showGraphPositionY.get() == 1:

 graphCanvas.create_line(t-3,prevY,t,y, fill="#0069b5", width=2)

 if showGraphAlpha.get() == 1:

 graphCanvas.create_line(t-3,240-prevAlpha*3,t,240-alpha*3,
fill="#8f0caf", width=2)

 if showGraphBeta_m.get() == 1:

 graphCanvas.create_line(t-3,240-prevBeta,t,240-beta_m,
fill="#476042", width=2)

 if t >= 480:

 t = 0

 graphCanvas.delete("all")

 graphCanvas.create_line(3,3,480,3,fill="black", width=3)

 graphCanvas.create_line(3,480,480,480,fill="black", width=3)

 graphCanvas.create_line(3,3,3,480,fill="black", width=3)

(Código)

```
graphCanvas.create_line(480,3,480,480,fill="black", width=3)
graphCanvas.create_line(550,32,740,32,fill="#b20000", width=5)
graphCanvas.create_line(550,53,740,53,fill="#0069b5", width=5)
graphCanvas.create_line(550,73,740,73,fill="#8f0caf", width=5)
graphCanvas.create_line(550,94,740,94,fill="#476042", width=5)

if showGraphPositionX.get() == 1:
    graphCanvas.create_line(3,consigneX,480,consigneX,fill="#ff7777",
width=2)
if showGraphPositionY.get() == 1:
    graphCanvas.create_line(3,consigneY,480,consigneY,fill="#6f91f7",
width=2)
    t += 3
else:
    graphWindow.withdraw()

def refreshGraph():
    global t
    t=480

def endProgam():
    global x_a, y_a, consigneX_a, consigneY_a, Ix_a, Iy_a, alpha_a, beta_m_a,
errorX_a, errorY_a, preX_a, preY_a, time_a
    fic = open("archivoX.txt","w")
    fic.writelines("%f\n" % f for f in x_a)
    fic.close()
    fic1 = open("archivoY.txt","w")
    fic1.writelines("%f\n" % f for f in y_a)
```

```
fic1.close()

fic2 = open("archivoCX.txt","w")

fic2.writelines("%f\n" % f for f in consigneX_a)

fic2.close()

fic3 = open("archivoCY.txt","w")

fic3.writelines("%f\n" % f for f in consigneY_a)

fic3.close()

fic4 = open("archivoIx.txt","w")

fic4.writelines("%f\n" % f for f in Ix_a)

fic4.close()

fic5 = open("archivoIy.txt","w")

fic5.writelines("%f\n" % f for f in Iy_a)

fic5.close()

fic6 = open("archivoalpha.txt","w")

fic6.writelines("%f\n" % f for f in alpha_a)

fic6.close()

fic7 = open("archivobeta_m.txt","w")

fic7.writelines("%f\n" % f for f in beta_m_a)

fic7.close()

fic8 = open("Error_x.txt","w")

fic8.writelines("%f\n" % f for f in errorX_a)

fic8.close()

fic9 = open("Error_y.txt","w")

fic9.writelines("%f\n" % f for f in errorY_a)

fic9.close()

fic10 = open("Prev_x.txt","w")

fic10.writelines("%f\n" % f for f in preX_a)

fic10.close()

fic11 = open("Prev_y.txt","w")
```

(Código)

```
fic11.writelines("%f\n" % f for f in preY_a)
fic11.close()
fic12 = open("time.txt","w")
fic12.writelines("%f\n" % f for f in time_a)
fic12.close()
controllerWindow.destroy()
```

```
sliderHDefault = 50
sliderSDefault = 50
sliderVDefault = 50
sliderCoefPDefault = 0
sliderCoefIDefault = 0
sliderCoefDDefault = 0
```

```
def resetSlider():
    sliderH.set(sliderHDefault)
    sliderS.set(sliderSDefault)
    sliderV.set(sliderVDefault)
    sliderCoefP.set(sliderCoefPDefault)
    sliderCoefI.set(sliderCoefIDefault)
    sliderCoefD.set(sliderCoefDDefault)
    sommeErreurX=0
    sommeErreurY=0
```

```
def donothing():
```

```
    pass
```

```
def rangerPlateau():
```

```
    if arduinoIsConnected == True:
```

```
        if tkinter.messagebox.askokcancel("Avertissement", "Pensez à retirer le
plateau.):
```

```
print("abaissement des bras")

ser.write(("descendreBras\n").encode())

else:

    if tkinter.messagebox.askokcancel("Avertissement","L'Arduino n'est pas
connecté"):

        donothing()

def eleverPlateau():

    global alpha

    if arduinoIsConnected == True:

        if tkinter.messagebox.askokcancel("Avertissement", "Pensez à retirer le
plateau."):

            print("Elevation des bras")

            ser.write((str(dataDict[(0,0)])+"\n").encode())

            alpha = 0

        else:

            if tkinter.messagebox.askokcancel("Avertissement","L'Arduino n'est pas
connecté"):

                donothing()

def servosTest():

    if arduinoIsConnected == True:

        if tkinter.messagebox.askokcancel("Avertissement", "Le plateau doit être
en place."):

            for i in range(2):

                beta = 0

                alpha = 35

                while beta < 360:

                    ser.write((str(dataDict[(alpha,beta)])+"\n").encode())

                    ser.flush()

                    time.sleep(0.002)

                    beta = round(beta+0.2,2)
```

(Código)

```
        print(alpha,beta)

        time.sleep(1)

        ser.write((str(dataDict[(0,0)])+"\n").encode())

    else:

        if tkinter.messagebox.askokcancel("Avertissement","L'Arduino n'est pas
connecté"):

            donothing()

arduinoIsConnected = False

def connectArduino():

    global ser

    global label

    global arduinoIsConnected

    ports = list(serial.tools.list_ports.comports())

    for p in ports:

        if "Arduino" in p.description:

            ser = serial.Serial(p[0], 19200, timeout=1)

            time.sleep(1) #give the connection a second to settle

            label.configure(text="Arduino connecté", fg="#36db8b")

            arduinoIsConnected = True

startBalanceBall = False

def startBalance():

    global startBalanceBall

    if arduinoIsConnected == True:

        if startBalanceBall == False:

            startBalanceBall = True

            BStartBalance["text"] = "Arrêter"

    else:
```



```
startBalanceBall = False

BStartBalance["text"] = "Commencer"

else:

    if tkinter.messagebox.askokcancel("Avertissement","L'Arduino n'est pas
connecté"):

        donothing()

FrameVideoControl = tk.LabelFrame(controllerWindow, text="Vidéo contrôle")
FrameVideoControl.place(x=20,y=20,width=380)

BRetourVideo = tk.Button(FrameVideoControl, text="Afficher le retour vidéo",
command=showCameraFrameWindow)

BRetourVideo.pack()

BPositionCalibration = tk.Button(FrameVideoControl, text="Calque",
command=showCalqueCalibration)

BPositionCalibration.place(x=290,y=0)

sliderH = tk.Scale(FrameVideoControl, from_=0, to=100, orient="horizontal",
label="Sensibilité H", length=350, tickinterval = 10)

sliderH.set(sliderHDefault)

sliderH.pack()

sliderS = tk.Scale(FrameVideoControl, from_=0, to=100, orient="horizontal",
label="Sensibilité S", length=350, tickinterval = 10)

sliderS.set(sliderSDefault)

sliderS.pack()

sliderV = tk.Scale(FrameVideoControl, from_=0, to=100, orient="horizontal",
label="Sensibilité V", length=350, tickinterval = 10)

sliderV.set(sliderVDefault)

sliderV.pack()

FrameServosControl = tk.LabelFrame(controllerWindow, text="Servos contrôle")
```

(Código)

```
FrameServosControl.place(x=20,y=315,width=380)

BAbaissementPlateau = tk.Button(FrameServosControl, text="Ranger les bras",
command=rangerPlateau)

BAbaissementPlateau.pack()

BElevationBras = tk.Button(FrameServosControl, text="Mettre en place le
plateau", command=eleverPlateau)

BElevationBras.pack()

BTesterServos = tk.Button(FrameServosControl, text="Tester les servomoteurs",
command=servosTest)

BTesterServos.pack()

BStartBalance = tk.Button(FrameServosControl, text="Démarrer",
command=startBalance, highlightbackground = "#36db8b")

BStartBalance.pack()

FramePIDCoef = tk.LabelFrame(controllerWindow, text="PID coefficients")
FramePIDCoef.place(x=420,y=20,width=380)

BafficherGraph = tk.Button(FramePIDCoef, text="Afficher graphique",
command=showGraphWindow)

BafficherGraph.pack()

sliderCoefP = tk.Scale(FramePIDCoef, from_=0, to=15, orient="horizontal",
label="P", length=350, tickinterval = 3, resolution=0.01)

sliderCoefP.set(sliderCoefPDefault)

sliderCoefP.pack()

sliderCoefI = tk.Scale(FramePIDCoef, from_=0, to=1, orient="horizontal",
label="I", length=350, tickinterval = 0.2, resolution=0.001)

sliderCoefI.set(sliderCoefIDefault)

sliderCoefI.pack()

sliderCoefD = tk.Scale(FramePIDCoef, from_=0, to=10, orient="horizontal",
label="D", length=350, tickinterval = 2, resolution=0.01)

sliderCoefD.set(sliderCoefDDefault)

sliderCoefD.pack()
```

```
FrameBallControl = tk.LabelFrame(controllerWindow, text="Bille contrôle")
FrameBallControl.place(x=420,y=315,width=380, height= 132)

BballDrawCircle = tk.Button(FrameBallControl, text="Faire tourner la bille en
cercle", command=startDrawCircle)

BballDrawCircle.pack()

BballDrawEight = tk.Button(FrameBallControl, text="Faire tourner la bille en
huit", command=startDrawEight)

BballDrawEight.pack()

label = tk.Label(controllerWindow, text="Arduino déconnecté ", fg="red",
anchor="ne")

label.pack(fill="both")

BReset = tk.Button(controllerWindow, text = "Reset", command = resetSlider)

BReset.place(x=20, y=460)

BConnect = tk.Button(controllerWindow, text = "Connexion", command =
connectArduino, background="black")

BConnect.place(x=100, y=460)

BQuit = tk.Button(controllerWindow, text = "Quitter", command = endProgam)

BQuit.place(x=730, y=460)

showGraphPositionX = tk.IntVar()

showGraphPositionX.set(1)

CheckbuttonPositionX = tk.Checkbutton(graphWindow, text="Position en X",
variable=showGraphPositionX, command=refreshGraph)

CheckbuttonPositionX.place(x=500,y=20)

showGraphPositionY = tk.IntVar()

showGraphPositionY.set(1)

CheckbuttonPositionY = tk.Checkbutton(graphWindow, text="Position en Y",
variable=showGraphPositionY, command=refreshGraph)
```

(Código)

```
    CheckbuttonPositionY.place(x=500,y=40)

    showGraphAlpha = tk.IntVar()

    CheckbuttonAlpha = tk.Checkbutton(graphWindow, text="Inclinaison du
plateau", variable=showGraphAlpha, command=refreshGraph)

    CheckbuttonAlpha.place(x=500,y=60)

    showGraphBeta_m = tk.IntVar()

    CheckbuttonBeta_m = tk.Checkbutton(graphWindow, text="Inclinacion
plataforma Beta", variable=showGraphBeta_m, command=refreshGraph)

    CheckbuttonBeta_m.place(x=500,y=80)

videoWindow.protocol("WM_DELETE_WINDOW",donothing)
videoWindow.bind("<Button-2>",getMouseClickedPosition)
videoWindow.bind("<Button-1>",setConsigneWithMouse)

sommeErreurX = 1
sommeErreurY = 1
timeInterval = 1
alpha, beta, prevAlpha, prevBeta = 0,0,0,0
omega = 0.2
indice_prueba = 1

def PIDcontrol(ballPosX, ballPosY, prevBallPosX, prevBallPosY, consigneX,
consigneY):

    global omega

    global sommeErreurX, sommeErreurY

    global alpha, beta, prevAlpha, prevBeta, gama, beta_m

    global startBalanceBall, arduinoIsConnected

    global x_a, write_index, y_a, consigneX_a, consigneY_a, Ix, Iy, alpha_a,
beta_m_a, prevX, prevY, x, y, errorX_a, errorY_a, preX_a, preY_a

    gama = 0
```

```
Kp = sliderCoefP.get()
```

```
Ki = sliderCoefI.get()
```

```
Kd = sliderCoefD.get()
```

```
Ix = Kp*(consigneX-ballPosX) + Ki*sommeErreurX + Kd*((prevBallPosX-  
ballPosX)/0.0333)
```

```
Iy = Kp*(consigneY-ballPosY) + Ki*sommeErreurY + Kd*((prevBallPosY-  
ballPosY)/0.0333)
```

```
Ix = round(Ix/10000, 4)
```

```
Iy = round(Iy/10000, 4)
```

```
if Ix == 0 and Iy == 0:
```

```
    alpha = 0
```

```
    beta = 0
```

```
    gama = 0
```

```
elif Ix != 0 and sqrt(Ix**2 + Iy**2) < 1:
```

```
    gama = atan(Iy/Ix)
```

```
    alpha = asin(sqrt(Ix**2 + Iy**2))
```

```
    gama = degrees(gama)
```

```
    alpha = degrees(alpha)
```

```
if Ix < 0 and Iy >= 0:
```

```
    beta = abs(gama)
```

```
elif Ix > 0 and Iy >= 0:
```

```
    beta = 180-abs(gama)
```

```
elif Ix > 0 and Iy <= 0:
```

```
    beta = 180+abs(gama)
```

(Código)

```
elif Ix < 0 and Iy <= 0:
    beta = 360-abs(gama)

elif Ix == 0 and sqrt(Ix**2 + Iy**2) < 1:
    if Iy > 0:
        beta = 90
        alpha = asin(sqrt(Ix**2 + Iy**2))
    elif Iy < 0:
        beta = 270
        alpha = asin(sqrt(Ix**2 + Iy**2))
    alpha = degrees(alpha)

elif Ix != 0 and sqrt(Ix**2 + Iy**2) > 1:
    beta = degrees(atan(Iy/Ix))
    alpha = 30
    if Ix < 0 and Iy >= 0:
        beta = abs(gama)
    elif Ix > 0 and Iy >= 0:
        beta = 180-abs(gama)
    elif Ix > 0 and Iy <= 0:
        beta = 180+abs(gama)
    elif Ix < 0 and Iy <= 0:
        beta = 360-abs(gama)

elif Ix == 0 and sqrt(Ix**2 + Iy**2) > 1:
    alpha = 30
    if Iy > 0:
        beta = 90
    elif Iy < 0:
```

```
beta = 270

if alpha > 30:
    alpha = 30
    alpha = round(round(alpha / 0.2) * 0.2, -int(floor(log10(0.2)))) ## permet
d'arrondire avec 0.2 de précision
    beta = round(round(beta / 0.2) * 0.2, -int(floor(log10(0.2))))
    beta_m = beta - 180
    if beta_m >= 0:
        beta_m = beta_m
        beta_m = round(round(beta_m / 0.2) * 0.2, -int(floor(log10(0.2))))
    else:
        beta_m = 360 - abs(beta_m)
        beta_m = round(round(beta_m / 0.2) * 0.2, -int(floor(log10(0.2))))

    if alpha <= 30 and beta <= 360 and arduinoIsConnected == True and
startBalanceBall == True:
        ser.write((str(dataDict[(alpha,beta_m)])+"\n").encode())

    alpha = prevAlpha * omega + (1-omega) * alpha
    beta_m = prevBeta * omega + (1-omega) * beta_m

    write_index=write_index+1
    if write_index<12000:
        x_a[write_index] = ballPosX

    if write_index<12000:
        y_a[write_index] = ballPosY

    if write_index<12000:
```

(Código)

```
consigneX_a[write_index] = consigneX
```

```
if write_index<12000:
```

```
    consigneY_a[write_index] = consigneY
```

```
if write_index<12000:
```

```
    Ix_a[write_index] = Ix
```

```
if write_index<12000:
```

```
    Iy_a[write_index] = Iy
```

```
if write_index<12000:
```

```
    alpha_a[write_index] = alpha
```

```
if write_index<12000:
```

```
    beta_m_a[write_index] = beta_m
```

```
if write_index<12000:
```

```
    errorX_a[write_index] = sommeErreurX
```

```
if write_index<12000:
```

```
    errorY_a[write_index] = sommeErreurY
```

```
if write_index<12000:
```

```
    preX_a[write_index] = prevX
```

```
if write_index<12000:
```

```
    preY_a[write_index] = prevY
```



```
if startBalanceBall == True:
    sommeErreurX += (consigneX-ballPosX)
    sommeErreurY += (consigneY-ballPosY)

prevX,prevY = 0,0
prevConsigneX, prevConsigneY = 0,0
start_time = 0
Time_INIT=time.time()

def main():
    start_timeFPS = time.time()
    global H,S,V
    global getPixelColor
    global x,y, alpha, beta, beta_m
    global prevX, prevY, prevAlpha, prevBeta, prevConsigneX, prevConsigneY
    global consigneX, consigneY, sommeErreurX, sommeErreurY
    global camWidth,camHeight
    global timeInterval, start_time, time_interval, Time_INIT
    global showVideoWindow
    global img
    global indice_prueba
    global x_a, write_index, y_a, consigneX_a, consigneY_a, Ix, Iy, alpha_a,
    beta_m_a, time_a

    _, img=cam.read()
    img = img[0:int(camHeight),int((camWidth-camHeight)/2):int(camWidth-
((camWidth-camHeight)/2))] #[Y1:Y2,X1:X2]
    imgCircle = np.zeros(img.shape, dtype=np.uint8)
    cv2.circle(imgCircle, (240,240), 190, (255, 255, 255), -1, 8, 0)
```

(Código)

```

img = img & imgCircle

imgHSV = cv2.cvtColor(img,cv2.COLOR_BGR2HSV)

if getPixelColor == True and mouseY > 0 and mouseY < 480 and mouseX <
480:

    pixelColorOnClick = img[mouseY,mouseX]
    pixelColorOnClick = np.uint8([[pixelColorOnClick]])
    pixelColorOnClick = cv2.cvtColor(pixelColorOnClick,cv2.COLOR_BGR2HSV)
    H = pixelColorOnClick[0,0,0]
    S = pixelColorOnClick[0,0,1]
    V = pixelColorOnClick[0,0,2]
    getPixelColor = False

lowerBound=np.array([10,100,20])
upperBound=np.array([25,255,255])

mask=cv2.inRange(imgHSV,lowerBound,upperBound)
mask = cv2.blur(mask,(7,7))           # ajoute du flou à l'image
mask = cv2.erode(mask, None, iterations=2)   # retire les parasites
mask = cv2.dilate(mask, None, iterations=2)   # retire les parasites

cnts,hierarchy=cv2.findContours(mask.copy(),
cv2.RETR_EXTERNAL,cv2.CHAIN_APPROX_SIMPLE)

cv2.circle(img, (int(consigneX), int(consigneY)), int(4),(255, 0, 0), 2)

if showCalqueCalibrationBool == True:

    cv2.circle(img, (240,240), 220,(255, 0, 0), 2)
    cv2.circle(img, (240,240), 160,(255, 0, 0), 2)
    cv2.line(img, (240, 240), (240, 240+160), (255,0,0), 2)

```

```
cv2.line(img, (240, 240), (240+138, 240-80), (255,0,0), 2)
```

```
cv2.line(img, (240, 240), (240-138, 240-80), (255,0,0), 2)
```

```
if len(cnts) > 0:
```

```
    cnts = cnts[0]
```

```
    center = None
```

```
    c = cnts
```

```
    timeInterval = time.time() - start_time
```

```
    (x, y), radius = cv2.minEnclosingCircle(c)
```

```
    if radius > 10:
```

```
        cv2.putText(img, str(int(x)) + ";" + str(int(y)).format(0, 0), (int(x)-50,  
int(y)-50), cv2.FONT_HERSHEY_SIMPLEX, 1, (255, 255, 255), 2)
```

```
        cv2.circle(img, (int(x), int(y)), int(radius), (0, 255, 255), 2)
```

```
        PIDcontrol(int(x), int(y), prevX, prevY, consigneX, consigneY)
```

```
        start_time = time.time()
```

```
    else:
```

```
        sommeErreurX, sommeErreurY = 0, 0
```

```
        x, y = prevX, prevY
```

```
if showVideoWindow == True:
```

```
    img = cv2.cvtColor(img, cv2.COLOR_BGR2RGB)
```

```
    img = Image.fromarray(img)
```

```
    imgtk = ImageTk.PhotoImage(image=img)
```

```
    lmain.imgtk = imgtk
```

```
    lmain.configure(image=imgtk)
```

```
lmain.after(10, main)
```

```
#drawWithBall()
```

```
if prevConsigneX != consigneX or prevConsigneY != consigneY:
```

(Código)

```
sommeErreurX, sommeErreurY = 0,0

paintGraph()
prevX,prevY = int(x), int(y)
prevConsigneX, prevConsigneY = consigneX, consigneY
prevAlpha = alpha
prevBeta = beta_m
time_interval = time.time()- Time_INIT

if (time.time() - start_timeFPS) > 0:
    print("FPS: ", 1.0 / (time.time() - start_timeFPS))

if write_index<12000:
    time_a[write_index] = time_interval

main()
tk.mainloop()
```

1.2. ARDUINO

El programa que se muestra a continuación es el que comanda los motores.

```
#include <Servo.h>
```

```
Servo servoA;
```

```
Servo servoB;
```

```
Servo servoC;
```

```
int ledTemoin = 8;
```

```
float angleA = 45;
```

```
float angleB = 45;
```

```
float angleC = 45;
```

```
int ledRojo = 8;
```

```
int ledR = LOW;
```

```
unsigned long previousMillis = 0;
```

```
void setup() {
```

```
  Serial.begin(19200);
```

```
  //pinMode(ledTemoin, OUTPUT); // led temoin
```

```
  pinMode(ledRojo, OUTPUT);
```

```
  //digitalWrite(ledTemoin, LOW);
```

```
  servoC.attach(9); //servo A
```

```
  servoB.attach(11); //servo B // se han cambiado el motor A por el C para  
ajustar el control
```

```
  servoA.attach(10); //servo C
```

```
  delay(1000);
```

(Código)

```
servoA.writeMicroseconds((-2380 + 1450)*float(angleA) / 90 + 2380);  
//servoB.writeMicroseconds((-2370 + 1480)*float(angleB) / 90 + 2370);  
servoB.writeMicroseconds((-2330 + 1480)*float(angleB) / 90 + 2330);  
servoC.writeMicroseconds((-2270 + 1430)*float(angleC) / 90 + 2270);  
  
}  
  
int count = 0;  
  
void loop() {  
    //digitalWrite(ledTemoin , millis() / 500 % 2 ); // led temoin clignotement  
  
    if (Serial.available()) {  
        unsigned long currentMillis = millis();  
        if (currentMillis - previousMillis >= 500) {  
            previousMillis = currentMillis;  
            if (ledR == LOW) {  
                ledR = HIGH;  
            } else {  
                ledR = LOW;  
            }  
            digitalWrite(ledRojo, ledR);  
        }  
  
        String a = Serial.readStringUntil('\n');  
        if (a == "descendreBras") {  
            angleA = 45;
```

```
    angleB = 45;
    angleC = 45;

} else {
    a.remove(0, 1);
    a.remove(a.length() - 1, 1);
    angleA = getValue(a, ',', 0).toFloat();
    angleB = getValue(a, ',', 1).toFloat();
    angleC = getValue(a, ',', 2).toFloat();
}

servoA.writeMicroseconds((-2380 + 1450)*float(angleA) / 90 + 2380);
servoB.writeMicroseconds((-2370 + 1480)*float(angleB) / 90 + 2370);
servoC.writeMicroseconds((-2300 + 1430)*float(angleC) / 90 + 2300);
}
}

String getValue(String data, char separator, int index) {
    int found = 0;
    int strIndex[] = { 0, -1 };
    int maxIndex = data.length() - 1;
    for (int i = 0; i <= maxIndex && found <= index; i++) {
        if (data.charAt(i) == separator || i == maxIndex) {
            found++;
            strIndex[0] = strIndex[1] + 1;
            strIndex[1] = (i == maxIndex) ? i + 1 : i;
        }
    }
    return found > index ? data.substring(strIndex[0], strIndex[1]) : "";
}
```

(Código)

A continuación se encuentra el programa que se realizó para comprobar el funcionamiento de los motores.

```
#include <Servo.h>

#include <math.h>

int ledRojo = 8;

int ledR = LOW;

int i=0;

unsigned long previousMillis = 0;

// Declaramos la variable para controlar el servo

Servo servoA;

Servo servoB;

Servo servoC;

int posicion, posicionA, posicionB, posicionC;

void setup() {

    // Iniciamos el monitor serie para mostrar el resultado

    Serial.begin(9600);

    pinMode(ledRojo, OUTPUT);

    // Iniciamos el servo para que empiece a trabajar con el pin 9

    servoA.attach(9);

    servoB.attach(10);

    servoC.attach(11);

}

void loop() {

    posicionA = 130;

    posicionB = 120;

    posicionC = 115;
```



```
servoA.write(posicionA+5*sin(2*3.14*i*1));  
servoB.write(posicionA+5*sin(2*3.14*i*1+120/10));  
servoC.write(posicionA+5*sin(2*3.14*i*1-120/10));  
  
i++;  
  
Serial.print(i);  
  
unsigned long currentMillis = millis();  
  
if (currentMillis - previousMillis >= 1000) {  
    previousMillis = currentMillis;  
  
    if (ledR == LOW) {  
        ledR = HIGH;  
    } else {  
        ledR = LOW;  
    }  
  
    digitalWrite(ledRojo, ledR);  
}  
}
```

1.3. OCTAVE

El código empieza con la tabla de datos (data) donde aparece la relación entre los ángulos de giro de la plataforma y los ángulos de giro de los motores, la cual no puede mostrarse debido a su gran tamaño ya que ocupa 316.976 filas en el editor del programa.

En esta primera parte de código se definen la relación entre los angulos de giro de la plataforma, theta_x y theta_y con el desplazamiento y con los angulos de los motores theta1, theta2 y theta 3.

```
data_converted=[data(:,1).*cos(data(:,2)*pi/180),data(:,1).*sin(data(:,2)*pi/180),d
ata(:,3:5)];
```

```
    a=15;
```

```
    r1=70;
```

```
    r2=85;
```

```
    l1=51.55;
```

```
    l3=103.1;
```

```
    w1=89.287;
```

```
    w2=89.287;
```

```
    theta=90*pi/180*[-1:0.1:1];
```

```
    theta_x=30*pi/180*[-1:0.1:1];
```

```
    theta_y=30*pi/180*[-1:0.1:1];
```

```
    for x=1:length(theta)
```

```
        d_m1(x)=sqrt(-a^2+2*a*r1*cos(theta(x))+r1^2*(sin(theta(x)))^2-
        r1^2+r2^2)+r1*sin(theta(x))-(sqrt(-
        a^2+2*a*r1*cos(52.97*pi/180)+r1^2*(sin(52.97*pi/180))^2-
        r1^2+r2^2)+(r1*sin(52.97*pi/180)));
```

```
    endfor
```

```
    plot(theta*180/pi,d)
```

```
    for i=1:length(theta_x)
```

```
        for j=1:length(theta_y)
```

```

d1(i,j)=-((l1+l3)*tan(theta_x(i)))/3+((w1+w2)*tan(theta_y(j)))/2;
theta1(i,j)=interp1(d_m1,theta,d1(i,j));
theta1_ref(i,j)=griddata(data_converted(:,1),data_converted(:,2),data_converted(:,3)
,theta_x(i)*180/pi,theta_y(j)*180/pi);
d2(i,j)=2*((l1+l3)*tan(theta_x(i)))/3;
theta2(i,j)=interp1(d_m1,theta,d2(i,j));
theta2_ref(i,j)=griddata(data_converted(:,1),data_converted(:,2),data_converted(:,4)
,theta_x(i)*180/pi,theta_y(j)*180/pi);
d3(i,j)=-((l1+l3)*tan(theta_x(i)))/3-((w1+w2)*tan(theta_y(j)))/2;
theta3(i,j)=interp1(d_m1,theta,d3(i,j));
theta3_ref(i,j)=griddata(data_converted(:,1),data_converted(:,2),data_converted(:,5)
,theta_x(i)*180/pi,theta_y(j)*180/pi);
endfor
endfor

```

En la siguiente parte que se muestra, corresponde a la que genera el plano con los puntos obtenidos en RecurDyn.

```

X_data=[19.46*pi/180,19.45*pi/180,17*pi/180,0,0,0,-19.46*pi/180,-19.45*pi/180,-
17*pi/180];
Y_data=[19.28*pi/180,0.21*pi/180,-18.39*pi/180,19.35*pi/180,0.047*pi/180,-
19.64*pi/180,19.28*pi/180,0.21*pi/180,-18.39*pi/180];
Z_data1=[16.743,32.960,48.042,43.140,52.970,65.530,65.179,73.670,90.702];
Z_data2=[83.907,54.850,29.932,77.060,52.970,28.770,83.907,54.850,29.932];
Z_data3=[65.179,73.670,90.702,43.140,52.970,65.530,16.743,32.960,48.042];
x1=[-0.3:0.1:0.3];
y1=[-0.3:0.1:0.3];
for i=1:length(x1)
    for j=1:length(y1)
z1(i,j)=griddata(X_data,Y_data,Z_data1,x1(i),y1(j));
z2(i,j)=griddata(X_data,Y_data,Z_data2,x1(i),y1(j));
z3(i,j)=griddata(X_data,Y_data,Z_data3,x1(i),y1(j));

```

(Código)

endfor

endfor

Y para terminar con la parte que compara los modelos cinemáticos, aparece el código mediante el cual se han dibujado los planos expuestos en la memoria.

```
figure(1);hold on;mesh(theta_x,theta_y,theta3'*180/pi,"facecolor","c"),
```

```
hold on;
```

```
mesh(-theta_x,-theta_y,theta1_ref,"facecolor","b")
```

```
hold off;
```

```
figure(2);mesh(theta_x,theta_y,theta2'*180/pi,"facecolor","c"),
```

```
hold on;
```

```
mesh(-theta_x,-theta_y,theta2_ref,"facecolor","b"),hold off;
```

```
figure(3);mesh(theta_x,theta_y,theta1'*180/pi,"facecolor","c"),
```

```
hold on;
```

```
mesh(-theta_x,-theta_y,theta3_ref,"facecolor","b"),hold off;
```

```
figure(1);hold on;mesh(x1,y1,z1,"facecolor","g");hold off;xlabel('Tx');ylabel('Ty');zlabel('T1');
```

```
figure(2);hold on;mesh(x1,y1,z2,"facecolor","g");hold off;xlabel('Tx');ylabel('Ty');zlabel('T2');
```

```
figure(3);hold on;mesh(x1,y1,z3,"facecolor","g");hold off;xlabel('Tx');ylabel('Ty');zlabel('T3');
```

A continuación se muestra el código utilizado para representar la grafica mediante la cual hemos obtenido el valor de la masa en función del ángulo alpha.

```
alpha_m=[0:1:90]*pi/180;
```

```
for x=1:length(alpha_m)
```

```
    beta_m(x)=acos((-0.015+0.07*cos(alpha_m(x)))/0.085));
```

```
end
```

```
for i=1:length(alpha_m)
```

```
m(i)=0.32/(9.8*cos(alpha_m(i))*0.07+(9.8/tan(beta_m(i)))*sin(alpha_m(i))*0.07-
9.8*cos(beta_m(i))*0.085+(9.8/tan(beta_m(i)))*sin(beta_m(i))*0.085);
```

```
end
```

```
plot(alpha_m*180/pi,m);
```

Para finalizar con el código generado en Octave, se muestran las pruebas que se realizaron aplicando el método de las raíces para comprobar que tipo de control favorecía al sistema.

```
s = tf('s');
```

```
Kd=0;
```

```
Ki=0;
```

```
Kp=0;
```

```
%g = tf([9.8],[1,0,0]);
```

```
g=(9.8*Kp/s^2)+(9.8*Kd/s)+(9.8*Ki/s^3);
```

```
%g=(Kp*9.8/s^2)+(9.8*Kd/s);
```

```
%g=(Kp*9.8/s^2)+(9.8*Ki/s^3);
```

```
%g=Kp*9.8/s^2;
```

```
%g=9.8*Kd/s;
```

```
%g=9.8*Ki/s^3;
```

```
rlocus(g);
```

(Código)



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ANEXO 2. (MODELO CINEMÁTICO ORIGINAL)

E Détermination des angles θ des servomoteurs

$$\text{Vecteur } \vec{v} : \begin{pmatrix} \cos\beta\sin\alpha \\ \sin\beta\sin\alpha \\ \cos\alpha \end{pmatrix} \perp \pi$$

$$\text{Plan du plateau } (\pi) : \cos\beta\sin\alpha x + \sin\beta\sin\alpha y + \cos\alpha z + d = 0$$

$$\text{Plan vertical contenant le bras du moteur A (planA) : } \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \wedge \begin{pmatrix} -\cos(30) \\ -\sin(30) \\ 0 \end{pmatrix} = \begin{pmatrix} \sin(30) \\ -\cos(30) \\ 0 \end{pmatrix} \Rightarrow \sin(30)x - \cos(30)y = 0$$

$$\text{Plan vertical contenant le bras du moteur B (planB) : } \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \wedge \begin{pmatrix} 0 \\ 1 \\ 0 \end{pmatrix} = \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix} \Rightarrow -x = 0$$

$$\text{Plan vertical contenant le bras du moteur C (planC) : } \begin{pmatrix} 0 \\ 0 \\ 1 \end{pmatrix} \wedge \begin{pmatrix} \cos(30) \\ -\sin(30) \\ 0 \end{pmatrix} = \begin{pmatrix} \sin(30) \\ \cos(30) \\ 0 \end{pmatrix} \Rightarrow \sin(30)x + \cos(30)y = 0$$

$$\text{Vecteur } \vec{a} \text{ se trouvant sur la droite } \text{planA} \cap \pi : \begin{pmatrix} \cos\beta\sin\alpha \\ \sin\beta\sin\alpha \\ \cos\alpha \end{pmatrix} \wedge \begin{pmatrix} \sin(30) \\ -\cos(30) \\ 0 \end{pmatrix} = \begin{pmatrix} \cos\alpha\cos(30) \\ \cos\alpha\sin(30) \\ -\cos(30)\cos\beta\sin\alpha - \sin\beta\sin\alpha\sin(30) \end{pmatrix}$$

$$\text{Vecteur } \vec{b} \text{ se trouvant sur la droite } \text{planB} \cap \pi : \begin{pmatrix} \cos\beta\sin\alpha \\ \sin\beta\sin\alpha \\ \cos\alpha \end{pmatrix} \wedge \begin{pmatrix} -1 \\ 0 \\ 0 \end{pmatrix} = \begin{pmatrix} 0 \\ -\cos\alpha \\ \sin\beta\sin\alpha \end{pmatrix}$$

$$\text{Vecteur } \vec{c} \text{ se trouvant sur la droite } \text{planC} \cap \pi : \begin{pmatrix} \cos\beta\sin\alpha \\ \sin\beta\sin\alpha \\ \cos\alpha \end{pmatrix} \wedge \begin{pmatrix} \sin(30) \\ \cos(30) \\ 0 \end{pmatrix} = \begin{pmatrix} -\cos\alpha\cos(30) \\ \cos\alpha\sin(30) \\ \cos(30)\cos\beta\sin\alpha - \sin\beta\sin\alpha\sin(30) \end{pmatrix}$$

d est la hauteur du plateau au-dessus des moteurs lorsque le plateau est à plat.

$$\text{Point A, position de l'extrémité du bras du moteur A : } A = \begin{pmatrix} 0 \\ 0 \\ d \end{pmatrix} + k \begin{pmatrix} \cos\alpha\cos(30) \\ \cos\alpha\sin(30) \\ -\cos(30)\cos\beta\sin\alpha - \sin\beta\sin\alpha\sin(30) \end{pmatrix} = \begin{pmatrix} X_a \\ Y_a \\ Z_a \end{pmatrix}$$

$$\text{Point B, position de l'extrémité du bras du moteur B : } B = \begin{pmatrix} 0 \\ 0 \\ d \end{pmatrix} + m \begin{pmatrix} 0 \\ -\cos\alpha \\ \sin\beta\sin\alpha \end{pmatrix} = \begin{pmatrix} X_b \\ Y_b \\ Z_b \end{pmatrix}$$

$$\text{Point C, position de l'extrémité du bras du moteur C : } C = \begin{pmatrix} 0 \\ 0 \\ d \end{pmatrix} + t \begin{pmatrix} -\cos\alpha\cos(30) \\ \cos\alpha\sin(30) \\ \cos(30)\cos\beta\sin\alpha - \sin\beta\sin\alpha\sin(30) \end{pmatrix} = \begin{pmatrix} X_c \\ Y_c \\ Z_c \end{pmatrix}$$

$$\|\vec{AB}\| = D \Rightarrow \|\vec{OB} - \vec{OA}\| = D = \left\| \begin{pmatrix} 0 \\ -m\cos\alpha \\ m\sin\beta\sin\alpha + d \end{pmatrix} - \begin{pmatrix} k\cos\alpha\cos(30) \\ k\cos\alpha\sin(30) \\ -k\cos(30)\cos\beta\sin\alpha - k\sin\beta\sin\alpha\sin(30) + d \end{pmatrix} \right\|$$

$$\|\vec{BC}\| = D \Rightarrow \|\vec{OC} - \vec{OB}\| = D = \left\| \begin{pmatrix} -t\cos\alpha\cos(30) \\ t\cos\alpha\sin(30) \\ t\cos\beta\sin\alpha\cos(30) - t\sin\beta\sin\alpha\sin(30) + d \end{pmatrix} - \begin{pmatrix} 0 \\ -m\cos\alpha \\ m\sin\beta\sin\alpha + d \end{pmatrix} \right\|$$

$$\|\vec{CA}\| = D \Rightarrow \|\vec{OA} - \vec{OC}\| = D = \left\| \begin{pmatrix} k\cos\alpha\cos(30) \\ k\cos\alpha\sin(30) \\ -k\cos(30)\cos\beta\sin\alpha - k\sin\beta\sin\alpha\sin(30) + d \end{pmatrix} - \begin{pmatrix} -t\cos\alpha\cos(30) \\ t\cos\alpha\sin(30) \\ t\cos\beta\sin\alpha\cos(30) - t\sin\beta\sin\alpha\sin(30) + d \end{pmatrix} \right\|$$

$$\begin{cases} (-k\cos\alpha\cos(30))^2 + (-m\cos\alpha - k\cos\alpha\sin(30))^2 + (m\sin\beta\sin\alpha + d + k\cos(30)\cos\beta\sin\alpha + k\sin\beta\sin\alpha\sin(30) - d)^2 = D^2 \\ (-t\cos\alpha\cos(30))^2 + (t\cos\alpha\sin(30) + m\cos\alpha)^2 + (t\cos\beta\sin\alpha\cos(30) - t\sin\beta\sin\alpha\sin(30) + d - m\sin\beta\sin\alpha - d)^2 = D^2 \\ (k\cos\alpha\cos(30) + t\cos\alpha\cos(30))^2 + (k\cos\alpha\sin(30) - t\cos\alpha\sin(30))^2 + (-k\cos(30)\cos\beta\sin\alpha - k\sin\beta\sin\alpha\sin(30) + d - t\cos\beta\sin\alpha\cos(30) + t\sin\beta\sin\alpha\sin(30) - d)^2 = D^2 \end{cases}$$

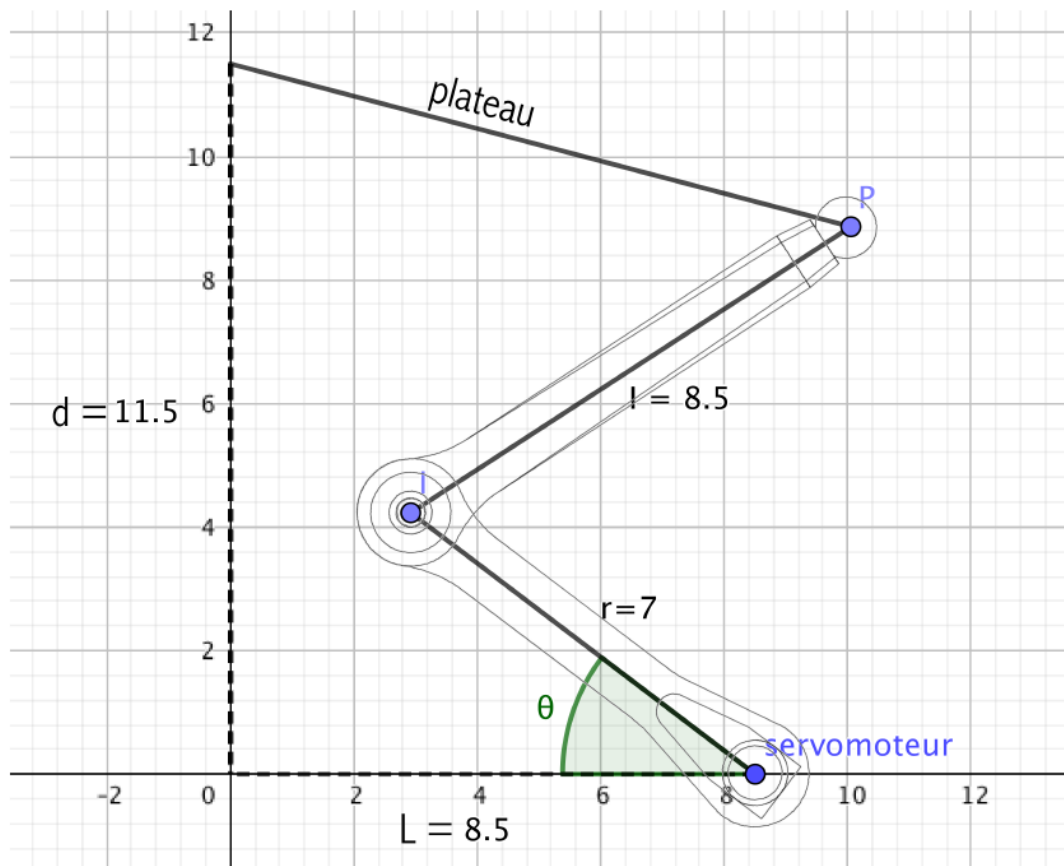
Point I , emplacement de l'articulation du bras d'un moteur : $I(L - r\cos\theta; r\sin\theta)$

Point P , emplacement de l'extrémité du bras d'un moteur : $P(\sqrt{X_p^2 + Y_p^2}; Z_p)$

$$\|\vec{PI}\| = l$$

$$\vec{PI} = \begin{pmatrix} L - r\cos\theta \\ r\sin\theta \end{pmatrix} - \begin{pmatrix} \sqrt{X_p^2 + Y_p^2} \\ Z_p \end{pmatrix}$$

$$(L - r\cos\theta - \sqrt{X_p^2 + Y_p^2})^2 + (r\sin\theta - Z_p)^2 = l^2$$



ANEXO 3. (PRESUPUESTO)

Piezas impresora 3D	Cantidad	Material	Precio
			7,96
Parte inferior de la camara	1	PLA	€
			5,71
Parte superior de la camara	1	PLA	€
			7,20
Parte inferior del soporte camara	1	PLA	€
			3,19
Parte superior del soporte camara	1	PLA	€
			2,71
Soporte PCB	1	PLA	€
			13,62
Contorno base 1	1	PLA	€
			13,27
Contorno base 2	1	PLA	€
			13,03
Contorno base 3	1	PLA	€
			14,62
Contorno base 4	1	PLA	€
			8,62
Contorno base 5	1	PLA	€
			12,34
Parte interior base 1	1	PLA	€
			13,79
Parte interior base 2	1	PLA	€
			13,40
Parte interior base 3	1	PLA	€
			1,23
Sujeccion conector joystck	1	PLA	€
			7,38
Parte inferior articulacion	3	PLA	€
			7,38
Parte superior articulacion	3	PLA	€
			145,45
			€

Posibles piezas impresora 3D (depende medidas impresion)	Cantidad	Material	Precio
Parte superior plataforma	1	Poliamida	142,80 €
Parte inferior plataforma	1	Poliamida	98,28 €
Tapa de la base	1	Poliamida	112,56 €
			353,64 €

Componentes comprados	Cantidad	Precio
Servomotor Futaba S3003	3	48,63 €
Camara	1	36,64 €
Kit de varillas y bolas	1	13,35 €
		98,62 €

El coste total del proyecto asciende a 597,71€.



Relación de documentos

- Memoria NN páginas
 Anexos NN páginas

La Almunia, a 27 de 11 de 2019

Firmado: Raúl López Martín