

1 Uncertainty assessment for on-machine tool 2 measurement: an alternative approach to the ISO 3 15530-3 technical specification

4 Unai Mutilba^{1,*}, Eneko Gomez-Acedo¹, Alejandro Sandá², Ibon Vega² and Jose A. Yagüe-Fabra³

5 ¹ Department of Mechanical Engineering, IK4-Tekniker, Eibar 20600, Spain; eneko.gomez-acedo@tekniker.es
6 (E.G.-A.)

7 ² Department of Production Engineering, IK4-Tekniker, Eibar 20600, Spain; alejandro.sanda@tekniker.es
8 (A.S.); ibon.vega@tekniker.es (I.V.)

9 ³ I3A, Universidad de Zaragoza, Zaragoza 50018, Spain; jyague@unizar.es

10 * Correspondence: unai.mutilba@tekniker.es; Tel.: +34-636-994-351

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12 **Abstract:** Touch probes are commonly employed in new machine tools (MTs), and enable
13 machining and measuring processes to occur on the same MT. They offer the potential to measure
14 components, either during or after the machining process, providing traceability of the quality
15 inspection on the MT. Nevertheless, there are several factors that affect measurement accuracy on
16 shop-floor conditions, such as MT geometric errors, temperature variation, probing system,
17 vibrations and dirt. Thus, the traceability of a measurement process on an MT is not guaranteed
18 and measurement results are therefore not sufficiently reliable for self-adapting manufacturing
19 processes. The current state-of-the-art approaches employ a physically calibrated workpiece to
20 realise traceable on-MT measurement according to the ISO 15530-3 technical specification, but it
21 has a significant limitation in that it depends on a physical workpiece to understand the
22 performance of the systematic error contributor (u_b). To this end, the aim of this paper is to
23 propose an alternative methodology for on-MT uncertainty assessment without using a calibrated
24 workpiece. The proposed approach is based on a volumetric error mapping of the MT prior to the
25 measurement process, which provides an understanding of how the systematic error contributor
26 (u_b) performs. An experimental exercise is performed for a medium-size prismatic component
27 according to the VDI 2617-11 guideline, and the results are compared with the ISO 15530-3
28 technical specification.

29 **Keywords:** uncertainty budget; on-machine tool measurement; traceability; uncertainty
30

31 1. Introduction

32 The development of flexible manufacturing processes for high-quality products at low cost is
33 one of the main research objectives in the field of production technology [1]. The quality inspection
34 of high-value components usually takes place on coordinate measuring machines (CMMs), either
35 beside the production line or in an isolated measurement room, so the manufacturing process is
36 interrupted and transportation, handling and the loss of the original manufacturing setup influence
37 the workpiece quality [2] and the overall equipment effectiveness (OEE). The high investment
38 required for a CMM and the above-mentioned limitations show the need for a machine tool (MT)
39 integrated traceable measuring process.

40 Although on-MT measurement can provide advantages for more flexible and intelligent
41 manufacturing processes, there are also some limitations. The main limitation is that MT time is
42 more expensive than CMM time, so measurements that are executed on an MT should clearly add
43 value to the manufacturing process. Here, it is particularly relevant to determine critical component
44 dimensions and measure them on the MT in order to ensure zero-defect manufacturing processes
45 [3].

46 The current manufacturing scenario shows that dimensional measurements are already being
47 employed for on-MT measurements at different stages of the manufacturing cycle, mainly because
48 the technology to perform a measurement, either touch-trigger probes (TTPs) or measurement
49 software, are already available on the MT side. There are four potential measurement scenarios
50 where on-MT measurement adds value to the manufacturing process: a) monitoring of the MT
51 geometry performance by employing a calibrated standard; b) workpiece set up on the MT
52 coordinate system; c) in-process measurements to provide correction values for the manufacturing;
53 and d) the performance of a final metrology validation of the finished product for final quality
54 inspection as well as statistical trend analysis of the manufacturing process. Nowadays, depending
55 on the size of the component, traceable on-MT measurement technology readiness levels (TRLs) are
56 at different stages: While large-scale manufacturing processes employ on-MT measurements to
57 reduce the setup time of large components on the MT bed, medium-size aeronautic manufacturers
58 are already performing on-MT measurement for the in-process measurement of high-value
59 components such as aircraft engines and components, close to realising a traceable on-MT
60 measurement.

61 From a technology point of view, the aim is to use an MT as a CMM, but there are some key
62 differences between a CMM and an MT, mainly because CMMs are designed for measurement
63 purposes and MTs are focused on manufacturing production. The main problem when executing a
64 measurement on an MT is that the machining and measuring processes are performed using the
65 same machine, and some error sources therefore cannot be distinguished if a calibration process is
66 not realised before the measurement execution [4]. This is currently the main limitation to close the
67 calibration chain for on-MT measurement.

68 Over the years, several standards and guidelines [5–10] have been developed in order to verify
69 the accuracy of either MTs [11–16] or CMMs [6,7], but measurement traceability assessments for on-
70 MT measurements are not as developed as is the case for CMMs. In this scenario, owing to the
71 similarity between CMMs and MTs, some of the methods employed for a correct assessment of
72 uncertainty in CMMs are being adopted for MTs. The general guide for a suitable evaluation of
73 measurement data is given in the ISO Guide 98-3: 2008, on the expression of uncertainty in
74 measurement (GUM) [17]. Three different approaches are considered for an uncertainty assessment
75 on an MT [3]: a) an experimental technique according to ISO 15530-3 technical specification [8]; b) a
76 numerical simulation-based approach, as described in the ISO 15530-4 technical specification [9];
77 and c) an uncertainty budget method based on the VDI 2617-11 guideline [10].

78 Several research works have focused on the idea of converting an MT into a CMM. In 2010,
79 Schmitt et al. proposed that a large MT should be employed as a comparator to measure the
80 geometry of large scale components during the manufacturing process [18]. In 2013, Schmitt et al.
81 also presented a study in which a specific workpiece was manufactured and calibrated on a CMM
82 for several on-MT measurement experimental tests [1]. In this regard, Mutilba et al. reported that a
83 research work where a calibrated workpiece was employed to assess the on-MT measurement
84 uncertainty on a real manufacturing process for a medium-size prismatic component [4]. In 2015,
85 Schmitt et al. went a step further, presenting an approach to determine the uncertainty assessment
86 for on-MT measurements according to the VDI 2617-11 guideline; they defined a maximum
87 permissible error (MPE) [7] for MTs to assess the systematic error of the on-MT measurement error
88 budget [2]. Recently, Holub et al. presented a capability assessment for on-MT measurement
89 assisted by an external laser interferometer [19]. Similarly, Sladek et al. reported an interesting
90 approach for the systematic error assessment of a CMM based on the use of a laser tracer for the
91 volumetric error mapping and compensation of geometric errors. It is an online accuracy-estimation
92 solution based on the virtual coordinate measuring machine (VCMM) concept for CMMs [9,20–22].

93 In this context, this paper presents a methodology to perform traceable on-MT measurements
94 without using a calibrated workpiece, performing the VDI 2617-11 guideline [10]. The approach
95 aims to perform the systematic error (u_b) assessment of on-MT measurements by means of a
96 previous volumetric error mapping of the MT using laser tracer technology.

97 Finally, an experimental exercise was performed on a three linear-axis medium-size MT. It
 98 shows that the uncertainty assessment for a medium-size prismatic component can be performed
 99 without using a calibrated workpiece. Results have been compared to the ISO 15530-3 technical
 100 specification [8].

101 2. On-machine tool measurement uncertainty budget

102 Before presenting the new approach, it is interesting to understand those uncertainty
 103 contributors that should be considered for on-MT measurement uncertainty budget. The ISO 15530-
 104 3 technical specification explicitly presents four uncertainty contributors that consist of all the
 105 systematic and random errors comprising the uncertainty budget for on-MT measurement [8]:

- 106 • u_b : Standard uncertainty associated with the systematic error of the measurement
 107 process.
- 108 • u_p : Standard uncertainty associated with the measurement procedure.
- 109 • u_{cal} : Standard uncertainty associated with the uncertainty of the workpiece calibration.
- 110 • u_w : Standard uncertainty associated with material and manufacturing variations.

111 Thus, the standard uncertainty of the measurement system (u_{MS}) is given by the quadrature
 112 sum of every uncertainty contributor, according to the formula expressed in Equation 1. In
 113 addition, the expanded measurement uncertainty of the measurement system (U_{MS}) is assessed by
 114 $U_{MS} = k \times u_{MS}$ for a coverage factor of $k=2$, as expressed in Equation 2. For the systematic error (u_b)
 115 contributor, different approaches are employed to assess it. If the measurement result is not
 116 corrected by the systematic error (b), the error fully contributes to the uncertainty, so $u_b = b$. Thus:

$$117 \quad u_{MS} = \sqrt{u_p^2 + u_{cal}^2 + b} \quad (1)$$

$$118 \quad U_{MS} = k * u_{MS} \quad (2)$$

119 With respect to the ISO 15530-3 technical specification, the uncertainty u_p is given by the
 120 maximum standard deviation of every measurement performed on the workpiece; therefore, it uses
 121 the experimental (type A) approach. The systematic error is defined as the difference between the
 122 mean value of the on-MT measurement and the calibrated value, and the calibration uncertainty is
 123 given by the workpiece's features calibration on a CMM. Both contributors are evaluated using the
 124 type B method. Further, if variations of form errors and roughness owing to fluctuating
 125 manufacturing processes and material properties are considered within their required limits, the u_w
 126 contribution is considered as insignificant [8]. In this case, u_w is considered negligible, so it is not
 127 introduced in Equation 1.

128 For the VDI 2617-11 guideline, the determination of the on-MT measurement uncertainty is
 129 determined using an uncertainty budget. Here, each uncertainty source and its magnitude on the
 130 measurement result is considered. In this case, the error sources are as follows [2]:

- 131 • The geometric error of the MT and its repeatability.
- 132 • Probing system.
- 133 • Temperature: MT structure, surroundings, and workpiece.
- 134 • Workpiece under measurement: Temperature and clamping.
- 135 • Measurement procedure.
- 136 • Geometric error mapping technique.

137 Those error sources comprise systematic and random errors for the on-MT uncertainty budget
 138 [23]. The result is the on-MT measurement uncertainty for a 95% confidence level.

139 Similar to the ISO 15530-3 technical specification, the systematic error contributor (u_b) on the
 140 VDI 2617-11 guideline is affected by the following error sources: geometric error of the MT, probing
 141 system, workpiece under measurement, measurement procedure, and geometric error mapping
 142 technique. The random contributor (u_p) comprises the MT repeatability, touch probe repeatability,
 143 and temperature variation for the measurement scenario. For the experimental approach presented
 144 below, the measurement procedure and the workpiece under measurement have not been
 145 considered for the uncertainty budget because an easy-to-measure medium-size prismatic
 146 component was measured. Moreover, negligible deformations occur during the clamping process.
 147 In addition, the probing system characterisation and the uncertainty of the MT volumetric error
 148 mapping technique are within $2 \mu\text{m}$. Thus, the uncertainty budget exercise focuses on major
 149 uncertainty contributors. In this manner, the geometric error of the MT is considered as the main
 150 error source within the systematic contributor (u_b), and the effect of the temperature on the
 151 measurement scenario and MT repeatability are highlighted as the main random error contributors
 152 (u_p).

153 Considering those major uncertainty error contributors, this study adopts the random error
 154 characterisation, which performed on the ISO 15530-3 technical specification and which does not
 155 require a calibrated workpiece to understand how (u_p) performs. For the systematic error
 156 contributor (u_b), Schmitt et al. presented an approach where an MPE value was defined for an MT.
 157 Their approach was validated within stable temperature conditions, but they proposed further
 158 research for unstable conditions because an unstable status causes gradients inside the structure,
 159 and the induced deviations are hard to simulate or predict [2]. Considering such limitations, a
 160 volumetric error mapping of the MT is performed immediately before the on-MT measurement
 161 process execution for the systematic error characterisation. Thus, the geometric error of each contact
 162 point is known, and the systematic error contributor (u_b) can therefore be assessed. This research
 163 work does not apply the systematic error value correction, so the error fully contributes to the
 164 uncertainty budget, as in Equation 1.

165 3. Methodology for on-MT uncertainty assessment without a calibrated workpiece

166 A new methodology is proposed to perform the on-MT uncertainty assessment without a
 167 calibrated workpiece:

- 168 • For the systematic error contributor (u_b), a volumetric error mapping of the MT is
 169 performed immediately before the on-MT measurement. Thus, the geometric error of each
 170 point is known for the working volume of the machine, which is the main contributor to the
 171 systematic error of the on-MT measurement. Once the on-MT measurement is performed,
 172 measurement contact points are registered, and the geometric error of every point is
 173 obtained from the volumetric error mapping. Thus, every measured feature is fitted again
 174 while considering the geometric error of each contact point. The difference between the
 175 feature characteristics before and after the second fitting exercise is the systematic error to
 176 be considered on the error budget. Figure 1 shows the flow chart for the systematic error
 177 characterisation.
- 178 • The systematic error originating from the tactile probe could also be considered for the
 179 systematic error contributor (u_b). Thus, as explained by Mutilba et al. [4] if a reliable
 180 calibration of the probing system is performed every time the tactile probe is mounted on
 181 the MT spindle, this contributor becomes negligible. However, if the calibration process is
 182 not executed correctly or if the uncertainty contributor is not sufficiently small ($< 1 \mu\text{m}$ for
 183 small MT and $< 3 \mu\text{m}$ for large MT) the tactile probe systematic error should be added to
 184 the u_b value according to the square root of the sum of squares.
- 185 • The measurement procedure uncertainty (u_p) is performed on the workpiece to be
 186 measured on the MT, similar to the ISO 15530-3 technical specification [8]. Thus, the

187 repeatability of the on-MT measurement is performed within the temperature range of the
 188 measurement scenario, considering that the temperature variation is critical for this
 189 uncertainty contributor. Therefore, several on-MT measurement cycles shall be performed
 190 within the complete temperature range of the measurement scenario. For example, consider
 191 an eolic hub being machined in a large MT, where the temperature variation on the
 192 surrounding air is between 18 °C and 23 °C. The u_p contributor should be assessed by
 193 means of repeated measurement cycles (every 15 min) on the workpiece within the
 194 working temperature range. Equation 3 shows how to calculate the u_p contributor.

- 195 • The u_{cal} contributor is considered as the standard uncertainty associated with the
 196 measurement uncertainty on the systematic error characterisation process.

$$197 \quad \bar{y} = \frac{1}{n} \sum_{i=1}^n y_i \quad u_p = \sqrt{\frac{1}{n-1} \sum_{i=1}^n (y_i - \bar{y})^2} \quad (3)$$

198 where:

- 199 • \bar{y} = mean value of the measurement result.
 200 • y = measured value.
 201 • n = number of measurement results.

202 Figure 1 shows the flow chart for the systematic error characterisation.

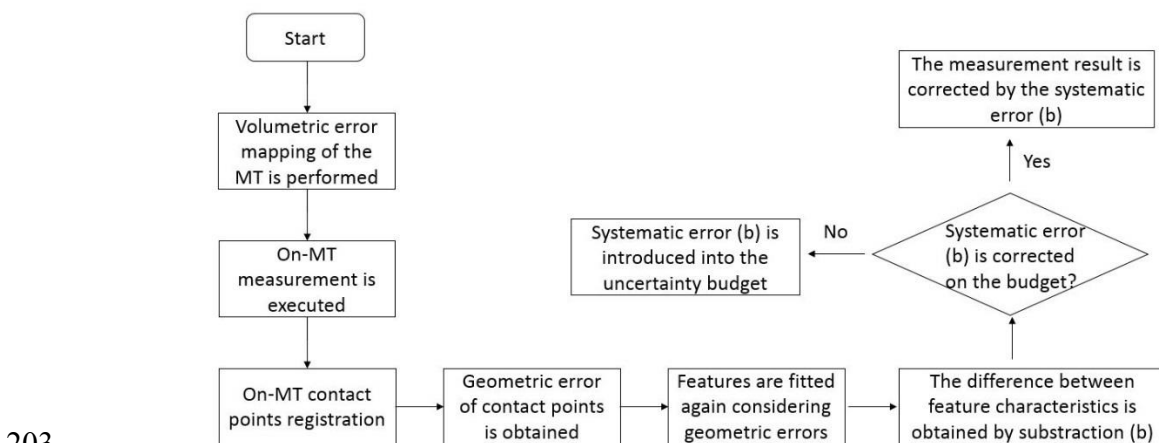


Figure 1. Systematic error assessment methodology.

205 For the geometric fitting of the measured plane and diameters, three dimensional (3D) and two
 206 dimensional (2D) fitting equations have been employed in MATLAB [24]. This fitting exercise
 207 considers the geometric error information of each contact point obtained in this case from the
 208 volumetric error mapping measurement. Results obtained on each fitted feature are compared to
 209 the initial fitting value obtained by the on-MT measurement software, so the difference between
 210 both fittings is the systematic error to be considered on the error budget according to the VDI 2617-
 211 11 guideline. Equation 4 shows the employed algorithm for circumference fitting; the variation of
 212 the radius shows the roundness error.

$$213 \quad r = \sqrt{(x - x_c)^2 + (y - y_c)^2} \quad (4)$$

214 where:

- 215 • r = circumference radius.
 216 • x, y = measured contact points (geometric error in each point is considered).
 217 • x_c, y_c = circumference centre coordinates (to be obtained).

218 For the 3D fitting of the plane, Equation 5 shows the algorithm which was employed in this
 219 experimental exercise. The least-squares fitting algorithm was employed to compare the flatness
 220 error before and after considering the geometric error of the contact points [25].

$$221 \quad f(x_i, y_i, z_i) = p_1 x_i + p_2 y_i + p_3 z_i + 1 \cong 0 \quad (5)$$

222 where:

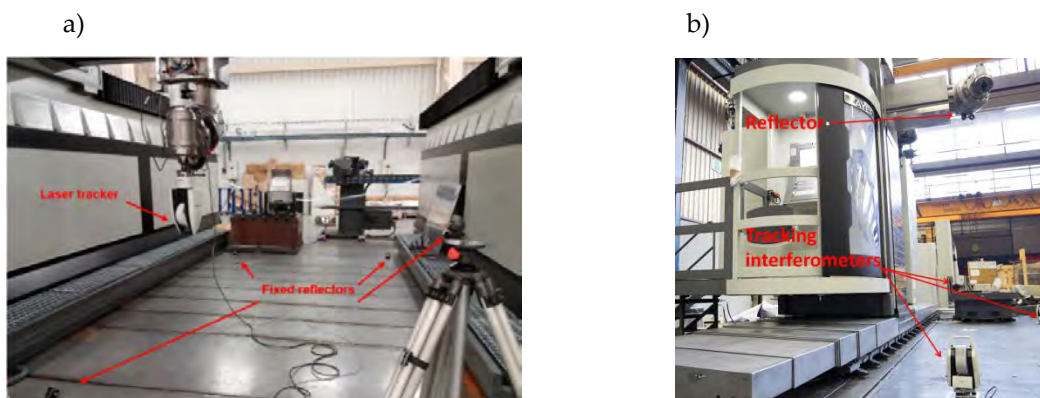
- 223 • p = plane feature parameters.
- 224 • x_i, y_i, z_i = measured contact points (geometric error in each point is considered)

225 4. Technology adoption on a machine tool

226 The presented methodology requires a volumetric error mapping of the MT before performing
 227 the on-MT measurement to characterise the geometric error of the MT as the main error source to
 228 the systematic error (u_b) of on-MT measurement. In this context, as explained by Nisch et al. [18],
 229 there are two main approaches to enable a traceable measurement on MTs: a) the MT geometric
 230 error is known at the moment when the measurement is performed through a volumetric error
 231 mapping of the MT; and b) an external high precision metrological frame is employed to measure
 232 and compensate for the geometric error of the MT in real time [21,22,26,27].

233 Figure 2 shows the above-mentioned two alternatives a) an MT volumetric error mapping
 234 exercise. It shows an integrated multilateration approach reported by Mutilba et al. [30], and b) an
 235 external high-precision metrological frame comprised of four tracking interferometers in
 236 simultaneous mode.

237



238

239 **Figure 2.** Multilateration approaches for MT error mapping a) integrated approach , and b) external
 240 high-precision frame with four tracking interferometers (Both measurements were performed by
 241 IK4-TEKNIKER on a ZAYER large MT)

242 The first approach increases the process capability by a volumetric verification and
 243 compensation of the MT, as shown in Figure 2(a). Currently, there are different options for the
 244 volumetric error mapping of MTs [28], but they are time-consuming, mainly for large-scale MTs. In
 245 this regard, the multilateration approach is suitable for realising such a fast performance. Schwenke
 246 et. al. reported an approach to continuously monitor the geometric variation of a large MT on shop
 247 floor conditions [29], and recently, Mutilba et al. reported an integrated and automatic volumetric
 248 error mapping solution for large MTs which is executed within 30 min [30]. For the proposed
 249 experimental approach, a volumetric error mapping of the MT under research was performed using
 250 laser tracer NG technology in sequential mode.

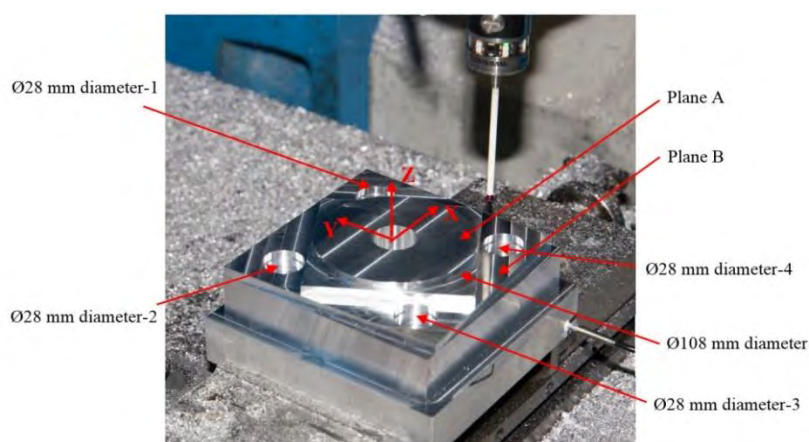
251 The second approach applies an external high precision metrological frame to monitor the tool
 252 centre point (TCP) position in real time. This option requires a line of sight between the measuring
 253 tracking interferometers and the TCP, which cannot be ensured when the workpiece is on the MT.
 254 The current cost of the solution is very high because four interferometers are required

255 simultaneously. However, it offers the possibility of being self-calibrating and represents a scalable
 256 measuring solution.

257 Currently, the first approach is under research, and according to the latest studies, with the
 258 continued development of interferometer-based non-contact measuring technology to realise more
 259 accurate absolute distance measurements, it will be incorporated into MTs, allowing traceable
 260 CMM measurements in MTs [31].

261 5. Uncertainty budget assessment experimental exercise

262 An experimental exercise of the proposed methodology was performed using a workpiece
 263 replica standard. The obtained results were compared to the ISO 15530-3 technical specification.
 264 The workpiece replica standard selected for the experimental uncertainty assessment exercise is
 265 defined at the ISO 10791-7:2014 standard [32], and it is referred as a 'Test piece ISO 10791-7, M1-
 266 160'. A description of the measured geometry is illustrated in Figure 3.

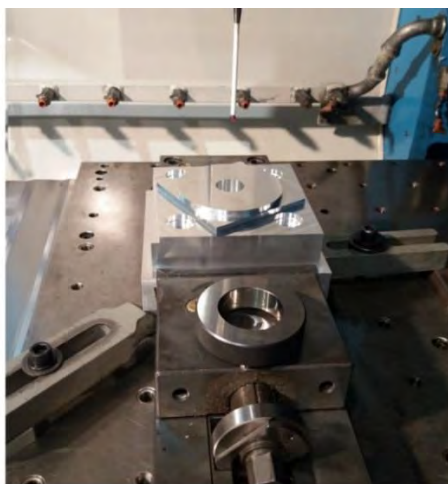
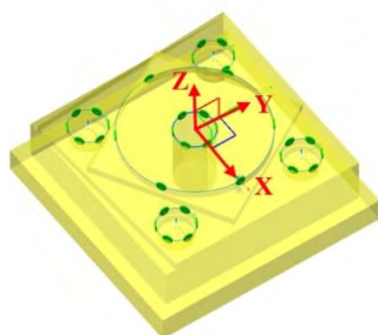


267
 268 **Figure 3.** Workpiece replica standard with measured geometry on the experimental test.

269 A medium-size KONDIA MAXIM MT equipped with a RENISHAW OMP 400 tactile probe
 270 and POWER INSPECT on-MT measurement software was selected to run the on-MT measurement
 271 experimental test. The MT cutting stroke is: X = 750 mm, Y = 1000 mm and Z = 500 mm. The
 272 computer numerical control (CNC) is a 16i-type FANUC controller. For the tactile probe calibration
 273 on the MT spindle, a 50 mm-diameter calibrated ring was employed immediately after it was
 274 mounted on the MT spindle. Figure 4 shows a) the measured contact points for the experimental
 275 on-MT measurement test and b) the measurement scenario on the MT.

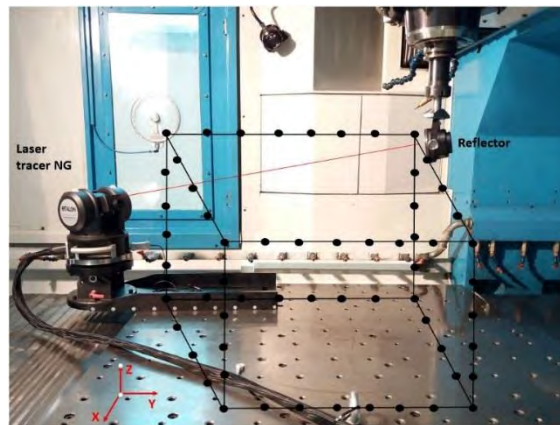
276 a)

b)



277
 278 **Figure 4.** On-MT measurement contact points, a) General overview of the measurement strategy (contact
 279 points in green), and b) the measurement scenario where the workpiece and the calibrated ring are shown.

280 For the systematic error contributor (u_b) assessment, a volumetric error mapping of the MT
 281 was performed immediately before the on-MT measurement. To do this, laser tracer technology
 282 from ETALON AG was employed [33]. It employs a kinematic model which enables to calculate the
 283 geometric error of any point within the measured volume from the volumetric error mapping
 284 information, so the geometric error of the on-MT measurement contacts points was assessed in this
 285 manner. Figure 5 shows the volumetric error mapping exercise and the measured point grid (in
 286 black) of the MT. The laser tracer NG, which is placed on the MT table, measures the distance to the
 287 reflector, which is fixed to the spindle, for every point comprising the point grid under the
 288 multilateration scheme [33]. It demonstrates the technology adoption of the above-mentioned first
 289 approach where a unique tracking interferometer is employed in sequential mode for the MT
 290 volumetric error mapping.

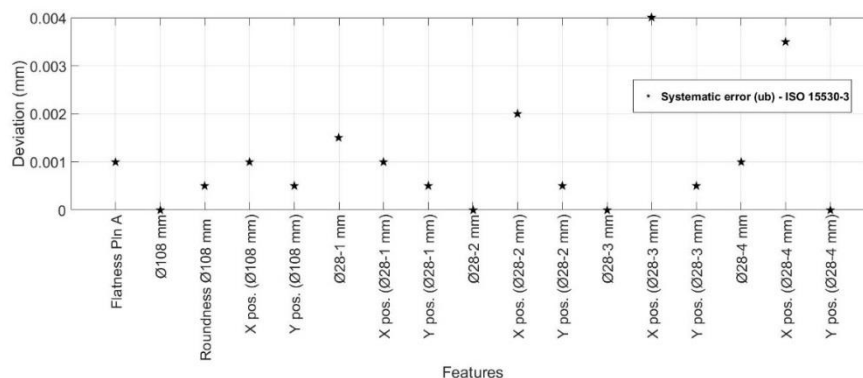


291
 292 **Figure 5.** Volumetric error mapping of MT and measured point grid (in black).

293 The volumetric error mapping measurement was performed under a no-load condition when
 294 the temperature on the MT side was 20 °C, with a temperature variation within 0.5 °C.

295 5.1 On-MT measurement results according to ISO 15530-3 technical specification

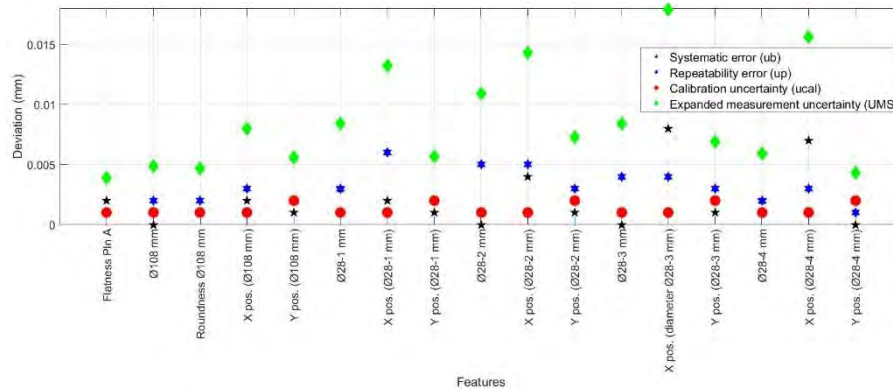
296 The experimental on-MT measurement exercise according to the ISO 15530-3 technical
 297 specification is explained in detail in the article: 'Traceability of on-MT measurement: Uncertainty
 298 budget assessment on shop floor conditions' which was reported by Mutilba et al in 2018 [4]. Here,
 299 the approach is to employ a CMM-calibrated workpiece replica standard to assess the on-MT
 300 measurement uncertainty. Figure 6 shows the absolute value of the systematic error contributor (u_b)
 301 assessed using the calibrated workpiece. All of the results are within 8 μm .



302
 303 **Figure 6.** Systematic error (u_b) according to ISO 15530-3 technical specification. [4]

304 The uncertainty budget of the task-specific uncertainty assessment on shop floor conditions
 305 according to the ISO 15530-3 technical specification [4] is shown in Figure 7. The measurement
 306 procedure uncertainty (u_p) is on average a few micrometres larger on than the systematic error (u_b)
 307 uncertainty, which is within 8 μm for every measured feature. The calibration uncertainty

308 contributor (u_{cal}) is within $2\ \mu\text{m}$ for each feature. Expanded measurement uncertainty results are
 309 obtained by Equation 2 for a coverage factor of $k = 2$, where u_{MS} is given by Equation 1. As
 310 previously mentioned, it should be considered that the systematic error (u_b) contributor is not
 311 corrected on the uncertainty budget, which significantly increases the expanded measurement
 312 uncertainty (U_{MS}) result.



313
 314

Figure 7. Uncertainty budget according to ISO 15530-3 technical specification. [4]

315 5.2 On-MT measurement results according to VDI 2617-11 guideline

316 The main difference for the VDI 2617-11 approach is that a calibrated workpiece is not
 317 employed to assess the systematic error uncertainty contributor (u_b) on the uncertainty budget.
 318 Thus, a volumetric error mapping of the MT was performed immediately before the on-MT
 319 measurement exercise, and the TRAC-CAL software from the company ETALON AG, which
 320 includes kinematic models for point-error determination, was used to calculate the geometric error
 321 of each contact point for the on-MT measurement process. Figure 5 shows the volumetric error
 322 mapping setup on the MT, and Figure 8 shows the 3D deviation result of each measured point
 323 comprising the point grid. The simple ETALON kinematic model was employed, and was
 324 performed by 17 components of the error, and the results are depicted in a 3D deviation-type plot.
 325 The uncertainty for the geometric error mapping measurement is within $1\ \mu\text{m}$. The volume of the
 326 point grid depicted in Figure 8 is similar to the MT cutting stroke, i.e. $X = 750\ \text{mm}$, $Y = 1000\ \text{mm}$ and
 327 $Z = 500\ \text{mm}$.

328
 329

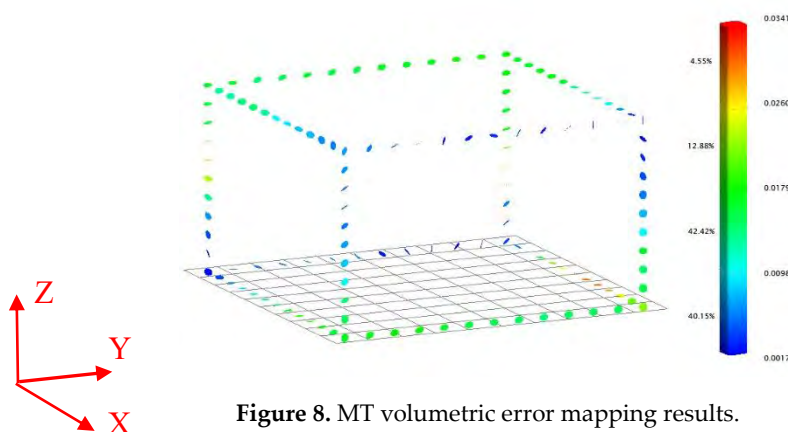
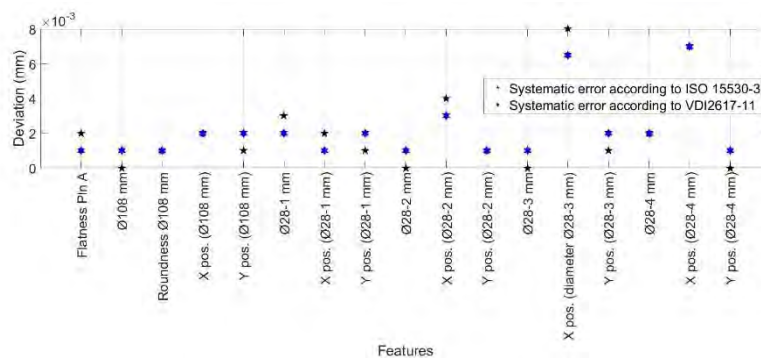


Figure 8. MT volumetric error mapping results.

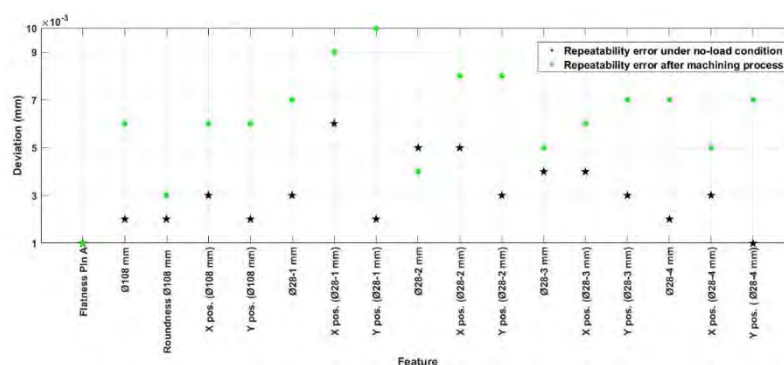
330 The MT volumetric error mapping exercise demonstrates that the geometric error is within $20\ \mu\text{m}$
 331 for almost the entire volume of the machine. Moreover, the workpiece replica standard size is
 332 $160\ \text{mm} \times 160\ \text{mm}$, which means that the geometric error on the MT side that applies to the on-MT
 333 measurement is within $5\ \mu\text{m}$. The volumetric error mapping process also measures the MT
 334 volumetric repeatability; in this case, the MT volumetric repeatability is within $2\ \mu\text{m}$. This means
 335 that either the backlash error or the repeatability itself are within this value.

336 For the systematic error contributor (u_b) assessment, the proposed methodology depicted in
 337 Figure 1 was applied. In addition, a reliable tactile probe calibration was performed prior to the on-
 338 MT measurement exercise to avoid systematic errors due to the probe set-up process. The
 339 repeatability of the calibrated ring measurement is within $1\ \mu\text{m}$, which is similar to the MT
 340 repeatability. In this manner, it was considered to be within the measurement procedure
 341 uncertainty (u_p) on the uncertainty budget. Figure 9 shows a comparison of the systematic error
 342 assessment for the ISO 15530-3 technical specification and the VDI 2617-11 guideline. The difference
 343 between both approaches is within $1.5\ \mu\text{m}$.



344
 345 **Figure 9.** Systematic error (u_b) assessment according to ISO 15530-3 technical specification and VDI
 346 2617-11 guideline.

347 For the measurement procedure uncertainty (u_p), results obtained from the ISO 15530-3-based
 348 experimental test were considered because they do not require a calibrated workpiece. Here, it is
 349 crucial to understand the effect of temperature gradients on the results. Thus, the experimental test
 350 suggests on-MT measurements immediately after the machining process of the workpiece replica
 351 standard and measurements under a no-load condition when the temperature on the MT side and
 352 workpiece side is constant at $20\ ^\circ\text{C}$. The temperature variation on the on-MT measurement scenario
 353 is within $3\ ^\circ\text{C}$, and the workpiece temperature increases to $22.5\ ^\circ\text{C}$ (on average) immediately after
 354 the machining process, after which it stabilises to $19.5\ ^\circ\text{C}$ (on average) after an on-MT measurement
 355 acquisition time of 2h. Figure 10 shows the measurement procedure uncertainty (u_p) for each
 356 measurement feature, both for measurements executed immediately after the machining process as
 357 well as measurements executed under no-load conditions [4].



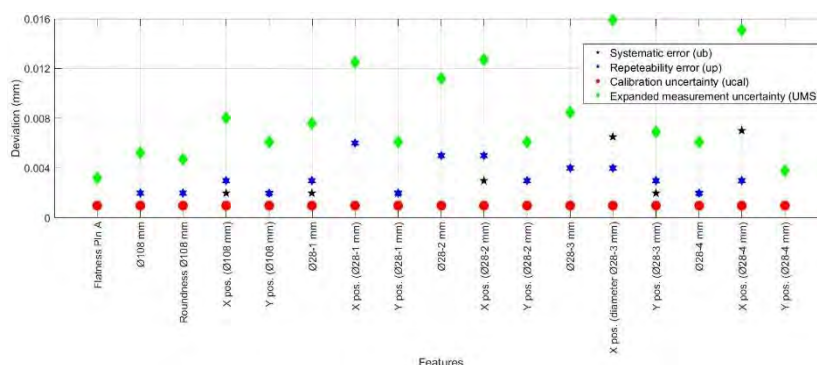
358
 359 **Figure 10.** Measurement procedure uncertainty (u_p) results for both approaches. [4]

360 The measurement procedure uncertainty results (u_p) show differences between the
 361 measurement executed under the no-load condition and the measurements executed immediately
 362 after the machining process. All of the results show repeatability within $6\ \mu\text{m}$ for the no-load
 363 condition, while the maximum repeatability values for the measurements immediately after the
 364 machining process are within $10\ \mu\text{m}$. The form error feature measurement (flatness and roundness)
 365 shows better measurement procedure uncertainty results than the scale-related feature
 366 measurement (diameter and positioning values) because these features are more sensitive to the

367 measurement scenario temperature variation [34]. Here, factors such as the swarf or dirty surfaces
 368 should affect the u_p uncertainty result.

369 For the uncertainty (u_{cal}) contributor, the volumetric error mapping of the MT also indicates the
 370 uncertainty of the volumetric measurement exercise; it is obtained using a Monte-Carlo simulation
 371 technique considering the spatial displacement measurement uncertainty for the laser tracer NG, U
 372 ($k = 2$) = $0.2 \mu\text{m} + 0.3 \mu\text{m}/\text{m}$ [33]. The obtained uncertainty contributor (u_{cal}) of the volumetric error
 373 mapping is within $1 \mu\text{m}$.

374 Finally, the uncertainty budget of the task-specific uncertainty assessment in shop floor
 375 conditions according to the VDI 2617-11 guideline [3] is depicted in Figure 11. Similar to the ISO
 376 15530-3 technical specification, the expanded measurement uncertainty results were obtained using
 377 Equation 2 for a coverage factor of $k = 2$, where u_{MS} is given by Equation 1. For the measurement
 378 procedure uncertainty (u_p), the contribution to the uncertainty budget uncertainty results for the
 379 no-load condition were considered.



380

381 **Figure 11.** Uncertainty budget according to VDI 2617-11 guideline (no-load condition).

382 Finally, Table 1 shows the uncertainty budget assessment within the VDI 2617-11 guideline
 383 and it is compared with the result obtained according to the ISO 15530-3 technical specification.

384 **Table 1** Uncertainty budget according to VDI 2617-11 guideline and comparison with ISO 15530-3 technical
 385 specification. (results in μm)

Feature	u_b	u_p	u_{cal}	u_{MS}	U_{MS} – VDI 2617-11	U_{MS} – ISO15530-3
Flatness Plan A	1.0	0.7	1.0	1.6	3.2	3.9
Ø108 mm	1.0	2.2	1.0	2.6	5.2	4.9
Roundness Ø108 mm	1.0	1.9	1.0	2.4	4.7	4.7
X position (Ø108 mm)	2.0	3.3	1.0	4.0	8.0	8.0
Y position (Ø108 mm)	2.0	2.1	1.0	3.1	6.1	5.6
Ø28-1 mm	2.0	3.1	1.0	3.8	7.6	8.4
X position (Ø28-1 mm)	1.0	6.1	1.0	6.3	12.5	13.2
Y position (Ø28-1 mm)	2.0	2.1	1.0	3.1	6.1	5.7
Ø28-2 mm	1.0	5.4	1.0	5.6	11.2	10.9
X position (Ø28-2 mm)	3.0	5.5	1.0	6.3	12.7	14.3
Y position (Ø28-2 mm)	1.0	2.7	1.0	3.0	6.1	7.3
Ø28-3 mm	1.0	4.0	1.0	4.2	8.5	8.4
X position (Ø28-3 mm)	6.5	4.5	1.0	8.0	15.9	17.9
Y position (Ø28-3 mm)	2.0	2.6	1.0	3.4	6.9	6.9
Ø28-4 mm	2.0	2.1	1.0	3.1	6.1	5.9
X position (Ø28-4 mm)	7.0	2.7	1.0	7.6	15.1	15.6
Y position (Ø28-4 mm)	1.0	1.3	1.0	1.9	3.8	4.3

386 Experimental results show that the uncertainty budget according to the VDI 2617-11 guideline
 387 obtains similar results to what obtained according to the ISO 15530-3 technical specification, where
 388 a calibrated workpiece is employed for the purpose. For the systematic error contributor (u_b), the
 389 difference between both approaches is within $1.5 \mu\text{m}$, which agrees with the accuracy of the
 390 volumetric error mapping performance, i.e. roughly $1 \mu\text{m}$, and also with the backlash error, which
 391 is within the $2 \mu\text{m}$ result that shows the volumetric repeatability. In addition, the calibration
 392 component (u_{cal}) is similar in both cases because of the employed reference standards, whether the
 393 calibrated workpiece or the volumetric error mapping solution have a similar uncertainty
 394 contributor. For the measurement procedure contributor (u_p), the same raw data is employed.

395 6. Conclusions and future work

396 This paper presents an alternative on-MT uncertainty assessment methodology based on the
 397 VDI 2617-11 guideline, which could allow scaling traceable on MT measurements to large-size MTs.
 398 The current approach, which is based on the ISO 15530-3 technical specification, requires a
 399 calibrated workpiece, which is similar to the manufactured part. Therefore, the solution is not very
 400 flexible, especially for larger parts, for which it is tedious and expensive. In addition, it also presents
 401 the two main alternatives for the adoption of the volumetric error mapping technology to MTs.

402 An experimental uncertainty budget of on-MT measurement was presented:

- 403 • Making a comparison with the ISO 15530-3 technical specification, the systematic error
 404 contributor (u_b) on the VDI 2617-11 guideline is shown to be affected by those error sources:
 405 the geometric error of the MT, probing system, workpiece under measurement,
 406 measurement procedure and the geometric error mapping technique.
- 407 • The random contributor (u_p) comprises the MT repeatability, touch probe repeatability, and
 408 temperature variation in the measurement scenario. For the experimental approach, the
 409 measurement procedure and the workpiece under measurement were not considered in the
 410 uncertainty budget because an easy-to-measure medium size prismatic component was
 411 measured. Moreover, negligible deformations occur during the clamping process.
 412 Furthermore, the probing system characterisation and the uncertainty of the volumetric
 413 error mapping technique are within $2 \mu\text{m}$. The former is considered within the procedure
 414 uncertainty contributor (u_p) and the latter is considered as the u_{cal} contributor.

415 The experimental exercise which was performed without a calibrated workpiece shows that
 416 the obtained results are similar to what was obtained using a calibrated workpiece. For the
 417 systematic error contributor (u_b), the difference between both approaches is within $1.5 \mu\text{m}$, which is
 418 similar to the volumetric error mapping uncertainty, for which the difference is approximately 1
 419 μm , and also with the volumetric repeatability of the MT, which includes the backlash error within
 420 $2 \mu\text{m}$. Random errors for both experimental approaches are the same because they were obtained
 421 on the ISO 15530-3 approach.

422 In summary, the methodology offers an opportunity to obtain traceable CMM measurements
 423 on MTs without employing a calibrated workpiece as long as interferometer-based technology is
 424 developed for MT volumetric error mapping and calibration.

425 The results obtained were validated on a three linear axis medium-size MT owing to machine
 426 availability and other practical issues. The future work will focus on scaling the presented
 427 methodology to large MTs similar to those used in large-scale manufacturing; the ISO 15530-3
 428 approach is not affordable because a calibrated workpiece similar to the manufactured part is
 429 required, which makes the solution difficult and expensive.

430 In this scenario, this research work is a gateway to large on-MT traceable measurement.

431

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 433 contributed to the execution of the on-MT measurement in shop floor conditions. J.A.Y.F contributed to the
 434 manuscript. U.M. led the research work and contributed significantly to the paper. All authors contributed to
 435 the editing of the manuscript.

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