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# Characterization of the autonomic nervous system response under emotional stimuli through linear and non-linear analysis of physiological signals

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NERVOUS SYSTEM RESPONSE UNDER  
EMOTIONAL STIMULI THROUGH LINEAR AND  
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**UNIVERSITAT POLITÈCNICA**  
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**CHARACTERIZATION OF THE AUTONOMIC NERVOUS SYSTEM  
RESPONSE UNDER EMOTIONAL STIMULI THROUGH LINEAR AND  
NON-LINEAR ANALYSIS OF PHYSIOLOGICAL SIGNALS**

**A thesis presented for the degree of Doctor of Biomedical Engineering**

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*Remain steadfast on the path with a pristine heart, unmoveable faith and a  
desperate thirst. You shall assuredly discover your own self.*

Sri Ma Anandamayí

To Gerard, Zipi and Zape.

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# Abstract

In this dissertation, linear and non-linear methodologies applied to physiological signals are presented, with the purpose of characterizing the autonomic nervous system response under emotional stimuli. This study is motivated by the necessity of developing a tool which identifies emotions based on their effect on cardiac activity, since it may have a potential impact on clinical practice for diagnosing psycho-neural illnesses.

The dissertation is articulated in five parts: an introduction in which motivation, objectives and relevant physiological aspects are described; the materials used in which the database is detailed as well as its validation; a methodological part in which linear and non-linear techniques are applied to physiological signals; a linear cluster application to the linear and non-linear characteristics; and finally the conclusions of the research.

In the introduction, composed by chapter 1, the motivation of the thesis, the work hypothesis of the research, the objectives achieve in the present dissertation and physiological aspects are described. In particular, the autonomic nervous system control of the heart and the connections between emotions, the sympathetic and parasympathetic nervous systems are highlighted.

The second part is composed by chapter 2, which faces the following issues: description of the

registered signals, details of the registered emotions and the emotion database validation.

In the third part of the dissertation, composed of chapter 3 and chapter 4, two methodological studies are described.

In chapter 3, a method based on the linear analysis of heart rate variability guided by respiration is proposed. The method was based on redefining the high frequency band, not only to be centered at the respiratory frequency, but also to have a bandwidth dependent on the respiratory spectrum. Firstly, the method was tested using simulated heart rate variability signals, yielding the minimum estimation errors as compared to classic and respiratory frequency centered at HF band based definitions, independently of the values of the sympathovagal ratio. Then, the proposed method was applied to discriminate emotions in a database of video-induced elicitation.

In chapter 4, non-linear techniques as the Auto-Mutual and the Cross-Mutual Information Function, the AMIF and the CMIF respectively, are used for human emotion recognition. The AMIF technique was applied to heart rate variability signals to study complex interdependencies, and the CMIF technique was considered to quantify the complex coupling between heart rate variability and respiratory signals. Both algorithms were adapted to short-term RR time series. Traditional band pass filtering was applied to the RR series at low frequency and high frequency bands, and a respiration-based filter bandwidth was also investigated. Both the AMIF and the CMIF algorithms were calculated with regard to different time scales as specific complexity measures. The ability of the parameters derived from the AMIF and the CMIF to discriminate emotions was evaluated on a database of video-induced emotion elicitation.

The fourth part is composed by chapter 5, which is investigated by a linear cluster the linear and non-linear characteristics that discriminate between pairs of emotions and between emotional valences

to determine which parameters allow differentiating between the groups and how many of them are necessary to achieve the best possible classification.

The fifth part is composed by chapter 6, where the main conclusions of the dissertation are exposed.

# Resumen

En esta disertación se presentan metodologías lineales y no lineales aplicadas a señales fisiológicas, con el propósito de caracterizar la respuesta del sistema nervioso autónomo bajo estímulos emocionales. Este estudio está motivado por la necesidad de desarrollar una herramienta que identifique emociones en función de su efecto sobre la actividad cardíaca, ya que puede tener un impacto potencial en la práctica clínica para diagnosticar enfermedades psico-neuronales.

La tesis se articula en cinco partes: una introducción en la que se describen la motivación, los objetivos y los aspectos fisiológicos relevantes; los materiales utilizados en los que se detalla la base de datos, así como su validación; una parte metodológica en la que se aplican técnicas lineales y no lineales a señales fisiológicas; la aplicación de un cluster lineal a las características lineales y no lineales; y finalmente las conclusiones de la investigación.

En la introducción, compuesta por el capítulo 1, se describen la motivación de la tesis, la hipótesis de trabajo de la investigación, los objetivos alcanzados en la presente tesis y los aspectos fisiológicos. En particular, se destacan el control del sistema nervioso autónomo sobre el corazón y las conexiones entre las emociones, los sistemas nerviosos simpático y parasimpático.

La segunda parte está compuesta por el capítulo 2, que se compone de las siguientes partes: de-

scripción de las señales registradas, detalles de las emociones registradas y validación de la base de datos de emociones.

En la tercera parte de la disertación, compuesta por el capítulo 3 y el capítulo 4, se describen dos estudios metodológicos.

En el capítulo 3, se propone un método basado en el análisis lineal de la variabilidad de la frecuencia cardíaca guiada por la respiración. El método se basó en la redefinición de la banda de alta frecuencia, no solo para centrarse en la frecuencia respiratoria, sino también para tener un ancho de banda que dependiera del espectro respiratorio. Primero, el método se validó con señales de variabilidad de la frecuencia cardíaca simuladas, obteniéndose errores mínimos de estimación en comparación con las definiciones de banda clásicas y centradas en la frecuencia respiratoria, independientemente de los valores del ratio simpático-vagal. Después, el método propuesto se aplicó en una base de datos de elicitación emocional inducida mediante vídeos para discriminar entre emociones.

En el capítulo 4, se proponen técnicas no lineales como la función de información mutua y la función de información mutua cruzada, AMIF y CMIF respectivamente, para el reconocimiento de emociones humanas. La técnica AMIF se aplicó a las señales de variabilidad de la frecuencia cardíaca para estudiar interdependencias complejas, y se consideró la técnica CMIF para cuantificar el acoplamiento complejo entre la variabilidad de la frecuencia cardíaca y las señales respiratorias. Ambos algoritmos se adaptaron a las series de tiempo RR a corto plazo. La serie de RR fue filtrada en la banda de alta y baja frecuencia, y también se investigó la serie de RR filtrada en un ancho de banda basado en la respiración.

Tanto el algoritmo AMIF como el CMIF se calcularon con respecto a diferentes escalas de tiempo como medidas de complejidad específica. La capacidad de los parámetros derivados de AMIF y

CMIF para discriminar emociones se evaluó en la base de datos de emociones inducida por vídeo.

La cuarta parte está compuesta por el capítulo 5, en el cual se investiga, mediante un cluster lineal, las características lineales y no lineales que discriminan entre pares de emociones y entre valencias emocionales para determinar qué parámetros permiten diferenciar los grupos y cuántos de éstos son necesarios para lograr la mejor clasificación posible.

La quinta parte está compuesta por el capítulo 6, en la que se exponen las principales conclusiones de la tesis.

# Resum

En aquesta dissertació es presenten metodologies lineals i no lineals aplicades a senyals fisiològiques, amb el propòsit de caracteritzar la resposta del sistema nerviós autònom sota estímuls emocionals. Aquest estudi està motivat per la necessitat de desenvolupar una eina que identifiqui emocions en funció del seu efecte sobre l'activitat cardíaca, ja que pot tenir un impacte potencial en la pràctica clínica per diagnosticar malalties psico-neuronals.

La tesi s'articula en cinc parts: una introducció en la qual es descriuen la motivació, els objectius i els aspectes fisiològics rellevants; els materials utilitzats en els quals es detalla la base de dades, així com la seva validació; una part metodològica en la qual s'apliquen tècniques lineals i no lineals a senyals fisiològiques; l'aplicació d'un clúster lineal a les característiques lineals i no lineals; i finalment les conclusions de la investigació.

A la introducció, composta pel capítol 1, es descriuen la motivació de la tesi, la hipòtesi de treball de la investigació, els objectius assolits en la present tesi i els aspectes fisiològics. En particular, es destaquen el control del sistema nerviós autònom que té sobre el cor i les connexions entre les emocions, els sistemes nerviosos simpàtic i parasimpàtic.

La segona part està composta pel capítol 2, que es compon de les següents parts: descripció dels

senyals registrats, detalls de les emocions registrades i validació de la base de dades d'emocions.

A la tercera part de la dissertació, composta pel capítol 3 i el capítol 4, es descriuen dos estudis metodològics.

En el capítol 3, es proposa un mètode basat en l'anàlisi lineal de la variabilitat de la freqüència cardíaca guiada per la respiració. El mètode es va basar en la redefinició de la banda d'alta freqüència, no només per centrar-se en la freqüència respiratòria, sinó també per tenir un ample de banda que depengués de l'espectre respiratori. Primer, el mètode es va validar amb senyals de variabilitat de la freqüència cardíaca simulades, obtenint errors mínims d'estimació en comparació amb les definicions de banda clàssiques i centrades en la freqüència respiratòria, independentment dels valors de la ràtio simpàtico-vagal. Després, el mètode proposat es va aplicar en una base de dades d'elicitació emocional induïda mitjanant vídeos per discriminar entre emocions.

En el capítol 4, es proposen tècniques no lineals com la funció d'informació mútua i la funció d'informació mútua creuada, AMIF i CMIF respectivament, per al reconeixement d'emocions humanes. La tècnica AMIF es va aplicar als senyals de variabilitat de la freqüència cardíaca per estudiar interdependències complexes, i es va considerar la tècnica CMIF per quantificar l'acoblament complex entre la variabilitat de la freqüència cardíaca i els senyals respiratoris. Tots dos algoritmes es van adaptar a les sèries de temps RR a curt termini. La sèrie RR va ser filtrada a la banda d'alta i baixa freqüència, i també es va investigar la sèrie RR filtrada en un ample de banda basat en la respiració.

Tant l'algoritme AMIF com el CMIF es van calcular respecte a diferents escales de temps com a mesures de complexitat específica. La capacitat dels paràmetres derivats de AMIF i CMIF per discriminar emocions es va avaluar a la base de dades d'emocions induïda per vídeo.



La quarta part està composta pel capítol 5, en el qual s'investiga, mitjanant un clúster lineal, les característiques lineals i no lineals que discriminen entre parells d'emocions i entre valències emocionals per determinar quins paràmetres permeten diferenciar els grups i quants d'aquests són necessaris per aconseguir la millor classificació possible.

La cinquena part està composta pel capítol 6, on s'exposen les principals conclusions de la tesi.

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# Chapter 1

## Introduction

### Contents

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This work has been developed within a joint PhD program in biomedical engineering at both the University of Zaragoza and the Universitat Politècnica de Catalunya.

## 1.1 Motivation

Emotions are an essential part of human existence because they determine the quality of our lives. These represent the evaluation of what happens in our life, but in some people, the affections are disconnected from reality. They have feelings of extreme euphoria (mania) or of desperation (depression) [20,35]. Depression, according to the World Health Organization<sup>1</sup>, is the world's leading cause of disability and contributes very significantly to the global burden of disease affecting 350 million people worldwide.

The emotional responses are formed by behaviors to face specific situations and by physiological responses, both neurovegetative and hormonal, that support these behaviors. The emotional reactions of people to aversive stimuli can harm their health. For example, the stress response, which Cannon called a fight or flight response [19], is useful as a short-term reaction to threatening stimuli, but in the long terms it is detrimental. The autonomic nervous system (ANS) exerts an antagonistic regulation in the organs and target tissues, thanks to the action of its two branches, one sympathetic and the other parasympathetic. Therefore, the stress response includes an increase in the activity of the sympathetic branch of the neurovegetative system and an increase in the secretion of hormones from the adrenal gland: adrenaline, noradrenaline and glucocorticoids. Prolonged exposure to high levels of these hormones can raise blood pressure (BP), damage muscle tissue, lead to infertility, slow growth, inhibit the inflammatory response and depress the activity of the immune system [20,30].

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<sup>1</sup><http://www.who.int/>

The organs of the immune system are also terminal organs of direct autonomic innervation [37,91], especially of the sympathetic nervous system [36]. The sympathetic denervation of the immune organs results in an increase in susceptibility to infectious and inflammatory diseases [91]. And on the other hand, there is a circuit of the nervous system composed of the limbic cortex, the limbic regions of the forebrain, the hypothalamus and the autonomous nuclei of the brainstem, which regulates autonomic and neuroendocrine flow and, thereby, contributes to modulate the immune system [37]. In addition, specifically the cortical areas and the limbic system of the forebrain mediate the affective and cognitive processes and, consequently, may be involved in the response to stressors, in states and affective disorders [52], and in aversive conditioning [37].

In addition, both the sympathetic and parasympathetic branches innervate the heart, specifically in the sinoatrial node (SA node), which allows the corresponding neurotransmitters to modulate their activity. The different emotional states cause a reaction in the ANS, which is reflected in the heart rhythm, due to this neuromodulation. Sympathetic hyperactivity, observed in response to sexual or combative nature can cause extra systole or tachycardia. Parasympathetic hyperactivity, observed in responses to aversive emotions, usually olfactory or visual origin, can cause bradycardia or cardiac arrest [30,96].

Therefore, emotional disorders are the result of the interaction between multiple factors, which depend both on the individual's environment and the individual's characteristics such as genetic, endocrine, nervous, immunological, emotional, cognitive and behavioral characteristics, gender, life experiences and psychosocial factors such as personal support and the perception of control. In addition, stressful situations processed by the interpretative belief system, typical of each individual, can generate negative feelings of fear, anger, depression, helplessness and hopelessness. These at-



titudes and emotions activate biochemical mechanisms, at the level of the hypothalamus, pituitary gland and adrenal glands, which tend to depress and/or suppress the immune response, which makes possible the development of diverse pathological processes [36, 52, 96].

Developing a tool which identifies human emotions may have a potential value in several fields. First, in the clinical practice, it may have value to reduce the diagnostic time of a psycho-neural illness, and, subsequently, it could directly represent a beneficial economic impact for the health system. Secondly, it can improve on the human-machine interaction since it could provide knowledge regarding the affective state of a user, bringing the machine closer to the human by including emotional content in the communication [23].

Several strategies have been proposed for emotion recognition by means of non-invasive techniques that allow registering biosignals as electroencephalography (EEG) [23, 55, 58, 66, 81, 90], galvanic skin response (GSR) [83, 92], skin temperature variation (ST), electrodermal activity [54] and electrocardiography (ECG) [9, 48, 84, 107], among others.

Among all the techniques mentioned, this work has been focused on emotion recognition by means of heart rate variability (HRV) analysis extracted from the ECG, because, as explained above, emotional stimuli cause an action on the hypothalamo-pituitary-adrenal axis, which has an effect on the ANS, and both branches, sympathetic and parasympathetic, have a field of action on the heart. For this reason, studying the electrical impulses of the heart by means of electrocardiography turns out to be a non-invasive measure of the autonomous cardiac response. In the same way, the spectral analysis of HRV is considered a non-invasive technique for evaluating the relationship between these two main branches of ANS and has been proposed for the recognition of human emotions in previous studies [23, 84]. Measurement standards, physiological interpretation and clinical use of

HRV under resting conditions have been previously established, which include three different spectral components: a very low frequency component (VLF) in the range between 0 Hz and 0.04 Hz, a low frequency component (LF) between 0.04 Hz and 0.15 Hz, and a high frequency component (HF) between 0.15 Hz and 0.4 Hz [94].

Sympathetic activity in the heart is encompassed in the power of the LF band and parasympathetic activity is included in both the LF and HF power bands. The influence of ANS in the HF band is mainly due to respiratory sinus arrhythmia (RSA). However, the spontaneous respiratory frequency ( $F_R$ ) is not limited to the band from 0.15 to 0.4 Hz. For example,  $F_R$  can be as low as 0.1 Hz during relaxation and as high as 0.7 Hz in different contexts. In these situations, the spectral analysis of the HRV within the standard frequency bands is an inaccurate measure of ANS activity. This problem has been studied in previous works [5, 7, 8, 43] where it is proposed that the HF band focus on the  $F_R$  but with fixed bandwidth, which does not avoid the problem to consider general spectral limits for all the analyzed subjects.

Besides all these techniques and strategies, the objective of this thesis is to develop a methodology that allows the characterization of emotional responses based on the study of HRV. This methodology will take into account the current limitations for a correct emotional identification of the subject. Therefore, an estimation of the spectral bands particularized for each subject will be taken into account, which will avoid the subjectivity of selection of the width of the HF band that depends to a great extent on considerations such as the age and physiological conditions of each person. This methodology will be developed based on algorithms of linear analysis of the signal.

In addition, within the framework of this thesis it is intended to expand the study of linear analysis with techniques based on the analysis of non-linear dynamics, in order to study the complexity

of the related cardiac signals. The study of the non-linear dynamics of these signals can provide very meaningful information on the characterization of the ANS [54, 89, 106]. The most important limitation presented by these techniques is that they need a sufficient signal length to be applied [54]. Therefore, it will be necessary to adapt the algorithms developed to be robust methods of analyzing short-term signals.

## 1.2 Work hypothesis

The starting hypotheses of this research work are listed below:

**First work hypothesis:** *emotions cause alterations on the autonomic nervous system.*

The effects of ANS on the heart are mediated through hypothalamic communications with spinal cardiovascular centers. This explains why cardiovascular responses are usually connected with some emotional responses, because an emotional stimulus regulates the activation and inhibition of communication between the hypothalamus, the pituitary and other peripheral glands. Therefore, the hormonal release of these glands has a direct effect on the heart. For example, the cardiovascular reaction to a stressful event is to increase BP, caused by an increase in the activity of the sympathetic system, a decrease in parasympathetic activity and the secretion of hormones from the adrenal gland: adrenaline, noradrenaline and glucocorticoids [10, 20, 71].

**Second work hypothesis:** *the alterations that cause the emotions on the ANS can be measured by means of analysis of physiological signals.*

An objective and non-invasive measurement of the ANS is done by studying the variability of the heart rhythm by processing the HRV signal which allows the balance between the sympathetic and

the parasympathetic system of the measured subject to be obtained [94] and therefore the emotional response. Many studies have been published showing the existing changes in HRV during different emotional states [103, 106], however, there are some limitations in the methods currently used. Within this thesis, several robust methods are proposed, both in the linear and non-linear analysis for the characterization of the response of the ANS to emotional stimuli, which take into account the limitations of the HRV analysis, such as the non-stationarity of the signal, changes in heart rate, a respiratory rate outside the classic range, among others.

Hernando, A., published that the HRV analysis methods are a suitable technique for the evaluation of stress [48], as long as respiratory information is taken into account. Rantanen, A., et al. [85] shows the evidence that the elicitation of the negative valence increases sympathovagal activity in women and Quintana, D. S., et al. [84] suggests that the increase in HRV may provide a new marker for recognizing emotions in humans.

On the other hand, Nyguen, V.T., et al. [73], found that cardiac activity is represented in the center of the posterior insula and demonstrated the perception of internal physiological processing states during the natural emotional experience providing an ecologically valid framework to elucidate the neuronal bases of emotional deficits in the neuropsychiatric disorders.

Several studies have revealed that patients with anxiety and phobias exhibit a low HRV. Therefore, a low HRV has been linked to psychological problems [15, 17, 32, 38, 39, 67, 70]. In addition, subjects with post-traumatic stress disorder consistently show a lower HRV [24, 25, 93]. Similarly to these studies, others researchers also suggest a connection between a low HRV and depression [21, 22, 53]. It is important to note that the relationship of a low HRV between anxiety, phobias, stress and depression exists independently of age, gender, cardiorespiratory capacity, heart rate, BP and

respiratory rate [32].

### 1.3 Objectives and outline of the thesis

The objective of this thesis is to develop a methodology that allows the characterization of emotional responses based on the study of HRV. This methodology will take into account the current limitations to characterize emotional responses and thus achieve a correct emotional identification of the subject, and also will consider both linear and non-linear HRV analysis parameters. As for the linear indices, an estimation of the spectral bands particularized for each subject will be proposed. Regarding non-linear parameters, this work is focused on the definition of robust and complexity measurements in short time series.

This general objective can be subdivided into:

**In chapter 3:** it is proposed the joint analysis of HRV and respiration (RSP) based on the spectral correlation of the high frequency band to improve human emotion characterization.

This methodology is based on the automatic detection of spectral limits, particularized for each subject, to avoid subjectivity in the selection of high-frequency bandwidth, since it strongly depends on individual considerations such as age and physiological conditions. Therefore, HF band will be defined based on the maximum spectral correlation between HRV and RSP. The maximum spectral correlation itself is proposed as an index to identify emotions. The hypothesis is that this index, characterizing the relationship between RSP and HRV, can add relevant information to HRV analysis to describe human emotions.

First, a simulation study is designed to evaluate the ability of the proposed HF band to quantify

RSA. The performance of the proposed HF band will be compared to other commonly used HF band definitions. Then, the ability of the proposed indices to characterize human emotions will be tested on a database of video-induced emotions.

Part of the work presented in this chapter has been published in:

[100] Valderas, M.T., Bolea, J., Laguna, P., Vallverdú, M. and Bailón, R., Human emotion recognition using heart rate variability analysis with spectral bands based on respiration, *37th International Conference on IEEE EMBS International Conference on Engineering in Medicine and Biology Society*, 2015, 6674-6677, DOI: 10.1109/EMBC.2015.7319792.

[101] Valderas, M.T., Bolea, J., Orini, M., Laguna, P., Orrite, C., Vallverdú, M. and Bailón, R., Human emotion characterization by heart rate variability analysis guided by respiration, *IEEE Journal of Biomedical and Health Informatics*, 2019, DOI: 10.1109/JBHI.2019.2895589.

**In chapter 4:** it is proposed to use non-linear techniques for HRV analysis because it has been demonstrated that it is a complementary tool of HRV analysis based on linear statistics for ANS analysis [50].

In the present work, both non-linear Auto-Mutual Information Function (AMIF) and Cross-Mutual Information Function (CMIF) techniques are proposed for human emotion recognition. On the one hand, the AMIF technique is applied to HRV signals to study complex communication within the ANS, and on the other hand the CMIF technique is considered to quantify the complex coupling between HRV and respiratory signals.

Both algorithms will be adapted to short term time series and applied to the redefined HF band described in chapter 3, as well as to classic LF and HF bands. Both AMIF and CMIF algorithms

will be calculated on these spectral bands with regard to different time scales as specific complexity measures. The ability of the parameters derived from the AMIF and the CMIF to discriminate emotions will be evaluated on a database of video-induced emotion elicitation.

Part of the work presented in this chapter has been published in:

[99] Valderas, M.T., Bolea, J., Laguna, P., Bailón, R. and Vallverdú, M., Mutual information between heart rate variability and respiration for emotion characterization, *Physiological Measurements*, Volume 40, Number 8, 2019, DOI: 10.1088/1361-6579/ab310a.

**In chapter 5:** it is proposed to use a linear cluster to identify the linear and non-linear characteristics that discriminate between pairs of emotions and between emotional valences to determine which parameters allow differentiating between the groups and how many of them are necessary to achieve the best classification.

The work presented in this chapter is being prepared to be sent to a research journal.

## 1.4 Physiological aspects

### 1.4.1 The autonomic nervous system

The autonomic nervous system is the component of the peripheral nervous system that controls cardiac muscle contraction, visceral activities, and glandular functions of the body. Specifically the ANS can regulate heart rate, BP, rate of respiration, body temperature, sweating, gastrointestinal motility and secretion, as well as other visceral activities that maintain homeostasis [16,46,62,86].

The ANS functions continuously without conscious effort. The ANS, however, is controlled by centers located in the spinal cord, brain stem, and hypothalamus [42].

#### 1.4. PHYSIOLOGICAL ASPECTS

The ANS is composed of a sympathetic division and a parasympathetic division (Fig. 1.1). The sympathetic nervous system is named for acting in sympathy with emotions. In combination with anger or fear, the sympathetic nervous system prepares the body for fight or flight. It produces the heart rate increases, the pupils dilate, the skin sweats, the blood is directed from the skin and the intestinal tube to the skeletal muscles and the sphincters of the digestive tract and the urinary system are closed. The parasympathetic nervous system usually counteracts the effect of the sympathetic nervous system. It adapts the eyes to the near vision, slows down the heart, favors the secretion of saliva and intestinal secretions and accelerates intestinal peristalsis [96].

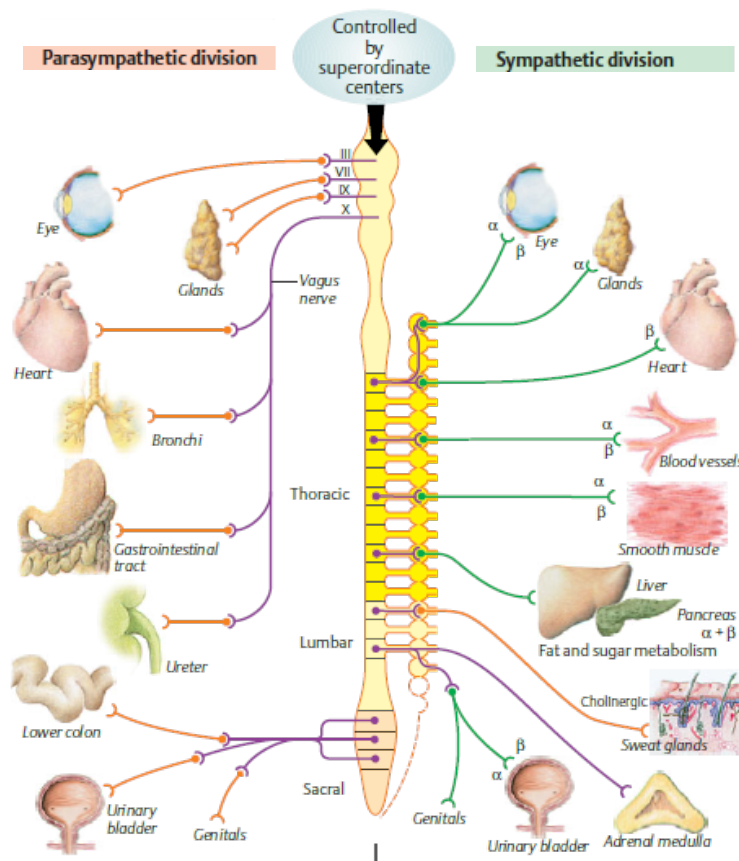


Figure 1.1: Schematic view of the autonomic nervous system composed of a sympathetic division and a parasympathetic division (From [30]).

The sympathetic nervous system releases norepinephrine while the parasympathetic nervous system releases acetylcholine. Both sympathetic and parasympathetic pathways are composed of a pregan-



glionic neuron and a postganglionic neuron. The neurotransmitter between the preganglionic and postganglionic neurons is acetylcholine. Messages from these systems are conveyed as electrical impulses that travel along axons and cross synaptic clefts using chemical neurotransmitter [42].

In the sympathetic system (thoracolumbar division), these nerves originate from the thoracolumbar region of the spinal cord (T1-L2) and radiate out towards the target organs. In contrast, the nerves of the parasympathetic system originate within the midbrain, pons and medulla oblongata of the brain stem and part of these fibers originate in the sacral region (S2-S4 sacral spinal nerves) of the spinal cord. While sympathetic nerves utilize a short preganglionic neuron followed by a relatively long postganglionic neuron, parasympathetic nerves (e.g., the vagus nerve, which carries about 75 percent of all parasympathetic fibers) have a much longer preganglionic neuron, followed by a short postganglionic neuron [42].

### **1.4.2 The autonomic nervous system control of the heart**

The heart is divided into four chambers: upper left and right atria; and lower left and right ventricles. It serves as the pump that moves blood through blood vessels thereby providing the needed oxygen and nutrients to the body. To achieve this goal, the heart must beat with a rhythm determined by a group of pacemaking cells in the SA node located in the right atrium. These cardiac cells generate action potentials that causes contraction of the heart, traveling through the atrioventricular node and along the conduction system of the heart [42].

The electrical activity in the heart is coordinated by the intrinsic conduction system which can be seen on an ECG [42].

Under normal conditions, the P wave of a ECG recording reflects atrial depolarization followed

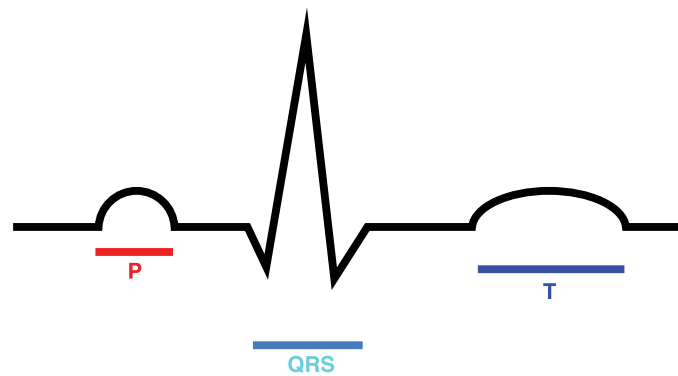


Figure 1.2: Schematic view of a normal electrocardiogram: P = P wave, QRS = QRS complex and T = T wave.

by atrial contraction. The QRS wave reflects ventricular depolarization followed by ventricular contraction and the T wave reflects ventricular repolarization and ventricular relaxation (Fig. 1.2) [42].

In the absence of extrinsic neural or hormonal influences, the SA node pacing rate would be about 100 beats per minute. The heart rate and cardiac output, however, must vary in response to the needs of the body's cells for oxygen and nutrients under varying conditions. In order to respond rapidly to changing requirements of the body's tissues, the heart rate and contractility are regulated by the autonomic nervous system, hormones, and other factors [42].

The regulation of the heart by the ANS is accomplished by control centers in the medulla that receive descending input from higher neural areas in the brain and afferent input from mechanically and chemically sensitive receptors located throughout the body [69]. The principal mechanisms in the brain that regulate the cardiovascular system are: 1) feedforward regulation, often referred to as central command, and 2) feedback or reflex regulation. These cardiovascular regulatory mechanisms are closely coordinated with respiratory and other regulatory mechanisms to maintain homeostasis [27].

The SA node responds clearly to emotional states. Sympathetic hyperactivity, in response to emotions of rapprochement of a sexual or combative nature, can cause the heart to lose a beat (extrasystole) or the pulse run (tachycardia). Parasympathetic hyperactivity in response to aversive emotions is usually of olfactory or visual origin, can cause bradycardia, or even cardiac arrest [96].

During rest, sleep, or emotional tranquility, the parasympathetic nervous system predominates and controls the heart rate at a resting rate of 60-75 beats per minute (bpm). At any given time, the effect of the ANS on the heart is the net balance between the opposing actions of the sympathetic and parasympathetic systems [42].

### **1.4.3 Heart rate variability**

Heart rate variability describes variations in consecutive cardiac cycles. Other terms have been used in the literature, for example cycle length variability, heart period variability, RR variability where R is a point corresponding to the peak of the QRS complex of the ECG wave, and RR interval tachogram [94]. In Fig. 1.3, 10 seconds of an ECG are shown with its corresponding tachogram. HRV exhibit temporal fluctuations, as shows Fig. 1.3, which are synchronized with RSP, increasing during inspiration and decreasing during expiration. This phenomenon called RSA reflects the changes in cardiac autonomic regulation [12].

The HRV analysis provides a tool for the evaluation of cardiac autonomic changes in patients. In fact, reduced HRV is associated with a variety of cardiovascular risk factors and disease states including diabetes, smoking, obesity, work stress, hypertension and heart failure [12].

Many techniques have been proposed to quantify the HRV in order to provide indices of cardiac autonomic regulation in both health and disease. Most of them were include in the Task Force

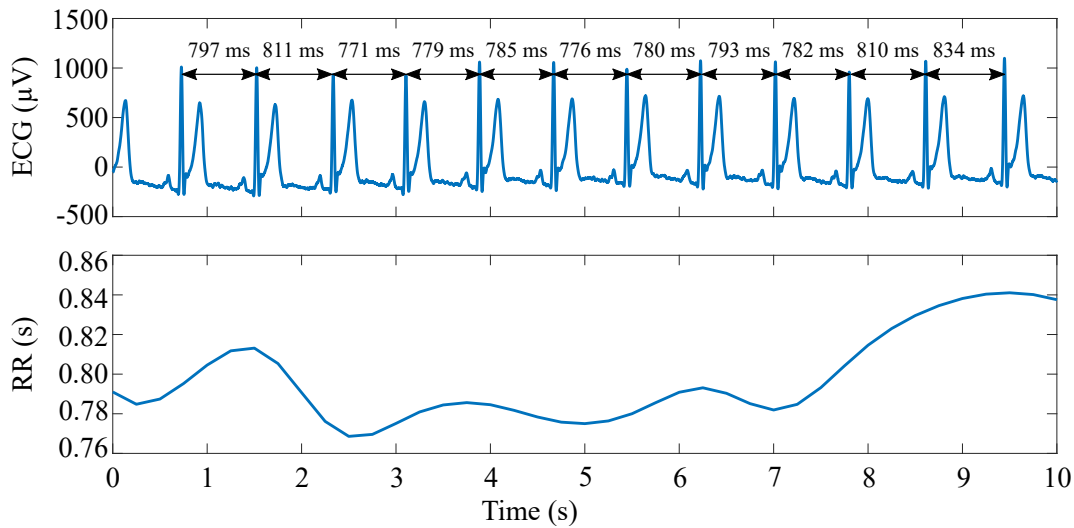


Figure 1.3: Ten seconds of (a) Electrocardiogram (ECG) - Lead II with the time duration of all RR intervals, and (b) RR time series interpolated to 4 Hz.

of 1996 [94]. There are two primary approaches for the analysis of HRV: linear and non-linear methods [12]. The linear methods are divided in the time domain and frequency domain methods, and they are reported in Table 1.1, and Table 1.2, respectively.

The time domain measures, reported in Table 1.1, are easier to calculate but less useful than the frequency domain approaches in identifying specific components of this variability [12]. Regarding the frequency domain measures, three main peaks are often identified for shorter duration recordings (2-5 min): VLF ( $f \leq 0.04$  Hz), LF ( $f \in [0.04-0.15]$  Hz), and HF ( $f \in [0.15-0.4]$  Hz). It should be noted that in response to exercise HF is shifted to a higher frequency ranges ( $f \in [0.24-1.04]$  Hz) [11]. A fourth peak, ultra low frequency (ULF) ( $f \in [0.03-0.04]$  Hz) appears during longer recording periods (24 h).

The sympathetic modulation of cardiac activity is encompassed in LF band and the parasympathetic activity affects both LF and HF band power [94]. The ratio of LF to HF (LF/HF) has been used as an index of the sympathetic/parasympathetic balance. However, this concept has been challenged as there is considerable controversy concerning the relationship between these frequency components

and a particular division of the autonomic nervous system [12].

As was previously mentioned, non-linear dynamic analysis approaches have also been used to evaluate HRV: dominant Lyapunov exponent, detrended fluctuation analysis, approximate entropy, quadratic coupling, auto-mutual information function or cross mutual information function [1, 49, 50, 102–106].

Table 1.1: Time-domain measures of HRV, from [94].

Variable (Units)	Description
SDNN (ms)	SD of all NN.
SDANN (ms)	SD of the averages of NN in all 5 min segments of the entire recording.
RMSSD (ms)	The square root of the mean of the sum of the squares of differences between adjacent NN.
SDNN index (ms)	Mean of the SD of all NN for all 5 min segments of the entire recording.
SDSD (ms)	SD of differences between adjacent NN.
NN50 count	Number of pairs of adjacent NN differing by more than 50 ms in the entire recording.
pNN50 (%)	NN50 count divided by the total number of all NN.
HRV triangular index	Total number of all NN divided by the height of the histogram of all NN measured on a discrete scale with bins of 7.8125 ms (1/128 s).
TINN (ms)	Baseline width of the minimum square difference triangular interpolation of the highest peak of the histogram of all NN.
Differential index (ms)	Difference between the widths of the histogram of differences between adjacent NN measured at selected heights.
Logarithmic index	Coefficient $\phi$ of the negative exponential curve $ke^{-\phi t}$ which is the best approximation of the histogram of absolute differences between adjacent NN.

NN = NN intervals corresponding to heart period during sinus rhythm.

SD = Standard deviation.

Table 1.2: Frequency-domain measures of HRV, from [94].

Variable (Units)	Description
power ( $\text{ms}^2$ )	The variance of NN over 5 minutes.
VLF ( $\text{ms}^2$ )	Power in very low frequency range ( $f \leq 0.04$ Hz).
LF ( $\text{ms}^2$ )	Power in low frequency range ( $f \in [0.04-0.15]$ Hz).
LF norm (n.u.)	Low frequency power in normalized units ( $\text{LF}/(\text{Total PowerVLF}) \times 100$ ).
HF ( $\text{ms}^2$ )	Power in high frequency range ( $f \in [0.15-0.4]$ Hz).
HF norm (n.u.)	High frequency power in normalized units ( $\text{HF}/(\text{Total PowerVLF}) \times 100$ ).
LF/HF	Ratio $\text{LF}(\text{ms}^2)/\text{HF}(\text{ms}^2)$ .

### 1.4.4 Physiology of emotions

Paul Ekman described in 1992 a theory about the six basic emotions as anger, disgust, fear, happiness, sadness and surprise [34]. These 6 basic emotions were discretely categorized because several theories believe they are distinguishable by biological processes and an individual's facial expression [26]. Despite the classification described by Paul Ekman, disgust and surprise were discarded to record because the psychologists involved in the study decided these two emotions were specific reactions rather than prolonged moods.

Emotions activate biochemical mechanisms at the level of the hypothalamus, pituitary, and other peripheral glands. These tend to restore or suppress the immune and endocrine responses, making the development of diverse pathological processes possible [41].

Transient behavior of the cardiovascular function is often linked with some emotional responses. In particular, heart rate is profoundly influenced by neural inputs from sympathetic and parasympathetic divisions of the ANS, which allows the modification of cardiac function to meet the changing homeostatic needs of the body [71]. For example, cardiovascular reaction to a perceived stress situation creates an increase in BP as a consequence of a general increase in cardiovascular sympathetic nerve activity and a decrease in parasympathetic activity [3, 10, 71]. When adrenergic sympathetic fibers activate, they release noradrenaline on cardiac cells, increasing the heart rate. When cholinergic parasympathetic nerve fibers activate, they release acetylcholine on cardiac muscle cells and the heart rate decelerates [96]. Sympathetic and parasympathetic activation work to increase and decrease cardiac pumping, respectively [30]. Usually, an increment in parasympathetic nerve activity is accompanied by a reduction in sympathetic nerve activity, and vice versa.

Several strategies have been proposed for recognition of emotional states assessed by means of HRV

spectral analysis [15, 24, 29, 40, 68, 84, 85]. As mention before, HRV is influenced by RSA. RSA has been used as an index of cardiac vagal or parasympathetic function, usually measured by the HF component of the HRV [111], while the LF component is affected by both sympathetic and parasympathetic activity. Therefore, there is a necessity of redefining the HF band based on HRV and RSP information [5].

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## Chapter 2

# Materials

### Contents

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2.3	Emotion database validation . . . . .	23

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In this dissertation it has been used physiological recorded data from emotion elicitation. In this section, it is described the database.

## 2.1 Registered signals

A database of 25 volunteers was recorded at the University of Zaragoza during an induced emotion experiment. It contains the simultaneous recording of ECG, RSP, BP, ST and GSR signals (Fig. 2.1). The signals used were: the limb ECG leads (I, II and III) which were sampled at 1 kHz and the respiratory signal,  $r(t)$ , at 125 Hz, with a MP100 BIOPAC device.

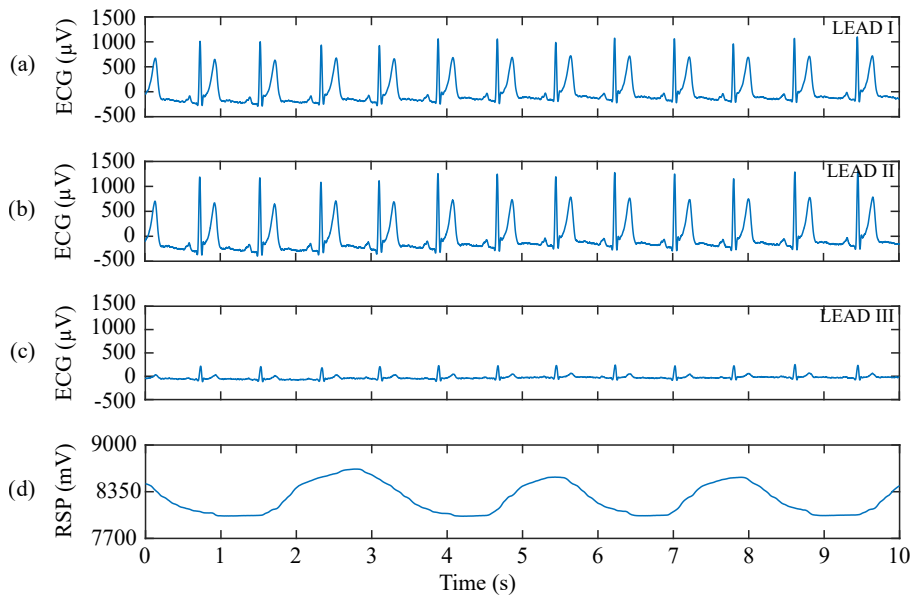


Figure 2.1: Ten seconds of the simultaneous recorded database of (a) electrocardiogram (ECG) Lead I, (b) electrocardiogram (ECG) Lead II, (c) electrocardiogram (ECG) Lead III, and (d) respiration (RSP).

The distribution of the subjects was: four men and five women for the age range 18 to 35 years, four men and four women for the age range 36 to 50 years and four men and four women over 50 years. All subjects were University students or employees with an estimated BMI of 22.9 kg/m<sup>2</sup>.

Previous to the inclusion in the study, the adequacy of each subject was evaluated with a General

Health Questionnaire.

## 2.2 Registered emotions

The experiment consisted on eliciting each subject by four emotions (joy, fear, anger and sadness) using videos (two videos per emotion). All the experiment extended over 2 consecutive days and two sessions were recorded each day. The experiment was split into two days, with the aim to have more than one sample per day for each emotion; therefore the recording is more representative of the emotion and not particularly biased for the specific mood of the day that was recorded. During sessions 1 and 4, the subject was stimulated with videos of joy (J) and fear (F), and during sessions 2 and 3 with videos of anger (A) and sadness (S). Therefore, each of the 25 subjects was elicited with 2 videos of the same emotion, resulting in a total of 50 recordings per emotion. All videos were presented in randomized order.

To ensure that the physiological parameters returned to the baseline condition, each video was preceded and followed by a relaxing video considered as baseline, which were excerpts from nature images with classical music. All sessions were recorded at the same time of the day and the order of the participant was maintained during all sessions to mitigate the circadian variations of HRV parameters. A schema of the organization of the video-induced emotion sessions is represented in Fig. 2.2.

The contents of the videos were: the joy videos were excerpts from laughing monologues; the fear videos were excerpts from scary movies, like Alien and Misery; the sadness videos were an excerpt from the film The Passion of the Christ and a documentary film about history wars; the anger videos were an excerpt of the documentary film of the Columbine High School massacre in 1999 and a

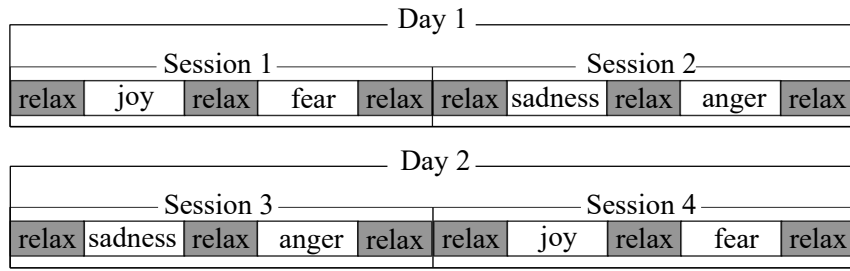


Figure 2.2: Scheme of the organization of the video-induced emotion sessions. Session 1 and 2 were recorded the first day, and session 3 and 4 were recorded the second day. In session 1 and 4, the subject was stimulated with videos of joy and fear, and with videos of anger and sadness in session 2 and 3. All videos were presented in randomized order.

Table 2.1: Specific time segments studied for each video: total video length, time range and video length studied. The unit time are expressed in hh:mm:ss.

	Video	Total video length	Time range studied	Video length studied
Session 1	Relax	00:06:46	[00:01:00-00:06:00]	00:05:00
	Joy	00:10:36	[00:02:00-00:07:00]	00:05:00
	Fear	00:02:47	[00:00:00-00:02:45]	00:02:45
Session 2	Relax	00:06:51	[00:01:00-00:06:00]	00:05:00
	Sadness	00:07:25	[00:01:00-00:06:00]	00:05:00
	Anger	00:09:18	[00:01:00-00:06:00]	00:05:00
Session 3	Relax	00:06:35	[00:01:00-00:06:00]	00:05:00
	Sadness	00:07:07	[00:01:00-00:06:00]	00:05:00
	Anger	00:06:29	[00:01:00-00:06:00]	00:05:00
Session 4	Relax	00:07:36	[00:01:00-00:06:00]	00:05:00
	Joy	00:06:13	[00:01:00-00:06:00]	00:05:00
	Fear	00:09:42	[00:04:00-00:09:00]	00:05:00

documentary about domestic violence; and the relax videos were excerpts from nature images with classical music.

Although each video had a different length, five minutes long were studied for all videos, except one of the videos corresponding to emotion fear, which lasted three minutes. In Table 2.1 are specified the total video length for each emotion, the time range evaluated and the resulting video length studied. The selected time range was defined by means of analyzing all recording one by one and avoiding those segments which contain noise or part of the signal was distorted. Regarding to the analysis of the relax, only the first relax of each session was analyzed as a basal condition during all the session.

Table 2.2: PANAS-X scale with the 60-item scale of different feelings and emotions.

PANAS-X SCALE		
I1: Cheerful	I21: Shaky	I41: Lively
I2: Disgusted	I22: Happy	I42: Ashamed
I3: Attentive	I23: Timid	I43: At ease
I4: Bashful	I24: Alone	I44: Scared
I5: Sluggish	I25: Alert	I45: Drowsy
I6: Daring	I26: Upset	I46: Angry at self
I7: Surprised	I27: Angry	I47: Enthusiastic
I8: Strong	I28: Bold	I48: Downhearted
I9: Scornful	I29: Blue	I49: Sheepish
I10: Relaxed	I30: Shy	I50: Distressed
I11: Irritable	I31: Active	I51: Blameworthy
I12: Delighted	I32: Guilty	I52: Determined
I13: Inspired	I33: Joyful	I53: Frightened
I14: Fearless	I34: Nervous	I54: Astonished
I15: Disgusted with self	I35: Lonely	I55: Interested
I16: Sad	I36: Sleepy	I56: Loathing
I17: Calm	I37: Excited	I57: Confident
I18: Afraid	I38: Hostile	I58: Energetic
I19: Tired	I39: Proud	I59: Concentrating
I20: Amazed	I40: Jittery	I60: Dissatisfied with self

Institutional Ethical Review Boards approved all experimental procedures involving human beings, and subjects gave their written consent. The experiments were conducted following the protocol approved by the Aragón Research Agency under contract: #PM055, 2005.

## 2.3 Emotion database validation

The emotion database has been validated by 16 subjects, different from the ones participating in the database, using the Positive and Negative Affect Schedule - Expanded Form (PANAS-X) [109]. To assess specific emotional states, a 60-item scale of different feelings and emotions was used as shown in Table 2.2. Each subject watched each video, and right after each display the person marked from 1 to 5 each item (I) with the appropriate answer indicating to what extent he or she felt, being 1 = very slightly, 2 = a little, 3 = moderately, 4 = quite a bit and 5 extremely.

Based on the sum of subject responses of specific items of the PANAS-X scale, the following affect

scales can be computed: fear scale ( $S_{fear}$ ) (Eq. 2.1), sadness scale ( $S_{sadness}$ ) (Eq. 2.2), guilt scale ( $S_{guilt}$ ) (Eq. 2.3), hostility scale ( $S_{hostility}$ ) (Eq. 2.4), shyness scale ( $S_{shyness}$ ) (Eq. 2.5), fatigue scale ( $S_{fatigue}$ ) (Eq. 2.6), surprise scale ( $S_{surprise}$ ) (Eq. 2.7), joviality scale ( $S_{joviality}$ ) (Eq. 2.8), self-assurance scale ( $S_{self-assurance}$ ) (Eq. 2.9), attentiveness scale ( $S_{attentiveness}$ ) (Eq. 2.10) and serenity scale ( $S_{serenity}$ ) (Eq. 2.11).

$$S_{fear} = I18 + I44 + I53 + I34 + I40 + I21 \quad (2.1)$$

$$S_{sadness} = I16 + I29 + I48 + I24 + I35 \quad (2.2)$$

$$S_{guilt} = I32 + I42 + I51 + I46 + I15 + I60 \quad (2.3)$$

$$S_{hostility} = I37 + I38 + I11 + I9 + I2 + I56 \quad (2.4)$$

$$S_{shyness} = I30 + I4 + I49 + I23 \quad (2.5)$$

$$S_{fatigue} = I36 + I19 + I5 + I45 \quad (2.6)$$

$$S_{surprise} = I20 + I7 + I54 \quad (2.7)$$

$$S_{joviality} = I22 + I33 + I12 + I1 + I37 + I47 + I41 + I58 \quad (2.8)$$

$$S_{self-assurance} = I39 + I3 + I57 + I28 + I6 + I14 \quad (2.9)$$

$$S_{attentiveness} = I25 + I3 + I59 + I52 \quad (2.10)$$

$$S_{serenity} = I17 + I10 + I43 \quad (2.11)$$

Then, a Basic Negative Emotion (BNE) scale is defined as the average of  $S_{sadness}$ ,  $S_{guilt}$ ,  $S_{hostility}$  and  $S_{fear}$  (Eq. 2.12), and a Basic Positive Emotion (BPE) scale as the average of  $S_{joviality}$ ,  $S_{self-assurance}$  and  $S_{attentiveness}$  (Eq. 2.13). In this work it is studied the BPE, BNE,  $S_{joviality}$ ,  $S_{fear}$ ,  $S_{sadness}$  and  $S_{hostility}$ .

$$BNE = (S_{sadness} + S_{guilt} + S_{hostility} + S_{fear})/4 \quad (2.12)$$

$$BPE = (S_{joviality} + S_{self-assurance} + S_{attentiveness})/3 \quad (2.13)$$

Table 2.3: Mean and standard deviation ( $\mu \pm \sigma$ ) of the PANAS-X scales: Basic Positive Emotion (BPE), Basic Negative Emotion (BNE),  $S_{joyality}$ ,  $S_{fear}$ ,  $S_{sadness}$  and  $S_{hostility}$ .

Scales	Emotions			
	Joy	Fear	Sadness	Anger
BPE	13.1 $\pm$ 4.8	8.1 $\pm$ 1.7	7.4 $\pm$ 1.5	7.8 $\pm$ 2.2
BNE	6.5 $\pm$ 0.8	12.2 $\pm$ 3.9	14.3 $\pm$ 4.4	12.8 $\pm$ 3.8
$S_{joyality}$	22.3 $\pm$ 8.6	9.0 $\pm$ 2.4	8.4 $\pm$ 0.8	8.8 $\pm$ 1.6
$S_{fear}$	6.4 $\pm$ 1.1	19.0 $\pm$ 6.6	14.8 $\pm$ 5.3	13.8 $\pm$ 5.9
$S_{sadness}$	5.2 $\pm$ 0.6	8.7 $\pm$ 4.6	14.8 $\pm$ 5.5	11.7 $\pm$ 4.5
$S_{hostility}$	8.1 $\pm$ 1.7	14.3 $\pm$ 5.3	15.7 $\pm$ 5.4	15.8 $\pm$ 4.8

Statistical analysis was done by T-test or Wilcoxon-test when necessary, depending on normality test results to evaluate differences for all followed paired conditions: relax vs. joy (R-J), relax vs. fear (R-F), relax vs. sadness (R-S), relax vs. anger (R-A), joy vs. fear (J-F), joy vs. sadness (J-S), joy vs. anger (J-A), fear vs. sadness (F-S), fear vs. anger (F-A) and sadness vs. anger (S-A).

The significant statistical level was  $p\text{-value} \leq 0.05$ , that provides a reliable value for statistical discrimination [87]. To analyze the capability of the indices to discriminate emotions, the area under the receiver operating characteristic curve (AUC) was calculated and only those indices with  $AUC \geq 0.70$  were further considered. Finally, sensitivity, specificity and accuracy for each index in 2-class emotion classification were calculated using the leave-one-out cross validation method [72].

In Table 2.3, the mean and standard deviation ( $\mu \pm \sigma$ ) of the scales evaluated for each emotion are shown. It could be observed that the highest mean value of BPE scale corresponds to the emotion with positive valence (joy), while mean value of BNE was higher for emotions with negative valence ( $S_{fear}$ ,  $S_{sadness}$ ,  $S_{anger}$ ). In addition, the affect scale with highest value in joy is  $S_{joyality}$  and the highest value in fear emotion is  $S_{fear}$ . However, there is not a single affect scale for sadness and anger that defines each emotion, resulting in high values for the  $S_{fear}$ ,  $S_{sadness}$  and  $S_{hostility}$ .

Table 2.4 displays the  $p$ -values obtained in the comparison of PANAS-X scales between different emotions. All affect scales showed statistically significant differences between positive valence

### 2.3. EMOTION DATABASE VALIDATION

Table 2.4:  $p$ -values of the PANAS-X scales: Basic Positive Emotion (BPE), Basic Negative Emotion (BNE),  $S_{joyality}$ ,  $S_{fear}$ ,  $S_{sadness}$  and  $S_{hostility}$  for the pair of emotional conditions induced by videos: joy vs. fear (J-F), joy vs. sadness (J-S), joy vs. anger (J-A), fear vs. sadness (F-S), fear vs. anger (F-A) and sadness vs. anger (S-A).

Scales	Emotions analyzed					
	J-F	J-S	J-A	F-S	F-A	S-A
BPE	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	0.011	0.043	n.s.
BNE	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	0.005	n.s.	0.007
$S_{joyality}$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	n.s.	n.s.	n.s.
$S_{fear}$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	n.s.
$S_{sadness}$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	0.002	$p \leq 0.001$
$S_{hostility}$	$p \leq 0.001$	$p \leq 0.001$	$p \leq 0.001$	n.s.	n.s.	n.s.

and negative valence emotions (J-F, J-S, J-A). Affect scales showing largest statistically significant differences between negative valence emotions were:  $S_{fear}$  (F-S, F-A) and  $S_{sadness}$  (F-S, S-A).

According to the analysis of the affect scales derived from the PANAS-X scale, shown in Table 2.3, it could be stated that: joy emotion presents the highest values for the BPE and  $S_{joyality}$ ; all negative emotions presented lower BPE and higher BNE, as expected; fear emotion obtains the highest mean value for the affect scale  $S_{fear}$ ; however, sadness and anger emotions have a high mean value for  $S_{fear}$ ,  $S_{sadness}$  and  $S_{hostility}$ .

As shown in Table 2.4, all PANAS-X affect scales were significantly different between joy and all negative valence emotions (fear, sadness, anger). Statistical differences between negative valence emotions were only found in a subset of PANAS-X affect scales, challenging their discrimination through HRV (Table 2.4).

Additionally, all subjects in this experiment reported an agreement between the theoretical positive valence of joy elicitation and the emotion felt, and fear, sadness and anger were identified as negative emotions. The duration of all videos is considered enough to induce an autonomic response, since those times are longer than the reported delay response to individuals who were exposed to musical stimulus [74].



# Chapter 3

## Linear Analysis Methodology

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## 3.1 Introduction

Developing a tool which identifies human emotions may have a potential value in several fields. First, in the clinical practice, it may have value to reduce the diagnostic time of a psycho-neural illness, and, subsequently, it could directly represent a beneficial economic impact for the health system. Secondly, it can improve on the human-machine interaction since it could provide knowledge regarding the affective state of a user, bringing the machine closer to the human by including emotional content in the communication [23].

Several strategies have been proposed for emotion recognition in the area of non-invasive biosignals as EEG [23,55,58,66,81,90], GSR [83,92], ST, electrodermal activity [54] and ECG [9,48,84,107], among others. This work has been focused on emotion recognition by means of HRV analysis.

In previous studies, recognition of emotional states assessed by means of HRV spectral analysis has been reported [15,24,29,40,68,84,85]. HRV spectral analysis typically considers the power in three bands: a) VLF component in the range between 0 Hz and 0.04 Hz, b) LF component between 0.04 Hz and 0.15 Hz, and c) HF component between 0.15 Hz and 0.40 Hz [94].

It is well known that HRV is influenced by respiration. Heart rate is increased during inspiration and reduced during expiration, phenomenon described as RSA. RSA has been used as an index of cardiac vagal or parasympathetic function, usually measured by the HF component of the HRV [111], while the LF component is affected by both sympathetic and parasympathetic activity. The necessity of redefining the HF band to be centered on the respiratory frequency when  $F_R$  is above 0.40 Hz, has already been highlighted, as well as the misinterpretation of spectral HRV indices when respiratory frequency lies within the LF band [5].

Several studies have already used respiratory information to define the HF band. Most of them define the HF band centered at respiratory frequency and use a fixed bandwidth. Only a few of them use variable HF bandwidth dependent on respiration. In [8], respiratory frequency as well as its rate of variation were used to estimate HF power based on a parametric decomposition of the instantaneous autocorrelation function. In [97], an HF bandwidth dependent on respiration stability was used to analyze HRV in critically ill patients. Recently, spectral coherence between respiration and HRV has been used to define the HF band [28, 57].

Moreover, the relationship between respiration and HRV might be further exploited to add relevant information regarding ANS regulation. Interactions between respiration and HRV have been continuously assessed using time-varying spectral coherence, partial coherence and phase differences during orthostatic test and under selective autonomic blockade [75, 77]. Characterization of these interactions might be crucial in applications where both respiration and HRV are altered, such as during stress [48].

In this work, it is proposed the joint analysis of HRV and respiration to improve human emotion characterization. HF band is defined based on the maximum spectral correlation between HRV and respiration. Both the center and bandwidth of HF band depend on respiration. The maximum spectral correlation itself is proposed as an index to identify emotions. The hypothesis is that this index, characterizing the relationship between respiration and HRV, can add relevant information to HRV analysis to describe human emotions.

First, a simulation study is designed to evaluate the ability of the proposed HF band to quantify RSA. The performance of the proposed HF band is compared to other commonly used HF band definitions. Then, the ability of the proposed indices to characterize human emotions will be tested

on a database of video-induced emotions.

## 3.2 Methods and materials

### 3.2.1 Signal preprocessing

Beat occurrence times were detected from the recorded ECG using a wavelet-based detector [64].

Instantaneous heart rate ( $d_{HR}(t)$ ) was estimated from the beat occurrence times based on the integral pulse frequency modulation (IPFM) model, which takes into account the presence of ectopic beats [65]. A time-varying mean heart rate ( $d_{HRM}(t)$ ) was computed by low pass filtering (cut-off frequency 0.03 Hz)  $d_{HR}(t)$ , and then the HRV was obtained as  $d_{HRV}(t) = d_{HR}(t) - d_{HRM}(t)$ . The modulating signal,  $m(t)$ , which is assumed to carry the ANS information according to the IPFM model [6], was estimated as  $m(t) = (d_{HR}(t) - d_{HRM}(t)) / \overline{d_{HRM}}$  [6], being  $\overline{d_{HRM}}$  the mean of  $d_{HRM}(t)$ . The  $m(t)$  was resampled at 4 Hz.

The respiratory signal,  $r(t)$ , was filtered by a band pass filter from 0.04 Hz to 0.80 Hz, which is assumed to cover the physiological frequency range for  $m(t)$  and  $r(t)$ , and undersampled at 4 Hz.

Spectral HRV indices were estimated from the power spectrum density (PSD) of  $m(t)$  ( $S_m(f)$ ), computed by means of the Welch Periodogram. Then, the power content in the HF band ( $P_{HF}$ ) and in the LF band ( $P_{LF}$ ), the normalized power in the LF band (i.e.  $P_{LFn} = P_{LF} / (P_{LF} + P_{HF})$ ) and the ratio  $R = P_{LF} / P_{HF}$  were computed. The limits of the bands are defined in Section 3.2.2 *Frequency band definition*. The respiratory frequency  $F_R$  was estimated from the location of the largest peak in the PSD obtained from  $r(t)$  ( $S_r(f)$ ).

$$\rho_{(S_m, S_r)}^{ab} = \frac{\int_a^b (S_m(f) - \overline{S_m}(f)) (S_r(f) - \overline{S_r}(f)) df}{\sqrt{\int_a^b (S_m(f) - \overline{S_m}(f))^2 df \int_a^b (S_r(f) - \overline{S_r}(f))^2 df}} \quad (3.1)$$

### 3.2.2 Frequency band definition

#### Shifted and resized HF band based on Spectrum Correlation (SCHF)

The HF band is redefined based on the correlation between  $S_m(f)$  and  $S_r(f)$  as given in Eq. (3.1), where  $a$  and  $b$  are the lower and upper limits of the analyzed frequency range. The maximum value of  $\rho_{(S_m, S_r)}^{ab}$  is searched, following the steps detailed below:

- Step 1: the spectral correlation of  $S_m(f)$  and  $S_r(f)$ ,  $\rho_{(S_m, S_r)}^{ab}$ , is computed within a bandwidth of 0.02 Hz centered at  $F_R$ .
- Step 2: the integration frequency range  $[a, b]$  is symmetrically expanded 0.02 Hz and  $\rho_{(S_m, S_r)}^{ab}$  is recomputed. This step is repeated until the physiological range from 0.1 Hz to  $\overline{d_{HRM}}/2$  is covered, with the following restrictions: (1) the lower limit  $a$  must be above 0.10 Hz, (2) the upper limit  $b$  must be below half the mean heart rate ( $\overline{d_{HRM}}/2$ ) and (3)  $S_r(b)$  must be above 5% of the maximum value of  $S_r(f)$  to avoid including in the correlation estimation frequencies with no respiratory power. In these cases, the restricted limit (lower or upper) is kept fixed and the other limit is increased in 0.01 Hz. The resulting integration frequency ranges are no longer symmetric with respect to  $F_R$ .
- Step 3: the maximum value of  $\rho_{(S_m, S_r)}^{ab}$ , denoted by  $\rho_{max} = \rho_{(S_m, S_r)}^{a_{max} b_{max}}$ , determines the lower and upper limits of the  $[a_{max}, b_{max}]$  redefined HF band (HF<sub>SC</sub>).

Only those recordings showing  $\rho_{max} \geq 0.5$  were considered for further analysis, being this value selected empirically as a trade-off between subject number inclusion and correlation strength. Fig.

3.1 shows a diagram of the SCHF method.

Standard LF band was considered in the range of [0.04, 0.15] Hz, except when the HF band encroached the LF band. In these cases, the upper limit of the LF band was reduced to the lower limit of the HF band, i.e., LF band was  $\in [0.04, a_{max}]$  Hz.

### Classic HF band

The classic HF band described in Task Force [94] was analyzed, i.e. [0.15, 0.40] Hz.

### Shifted HF band centered at $F_R$ with fixed bandwidth

As defined in previous studies [5, 100], the HF band was centered at  $F_R$  and had a fixed bandwidth of 0.11 Hz ( $HF_{F_R}$ ).

In approaches to  $HF_{SC}$  and  $HF_{F_R}$ , which take into account respiratory information, those recordings with  $F_R < 0.1$  Hz are excluded from the analysis due to the overlapping between the LF and HF bands.

### 3.2.3 Simulation study

A simulation study was carried out to validate the proposed  $HF_{SC}$  definition.

Synthetic modulating signals ( $m_s(t)$ ) were generated as the sum of a HF and a LF component, following the steps detailed below:

- Step 1: the HF component was obtained by filtering a respiration signal  $r(t)$  from the emotion database from 0.25 Hz to  $\overline{d_{HRM}}/2$ . This HF component is denoted by  $m_{HF_i}(t)$ ,  $i = 1, \dots, I$ ,

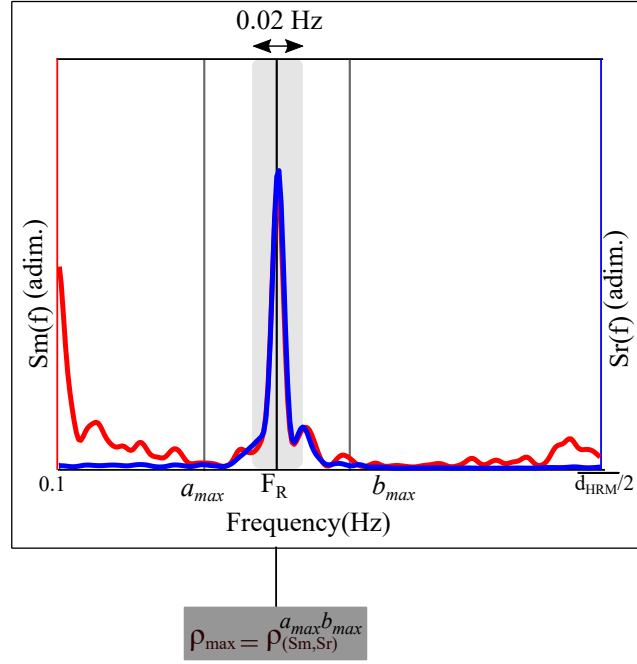


Figure 3.1: Diagram of the SCHF methodology: PSD of  $m(t)$  ( $S_m(f)$ ) and PSD of  $r(t)$  ( $S_r(f)$ ). The correlation between  $S_m(f)$  and  $S_r(f)$  was calculated by expanding symmetrically the  $[a, b]$  range in steps of 0.02 Hz per iteration. The maximum value of the correlation between  $S_m(f)$  and  $S_r(f)$  ( $\rho_{max}$ ) determines the lower and upper limits ( $a_{max}, b_{max}$ ) of the redefined HF band ( $HF_{SC}$ ).

where I is the number of cases with  $F_R > 0.35$  Hz since those are the most challenging for the classic HF band. A total of  $I = 59$  cases were identified.

- Step 2: the LF component was simulated based on a time-varying autoregressive moving average (ARMA) model [76]. The frequency for the ARMA model was obtained as the maximum of the original modulating signal spectrum  $S_m(f)$ , associated with the  $i$ -th subject, in the band from 0.04 Hz to 0.15 Hz and the amplitude was fixed to 0.1. A total of 50 realizations of the LF component were generated for each considered subject, yielding  $m_{LF_i}^k(t)$  with  $k = 1, \dots, 50$ .
- Step 3: the simulated modulating signals were constructed as  $m_{s_i}^k(t) = m_{LF_i}^k(t) + \alpha m_{HF_i}(t)$ , where the  $\alpha$  parameter allows to simulate a set of sympathovagal ratios,  $R$ . The following  $R$  were considered: 0.5, 1, 2, 5, 10, 15, 20 and 30, as shown in Fig. 3.2. This range allows to

cover the physiological  $R$  values computed during pure parasympathetic stimulation, median (interquartile range) of 1.53(0.83|2.11) and pure sympathetic stimulation 19.52(11.80|27.75) in a database of healthy subjects during pharmacological blockade and body position changes [14].

- Step 4: finally, each modulating signal  $m_{s_i}^k(t)$  fed an IPFM model with time-varying threshold which generates the beat occurrence time series [6]. The time-varying threshold is defined as  $1/d_{HRM_i}(t)$ . From the simulated beat occurrence time series, a simulated instantaneous heart rate was obtained  $d_{HR_{s_i}}^k(t)$ . The same processing described in Section 3.2.1 *Signal preprocessing* for real signals was applied to simulated  $d_{HR_{s_i}}^k(t)$ . A diagram of the whole process is shown in Fig. 3.3.

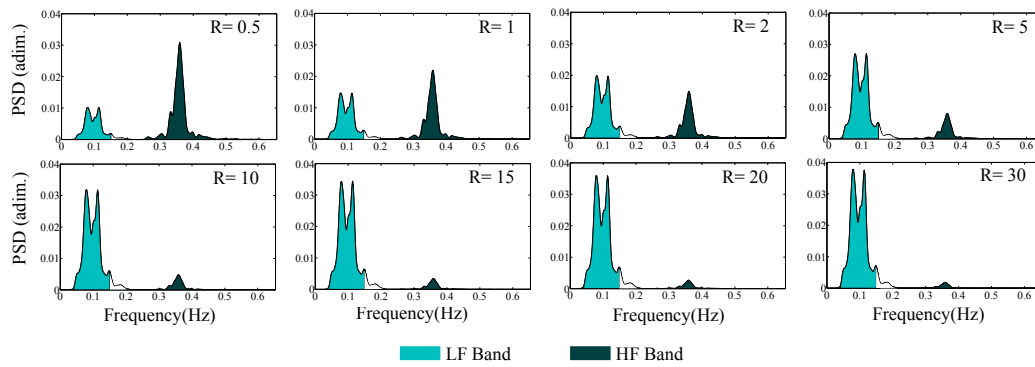


Figure 3.2: PSD of the modulating signal simulated  $d_{HR_{s_i}}^k(t)$  for the physiological sympathovagal ratios: 0.5, 1, 2, 5, 10, 15, 20 and 30.

#### 3.2.4 Performance measurement

The mean relative error (MRE) of HF power was calculated for each ratio Eq. (3.2).

$$MRE(\%) = \text{mean} \left( \frac{P_{HF_i}^k - P_{HF_{r_i}}}{P_{HF_{r_i}}} \right) 100 \quad (3.2)$$



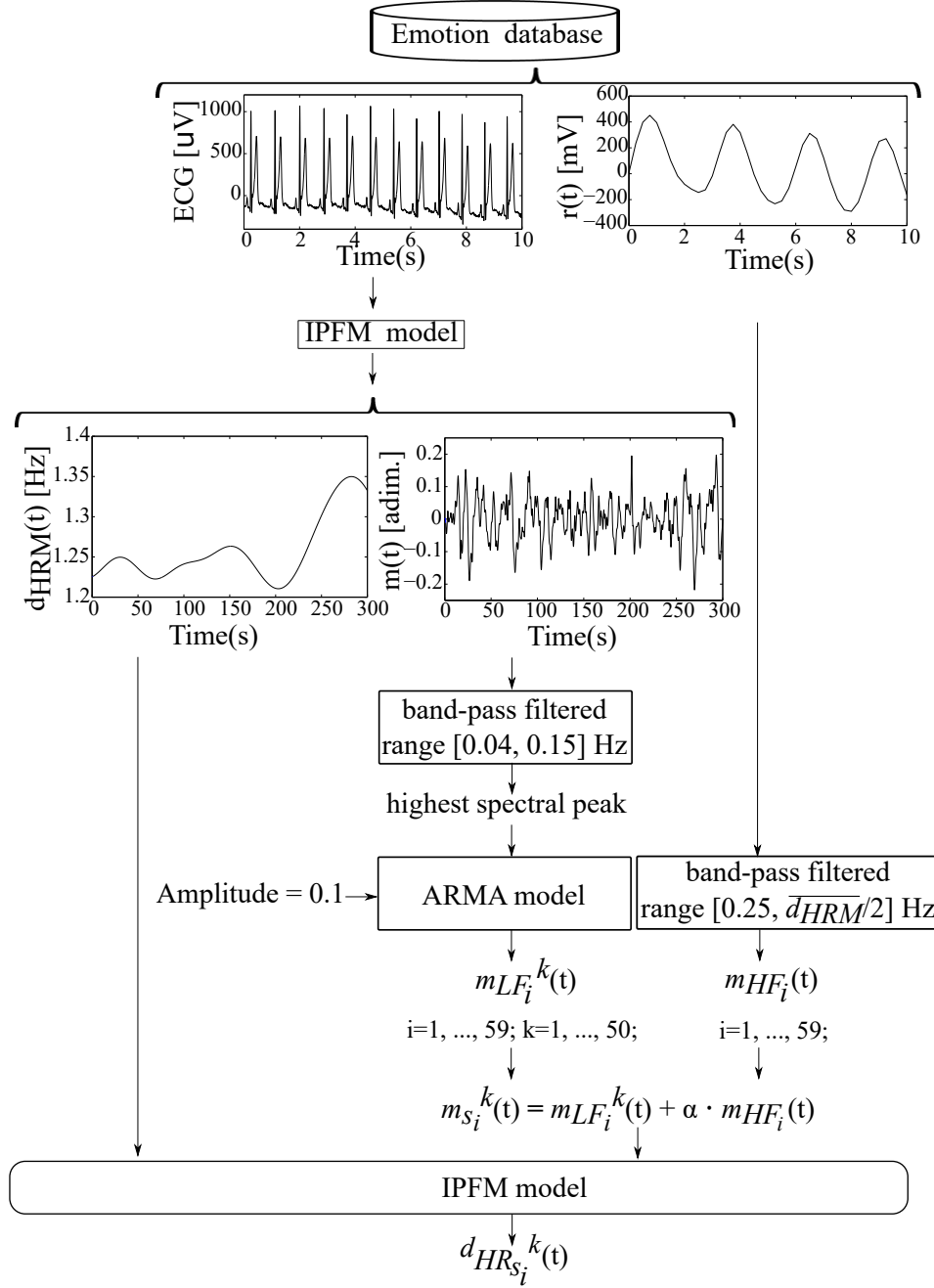


Figure 3.3: Schema of the simulation process for a single recording detailed in the following steps: (1) the HF component of the synthetic  $m(t)$  signals was obtained by filtering the  $r(t)$  of the emotion database from 0.25 Hz to the  $\overline{dHRM}/2$ , resulting in  $m_{HF_i}(t)$ , (2) the LF component was simulated by an ARMA model with a fixed amplitude of 0.1 and a frequency calculated by the maximum of the original  $S_m(f)$ , associated with the  $i$ -th subject, resulting in  $m_{LF_i}^k(t)$ , (3) the simulated modulating signals  $m_{S_i}^k(t)$  were constructed as the sum of the LF and HF components, where  $i$  is the number of the subject analyzed and  $k$  the number of the realization performed and (4) each modulating signal  $m_{S_i}^k(t)$  fed an IPFM model with time-varying threshold ( $1/dHRM_i(t)$ ) which generates the beat occurrence times, and from them the HRV signal  $d_{HR_{S_i}}^k(t)$  is derived.

Where  $P_{HF_i}^k$  was the spectral content in the HF band, calculated as explained in Section 3.2.2 *Frequency band definition*, from the simulated  $d_{HR_{s_i}}^k(t)$  signal (Fig. 3.3) for each simulation and the  $P_{HF_{F_i}}$  was the reference spectral content  $\in [0.25, \overline{d_{HRM}}/2]$  Hz derived from  $d_{HR_{s_i}}^k(t)$  signal.

The proposed SCHF methodology was compared with the other HF band definitions. Therefore,  $P_{HF_i}^k$  and  $P_{HF_{F_i}}$  for the MRE calculation were computed according to the bandwidth definitions detailed in Section 3.2.2 *Frequency band definition*: (1)  $HF_{SC}$ , (2) HF and (3)  $HF_{F_R}$ .

#### 3.2.5 Statistical analysis

Prior to the statistical analysis, normality distribution of all indices was evaluated by Lillie test.

Statistical analysis was done by T-test or Wilcoxon-test when necessary, depending on normality test results to evaluate differences for all followed paired conditions: relax vs. joy (R-J), relax vs. fear (R-F), relax vs. sadness (R-S), relax vs. anger (R-A), joy vs. fear (J-F), joy vs. sadness (J-S), joy vs. anger (J-A), fear vs. sadness (F-S), fear vs. anger (F-A) and sadness vs. anger (S-A).

Firstly, the affect scales BPE, BNE, joviality, fear, sadness and hostility have been statistically evaluated for database validation. Subsequently, the following HRV indices have been analyzed:

- Indices derived from the  $HF_{SC}$  band:  $P_{HF_{SC}}$ ,  $P_{LF_{n_{SC}}}$ ,  $R_{SC}$ ,  $\Delta HF$ ,  $a_{max}$  and  $b_{max}$  and the novel index proposed in this work  $\rho_{max}$ . The respiratory frequency of the recordings which accomplishes all the restrictions imposed in Section 3.2.2 *Frequency band definition*, denoted by  $F_{R_{SC}}$  was also considered.
- Indices derived from the classic HF band:  $P_{HF}$ ,  $P_{LF_n}$  and  $R$ . The respiratory frequency,  $F_R$ , of all recordings was also studied.

- Indices derived from the  $HF_{F_R}$  band:  $P_{HF_{F_R}}$ ,  $P_{LFn_{F_R}}$  and  $R_{F_R}$ . The respiratory frequency of the recordings which accomplishes the unique restriction of  $F_R \geq 0.10$  Hz, denoted by  $F_{R_{F_R}}$  was also considered.

The significant statistical level was  $p\text{-value} \leq 0.05$ , that provides a reliable value for statistical discrimination [87]. To analyze the capability of the indices to discriminate emotions, the area under the receiver operating characteristic curve (AUC) was calculated and only those indices with  $AUC \geq 0.70$  were further considered. Finally, sensitivity, specificity and accuracy for each index in 2-class emotion classification were calculated using the leave-one-out cross validation method [72].

### 3.3 Results

#### 3.3.1 Evaluation of the methods for synthetic data

Fig. 3.4 presents the mean and standard deviation ( $\mu \pm \sigma$ ) of the relative errors in PHF estimation obtained from  $HF_{SC}$ , HF and  $HF_{F_R}$  for several physiological sympathovagal ratios,  $R$  i.e. 0.5, 1, 2, 5, 10, 15, 20 and 30. The standard HF bandwidth presents relative error values strongly dependent on the ratio, while the  $HF_{F_R}$  and the  $HF_{SC}$  bandwidth presents lower relative error values regardless of the ratio values. Furthermore, the  $HF_{SC}$  bandwidth presents lower relative errors than the  $HF_{F_R}$  one.

#### 3.3.2 Evaluation of the methods for real data

All indices derived from the  $HF_{SC}$ , HF and  $HF_{F_R}$  bands have been evaluated and compared between each pair of emotions. In Table 3.1, the results obtained by the studied indices in terms of median and interquartile ranges as first (Q1) and third (Q3) quartile, median (Q1|Q3), for all emotional

### 3.3. RESULTS

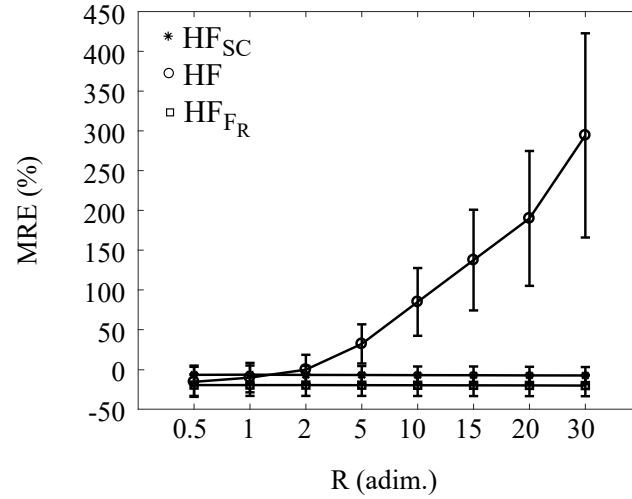


Figure 3.4: Mean and standard deviation ( $\mu \pm \sigma$ ) of the mean relative errors (MRE) obtained by Eq. (3.2) for HF<sub>SC</sub>, HF and HF<sub>FR</sub> methods for eight physiological sympathovagal ratios studied: 0.5, 1, 2, 5, 10, 15, 20 and 30.

conditions (i.e. relax, joy, fear, sadness and anger) are shown. And Table 3.2 displays the  $p$ -values

obtained from the statistical analysis and AUC values for the comparison of all pair of emotions.

Table 3.1: Median (Q1|Q3) values of the parameters studied for relax, joy, fear, sadness and anger.

	Relax	Joy	Fear	Sadness	Anger
$P_{HF}$ ( $10^{-4}$ ) (adim.)	3.60(1.52 8.01)	3.30(1.54 6.62)	3.62(1.67 5.91)	2.56(1.61 5.49)	2.76(1.34 4.60)
$P_{LFn}$ (%)	73.93(56.44 83.34)	81.74(75.52 88.30)	70.21(56.89 80.85)	75.86(62.19 80.81)	78.61(69.13 83.75)
$R$ (adim.)	2.84(1.30 5.00)	4.48(3.09 7.55)	2.37(1.32 4.22)	3.14(1.64 4.21)	3.67(2.24 5.16)
$d_{HRM}$ (bpm)	0.61(0.57 0.69)	0.63(0.57 0.69)	0.64(0.58 0.69)	0.64(0.58 0.72)	0.64(0.60 0.69)
$F_R$ (Hz)	0.29(0.24 0.35)	0.18(0.08 0.33)	0.31(0.27 0.35)	0.31(0.28 0.36)	0.30(0.25 0.35)
$P_{HF_{FR}}$ ( $10^{-4}$ ) (adim.)	1.93(0.73 4.95)	2.50(0.44 9.68)	1.91(0.86 4.08)	1.44(0.88 2.54)	1.58(0.78 2.71)
$P_{LFn_{FR}}$ (%)	78.94(61.49 90.24)	83.42(68.42 93.55)	73.64(61.92 89.24)	82.57(63.97 90.51)	85.96(76.35 91.01)
$R_{FR}$ (adim.)	3.75(1.60 9.27)	5.03(2.19 14.50)	2.79(1.63 8.29)	4.75(1.80 9.61)	6.12(3.23 10.12)
$F_{R_{FR}}$ (Hz)	0.30(0.27 0.35)	0.32(0.15 0.35)	0.32(0.28 0.35)	0.32(0.28 0.36)	0.31(0.27 0.35)
$P_{HF_{SC}}$ ( $10^{-4}$ ) (adim.)	2.42(0.95 6.21)	2.25(0.46 4.21)	2.61(0.97 4.36)	1.65(0.11 2.95)	1.86(0.94 2.64)
$P_{LFn_{SC}}$ (%)	76.32(58.39 86.03)	82.45(77.40 90.69)	71.70(59.39 88.58)	80.60(61.57 88.10)	84.29(73.72 90.41)
$R_{SC}$ (adim.)	3.22(1.40 6.16)	4.70(3.60 13.46)	2.53(1.46 7.76)	4.17(1.62 7.41)	5.37(2.81 9.43)
$\Delta HF$ (Hz)	0.16(0.12 0.20)	0.18(0.14 0.23)	0.14(0.12 0.18)	0.16(0.12 0.18)	0.14(0.12 0.18)
$a_{max}$ (Hz)	0.21(0.18 0.27)	0.25(0.22 0.27)	0.24(0.20 0.26)	0.24(0.20 0.27)	0.24(0.21 0.27)
$b_{max}$ (Hz)	0.40(0.35 0.42)	0.41(0.39 0.51)	0.40(0.36 0.44)	0.40(0.36 0.45)	0.40(0.36 0.43)
$\rho_{max}$ (adim.)	0.95(0.88 0.98)	0.89(0.76 0.92)	0.93(0.89 0.97)	0.96(0.90 0.98)	0.93(0.89 0.98)
$F_{R_{SC}}$ (Hz)	0.30(0.27 0.35)	0.33(0.31 0.38)	0.32(0.29 0.35)	0.32(0.28 0.36)	0.32(0.29 0.36)

Only those parameters that revealed statistical differences to discriminate between pairs of emotions

are shown in Fig. 3.5 by means of boxplots in terms of median and interquartile ranges as first (Q1)

and third (Q3) quartile, median (Q1|Q3) of: (a)  $P_{LFn_{SC}}$ , (b)  $P_{LFn}$ , (c)  $P_{LFn_{FR}}$ , (d)  $R_{SC}$ , (e)  $R$ , (f)  $R_{FR}$

and (g)  $\rho_{max}$  for the emotions studied.

The spectral indices  $P_{LFn}$  and  $R$  revealed statistically significant differences between R-J, J-F and J-

Table 3.2:  $p$ -values and AUC indices of the parameters studied for the emotional conditions: relax vs. joy (R-J), relax vs. fear (R-F), relax vs. sadness (R-S), relax vs. anger (R-A), joy vs. fear (J-F), joy vs. sadness (J-S), joy vs. anger (J-A), fear vs. sadness (F-S), fear vs. anger (F-A) and sadness vs. anger (S-A).

		R-J	R-F	R-S	R-A	J-F	J-S	J-A	F-S	F-A	S-A
Number of comparisons		35	43	30	34	34	21	26	25	31	22
$P_{HF}$	$p$ -value	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.52	0.48	0.52	0.52	0.49	0.56	0.51	0.50	0.56	0.55
$P_{LFn}$	$p$ -value	<b><math>\leq 0.001</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.01</math></b>	$\leq 0.05$	n.s.	$\leq 0.05$	n.s.
	AUC index	<b>0.70</b>	0.50	0.48	0.53	<b>0.72</b>	<b>0.76</b>	0.59	0.57	0.62	0.54
R	$p$ -value	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.01</math></b>	$\leq 0.05$	n.s.	$\leq 0.05$	n.s.
	AUC index	<b>0.70</b>	0.50	0.52	0.53	<b>0.72</b>	<b>0.76</b>	0.59	0.57	0.62	0.54
$\overline{d_{HRM}}$	$p$ -value	$\leq 0.05$	$\leq 0.01$	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.55	0.56	0.54	0.51	0.50	0.46	0.51	0.53	0.52	0.51
$F_R$	$p$ -value	$\leq 0.05$	$\leq 0.05$	n.s.	$\leq 0.05$	$\leq 0.01$	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.
	AUC index	0.65	0.58	0.56	0.54	0.68	0.67	0.60	0.51	0.58	0.55
Number of comparisons		17	38	26	28	17	12	16	21	25	19
$P_{HF_{FR}}$	$p$ -value	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.61	0.48	0.52	0.52	0.58	0.38	0.43	0.45	0.47	0.52
$P_{LF_{FR}}$	$p$ -value	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.01</math></b>	$\leq 0.05$	$\leq 0.05$	n.s.	n.s.	n.s.
	AUC index	<b>0.72</b>	0.50	0.53	0.58	<b>0.75</b>	0.67	0.60	0.54	0.57	0.56
$R_{FR}$	$p$ -value	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.01</math></b>	$\leq 0.05$	$\leq 0.05$	n.s.	n.s.	n.s.
	AUC index	<b>0.72</b>	0.50	0.47	0.58	<b>0.75</b>	0.67	0.60	0.54	0.57	0.56
$F_{R_{FR}}$	$p$ -value	$\leq 0.05$	$\leq 0.05$	n.s.	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.63	0.58	0.54	0.55	0.51	0.62	0.60	0.52	0.54	0.49
Number of comparisons		12	33	22	26	12	9	11	17	21	17
$P_{HF_{SC}}$	$p$ -value	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.59	0.49	0.53	0.54	0.62	0.48	0.60	0.5	0.54	0.50
$P_{LF_{SC}}$	$p$ -value	<b><math>\leq 0.05</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	<b>0.72</b>	0.49	0.53	0.59	<b>0.76</b>	0.63	0.49	0.56	0.61	0.56
$R_{SC}$	$p$ -value	<b><math>\leq 0.05</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	<b>0.72</b>	0.51	0.47	0.59	<b>0.76</b>	0.63	0.49	0.44	0.61	0.56
$\Delta HF$	$p$ -value	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.62	0.62	0.57	0.54	0.62	0.67	0.69	0.5	0.52	0.53
$a_{max}$	$p$ -value	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.57	0.55	0.56	0.58	0.55	0.49	0.53	0.55	0.50	0.51
$b_{max}$	$p$ -value	n.s.	n.s.	n.s.	n.s.	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.65	0.52	0.51	0.52	0.63	0.62	0.64	0.49	0.50	0.50
$\rho_{max}$	$p$ -value	<b><math>\leq 0.01</math></b>	n.s.	n.s.	n.s.	<b><math>\leq 0.05</math></b>	<b><math>\leq 0.05</math></b>	<b><math>\leq 0.01</math></b>	<b><math>\leq 0.05</math></b>	n.s.	n.s.
	AUC index	<b>0.90</b>	0.54	0.63	0.55	<b>0.77</b>	<b>0.84</b>	<b>0.82</b>	<b>0.70</b>	0.47	0.55
$F_{R_{SC}}$	$p$ -value	n.s.	n.s.	n.s.	$\leq 0.05$	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
	AUC index	0.65	0.54	0.53	0.56	0.55	0.59	0.62	0.51	0.54	0.49

n.s. Stands for non-significant.

Note that parameters with  $p \leq 0.05$ , AUC index  $\geq 0.70$ , sensitivity, specificity, accuracy values  $\geq 70\%$  are remarked in bold type.

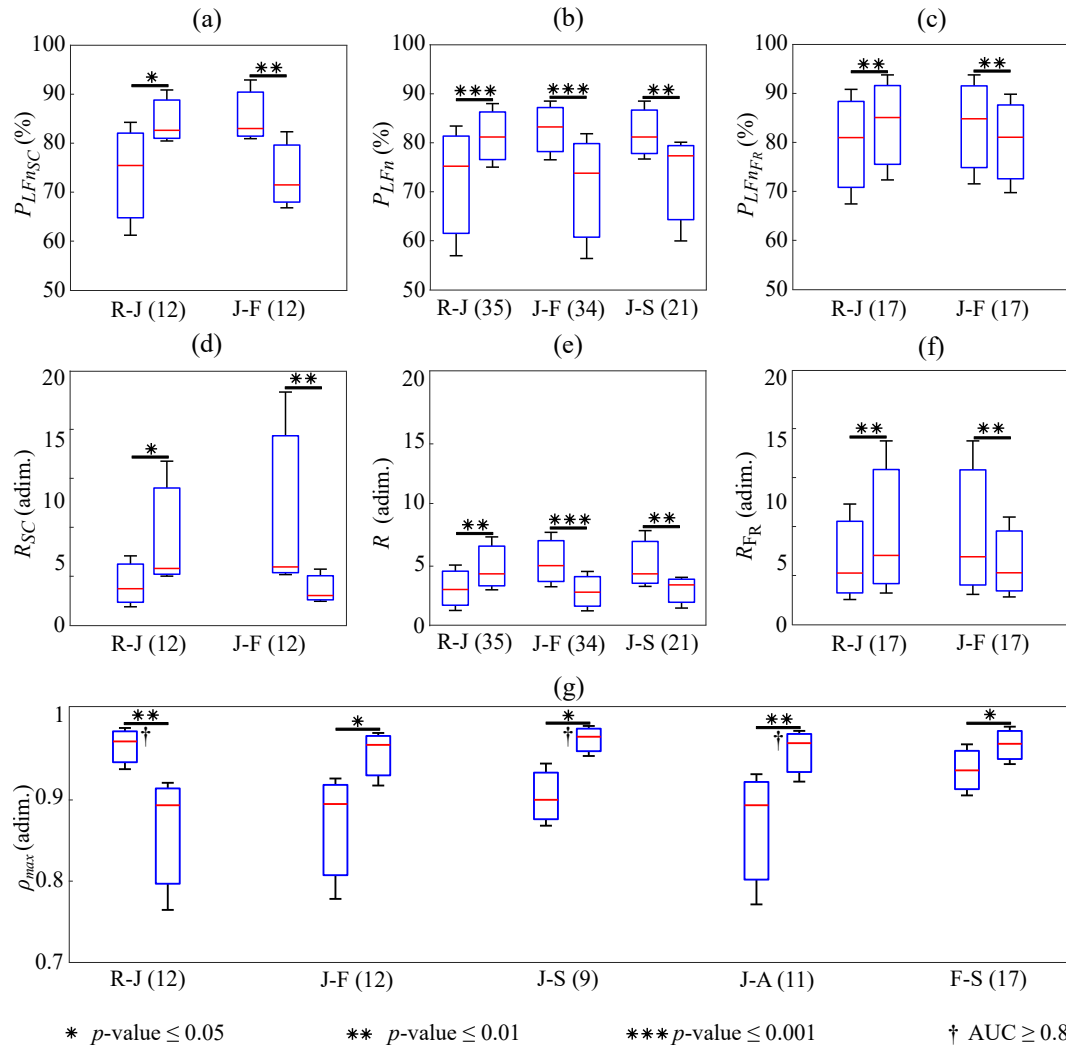


Figure 3.5: Boxplots of the median (Q1|Q3) values of only those parameters which present statistical differences between the emotional conditions induced by videos: (a)  $P_{LFn_{SC}}$ , (b)  $P_{LFn}$ , (c)  $P_{LFn_{FR}}$ , (d)  $R_{SC}$ , (e)  $R$ , (f)  $R_{FR}$  and (g)  $\rho_{max}$ . The nomenclature used for each pair of emotions is: relax vs. joy (R-J), joy vs. fear (J-F), joy vs. sadness (J-S), joy vs. anger (J-A) and fear vs. sadness (F-S). The statistical differences between the pair of emotions are indicated by \* for  $p$ -value  $\leq 0.05$ , \*\* for  $p$ -value  $\leq 0.01$ , \*\*\* for  $p$ -value  $\leq 0.001$  and † for AUC  $\geq 0.80$ . It can be noted that those indices which are not marked by a † have an AUC  $\geq 0.70$ . Together to the label of the pair of studied emotions in parentheses, it is the number of comparisons.

S. However,  $P_{LFn_{FR}}$ ,  $P_{LFn_{SC}}$ ,  $R_{FR}$  and  $R_{SC}$  only show statistically significant differences between R-J and J-F. Additionally, the novel  $\rho_{max}$  provided statistically significant differences between R-J, J-F, J-S, J-A and F-S. Since  $\rho_{max}$  obtained AUC  $\geq 0.8$ , its discrimination capability was further analyzed, calculating sensitivity, specificity and accuracy using cross validation (Table 3.3).

Therefore, among all the emotions compared, neutral state vs. positive valence, positive valence vs.

Table 3.3: Sensitivity, specificity and accuracy calculated using cross validation for the parameter  $\rho_{max}$  with  $AUC \geq 0.8$ : relax vs. joy (R-J), joy vs. sadness (J-S) and joy vs. anger (J-A).

	R-J	J-S	J-A
Sensitivity (%)	66.7	88.9	99.9
Specificity (%)	91.7	66.7	63.6
Accuracy (%)	79.2	77.8	77.3

all negative valences and F-S were significantly different. No statistical differences were found in the comparison between neutral state vs. negative valences and anger vs. negative valences.

Fig. 3.6 displays two examples where the SCHF method is especially useful:

- (a) The  $F_R$  is below 0.15 Hz and therefore the  $HF_{SC}$  band encroaches the classic LF band. In this particular case the  $HF_{SC}$  band limits are:  $a_{max} = 0.10$  Hz and  $b_{max} = 0.29$  Hz. The  $LF_{SC}$  band is redefined from 0.04 Hz to 0.10 Hz.
- (b)  $F_R$  is 0.40 Hz and the  $HF_{SC}$  upper band limit should be shifted to the right to consider all the RSA information. In this particular case, the  $HF_{SC}$  band limits are:  $a_{max} = 0.34$  Hz and  $b_{max} = 0.46$  Hz.

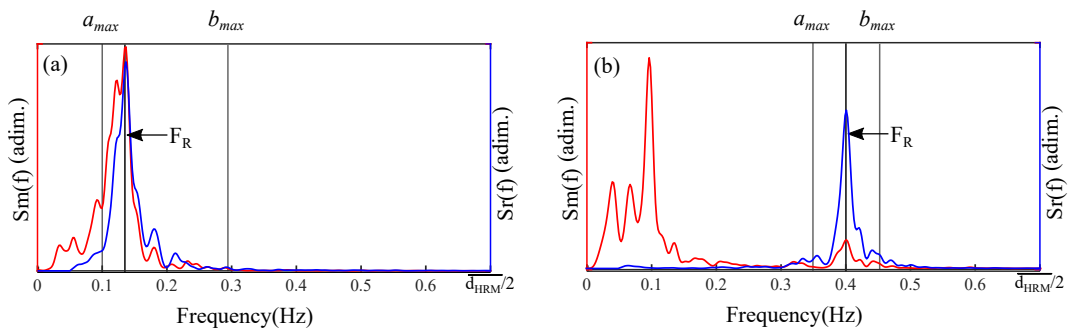


Figure 3.6: Correlation between  $S_m(f)$  and  $S_r(f)$  in two particular cases: (a)  $F_R$  is below 0.15 Hz and (b)  $F_R$  is 0.40 Hz.

### 3.4 Discussion

According to the simulation results, the SCHF method presented the lowest relative error values for HF content estimation independently of the considered low-to-high frequency ratio,  $R$ , values (Fig. 3.4). In this way, the choice of adaptive HF frequency limits may avoid physiological misinterpretations of HF power content, because frequency limits depend strongly on age and physiological conditions [43].

The statistical analysis presented in Table 3.2 and in Fig. 3.5 revealed statistically significant differences between: (1) neutral state vs. positive valence by means of  $P_{LFn}$ ,  $R$ ,  $P_{LFnF_R}$ ,  $R_{F_R}$ ,  $P_{LFnSC}$ ,  $R_{SC}$  and  $\rho_{max}$ , (2) joy vs. fear by means of  $P_{LFn}$ ,  $R$ ,  $P_{LFnF_R}$ ,  $R_{F_R}$ ,  $P_{LFnSC}$ ,  $R_{SC}$  and  $\rho_{max}$ , (3) joy vs. sadness by means of  $P_{LFn}$ ,  $R$  and  $\rho_{max}$ , (4) joy vs. anger by means of  $\rho_{max}$  and (5) fear vs. sadness by means of  $\rho_{max}$ .

The SCHF methodology proposed in this study differentiated R-J, J-F, J-S, J-A and F-S by means of  $\rho_{max}$ . No statistical differences were found for neutral state vs. negative valences and anger vs. negative valences.

Classic frequency indices  $P_{LFn}$  and  $R$  were able to discriminate between R-J, J-F and J-S. It can be noted that emotions J-A and F-S were only distinguished by parameter  $\rho_{max}$  derived from the new method SCHF, which offered additional statistical significant information based on the relationship between HRV and respiration.

Regarding respiratory information, neither  $F_R$ , nor  $F_{R_{F_R}}$ , nor  $F_{R_{SC}}$  showed statistical significant differences between all pairs of emotions studied. Hernando et al. [48] did not find significant differences in respiratory frequency between relax and stress. The  $F_R$  index, computed from all recordings,



showed a median value around 0.30 Hz and with a first quartile above 0.15 Hz for relax, fear, sadness and anger. Therefore, in all these cases, the redefined HF band  $HF_{SC}$  does not encroach the classic LF band. However, in the case of joy,  $F_R$  presented the lowest median value of 0.18 Hz with a first quartile of 0.08 Hz. For this reason and during joy elicitation, the  $HF_{SC}$  could encroach the classic LF band. Therefore, this highlights the need to redefine the HF band, especially in joy condition.

For this reason, all cases presenting a  $F_R$  inside the classic LF band, a redefinition of the HF classic band could improve the measurement of the HF band, as shown in Fig. 3.6 (a). A similar situation occurs in Fig. 3.6 (b) when  $F_R$  is near to or above the classic upper limit of the HF band (0.40 Hz), where the classic range [0.15, 0.40] Hz could miss the RSA information. With a redefinition of the HF band in these cases, a more refined description of the physiological information could be extracted from the signals. However, only recordings which accomplished the restrictions of the SCHF method could be analyzed. This implies to discard an amount of signals from the analysis, and subsequently the number of analyzed subjects in each case is reduced. It can be noted that the percentage of subjects excluded is different for each of the comparisons, with a minimum of 22.7% for the comparison S-A and a maximum of 65.7% for the comparison R-J.

Classic  $\Delta HF$  [0.15, 0.40] Hz has a bandwidth of 0.25 Hz. Analyzing the results obtained by the SCHF method, the  $\Delta HF$  presented a median bandwidth value of 0.16 Hz for relax, 0.18 Hz for joy, 0.14 Hz for fear and anger and 0.16 Hz for sadness. The lower and upper limit of the  $HF_{SC}$ , i.e.,  $a_{max}$  and  $b_{max}$ , showed similar values within the different emotions, although both are subject dependent. The SCHF reveals a slight improvement in the reliability of sympathovagal balance estimation capable of discriminating neutral (relax) vs. positive (joy) valence, positive vs. negative (fear, sadness and anger) valences and negative (fear) vs. negative (sadness) valence. In accordance

with our results, Goren Y. et al. [43] concluded the importance of redefining the boundary of the HF band for a correct evaluation of physiological changes of the ANS.

$P_{HF_{SC}}$  was found higher for fear and relax than for joy, sadness and anger. These results are different from the ones in previous studies [74] where PHF values were higher during listening to unpleasant than pleasant music. This difference may be due to the different stimuli utilized in [68] and [74] where music was used as opposed to videos as in the present study.

Mikuckas A. et al. [68] found that LF component and LF/HF ratio increased during exciting and sedative music, but decreased during silence. Moreover, Rantanen A. et al. [85] evidenced that negative valence elicitation, induced by unpleasant pictures, produced a higher LF/HF ratio than neutral and pleasant pictures in a female cohort. Valenza G. et al. [105] investigated the synchronization between breathing patterns and heart rate during emotional visual elicitation by means of a set of neutral vs. increasing level of arousal images. In that study, it was found that the LF/HF ratio presented statistical differences between neutral and arousal sessions with higher LF/HF ratio values while arousal sessions, in which sympathetic activity should be dominant. In this study, an increase in the  $P_{LFn_{SC}}$  and  $R_{SC}$  indices during joy (Fig. 3.5 (a-f)) was observed. Thus, joy could be associated with a sympathetic predominance. Additionally,  $P_{LFn_{SC}}$  and  $R_{SC}$  presented statistical differences discriminating neutral sessions vs. positive valence and J-F.

Besides the aforementioned elicitation types and emotions, population characteristics such as age could influence the results [43]. Thus, interpretation of the results should be addressed within this framework.

## Chapter 4

# Non-Linear Analysis Methodology

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## 4.1 Introduction

Interest in emotion recognition has burgeoned in recent years aiming to provide a useful tool in the field of emotion regulation. In that sense, a subject's emotional response is mediated by individual influences depending on which emotions the subject has and how he/she experiences and expresses them [45]. Many clinical features of depression, stress, anxiety and mood disorders may be construed as maladaptive attempts to regulate unwanted emotions [18]. A system for emotion recognition could help people to manage their own emotions, providing a tool to record their feelings and consequently, focusing their attention on modulating their emotional responses.

A complex mixture of cognitive, affective, behavioral, and physiological factors contributes to individual differences in health and disease. All these factors produce wide variation in outcomes of heart rate variability (HRV), blood pressure and autonomic balance which have important implications for both physical and mental health [95].

Human emotion recognition has been studied by means of HRV spectral analysis [15, 24, 29, 40, 68, 84, 85, 101]. Generally, the power spectra of HRV is divided into two main components: LF component [0.04, 0.15] Hz, and HF component [0.15, 0.4] Hz [94]. This spectral HRV analysis can describe the regulatory mechanisms of the heart rate which are influenced by neural inputs from sympathetic and parasympathetic divisions of the ANS, RSP, thermoregulation and hormonal systems, among others [94]. The sympathetic modulation of cardiac activity is encompassed in LF band and the parasympathetic activity affects both LF and HF band power [94]. Furthermore, respiration has a dominant influence in the HF component of the HRV, since heart rate is increased during inspiration and reduced during expiration, phenomenon described as RSA [111].

As before mentioned, HRV analysis based on linear methods (such spectral analysis) is a usual strategy for ANS analysis, although non-linear HRV analysis has also been demonstrated as a useful complementary tool [50]. Traditional time and frequency domain measures of HRV assess the amplitude of variations between subsequent intervals and the amplitude distributions in the power spectra, respectively. However, none of them provide information about the complex communication involved in the control of the cardiovascular system that generates the HRV [78]. Non-linear techniques such as the Dominant Lyapunov Exponents, the Detrended Fluctuation Analysis, the Approximate Entropy, the Sample Entropy, the Fuzzy Measure Entropy, the Cross Sample Entropy, the Cross Fuzzy Measure Entropy, the Permutation Entropy, Permutation Min-Entropy, the Pointwise Correlation Dimension, the Lagged Poincaré Plot or the Quadratic Coupling have been used to detect emotional stimuli and all of them have shown better results than linear techniques [13,31,44,102–106,110,112]. Some of these techniques have also been used to study non-linear relationships between HRV and respiration signals [56,104–106,112]. Table 4.1 reports a summary of different non-linear techniques applied to RR series during diverse emotional states.

This complementary information can be assessed by non-linear methods such as the AMIF and the CMIF, which have been demonstrated to be independent of signal amplitudes and able to describe the predictability and regularity of the signals [49,50]. Both functions, the AMIF and the CMIF, have been proposed as predictors of cardiac mortality [50]. The AMIF has been studied as an indicator of the increased cardiac mortality in depressed patients [13] and in multiple organ dysfunction syndrome patients [49], and the CMIF has been applied to electroencephalographic signals for stress assessment [1].

In the present work, both the non-linear techniques, the AMIF and the CMIF are proposed for

Table 4.1: Bibliographic Summary of non-linear techniques applied to HRV series in different emotional states.

Ref.	Technique	Emotional state	Results
[102]	DLEs ApEn	Neutral and arousal elicitation	Mean ApEn decrease and DLEs became negative during arousal elicitation.
[13]	AMIF	Depression	Increased total area under the AMIF curve are associated with major depression.
[112]	SEn FMEn CSEn CFMEn	Depression	Increased CSEn and CFMEn are associated with depression severity.
[110]	PE PME	Neutral, happiness, fear, sadness, anger, and disgust	Increased PE and PME during happiness, sadness, anger, and disgust. PME is more sensitive than PE for discriminating non-neutral from neutral emotional states.
[31]	DLEs ApEn SEn PD2 DFA	Anxiety	Decreased DLEs, ApEn, SEn, PD2 and increased $\alpha 1$ during anxiety state.
[44]	LPP	Peacefulness, happiness, fear, sadness	Maximum changes in LLP measures during happiness, and minimum changes during fear.

The nomenclature used is:

Dominant Lyapunov Exponents (DLEs), Approximate Entropy (ApEn), Sample Entropy (SEn), Fuzzy Measure Entropy (FMEn), Cross Sample Entropy (CSEn), Cross Fuzzy Measure Entropy (CFMEn), Permutation Entropy (PE), Permutation Min-Entropy (PME), Pointwise Correlation Dimension (PD2), Detrended Fluctuation Analysis (DFA), Lagged Poincaré Plot (LLP).

human emotion recognition. The AMIF technique is applied to HRV signals to study complex communication within the ANS, while the CMIF technique is considered to quantify the complex coupling between HRV and respiratory signals. Both algorithms are, in this work, adapted to short-term time series modifying the number of histogram bins involved in the methodology. Traditional RR band filtering is considered (i.e. LF and HF band), and also a redefined HF band,  $HF_{SC}$ , centered at the  $F_R$  and whose width is determined based on the SCHF method, are investigated [101]. The aim of including the  $HF_{SC}$  band is the analysis of RSA influences on HRV, mainly when  $F_R$  is above 0.40 Hz or  $F_R$  lies within the LF band [5, 101]. The ability of the parameters derived from the AMIF and the CMIF to discriminate elicited states is evaluated on a database of video-induced emotion

elicitation, described in [101].

In [101], the discrimination between different emotional states was addressed using frequency domain HRV indices (linear features). However, it was not possible to discriminate between relax and all negative valences, as well as between fear and anger, and sadness and anger. Here, we aim to study the discrimination capability of the non-linear AMIF and CMIF techniques of emotions complementing the linear-feature information. We propose the use of these non-linear techniques for human emotion recognition hypothesizing that ANS response to different emotions will impinge differential regularity patterns in HRV and will change the complex interaction between respiration and heart rate variability.

## 4.2 Methods and materials

### 4.2.1 Signal preprocessing

The RR interval was defined as the time between two consecutive R wave peaks, detected from the ECG lead with the best signal-to-noise ratio using a wavelet-based detector [64]. The presence of ectopic beats and misdetections was detected and corrected [65]. Evenly sampled RR time series,  $RR(t)$ , were obtained by linear interpolation at 4 Hz.

Then, the  $RR(t)$  was filtered in: (1) the LF band of [0.04, 0.15] Hz ( $RR_{LF}(t)$ ), (2) the HF band of [0.15, 0.40] Hz ( $RR_{HF}(t)$ ) and (3) the  $HF_{SC}$  band [101] based on the SCHF method, ( $RR_{SC}(t)$ ). In the SCHF method, the HF band was redefined to be centered at the  $F_R$  and its limits were calculated by means of the cross-correlation function between the power spectrum of HRV and respiration, being subject-dependent. The maximum value of correlation determined the lower ( $a_{max}$ ) and upper limit



$(b_{max})$  of the  $HF_{SC}$  band.

The respiratory signal ( $r(t)$ ) was filtered by a band pass filter from 0.04 Hz to 0.8 Hz, and downsampled at 4 Hz.

Then, a transformation of all time series was carried out by ranking data in order to have the best statistics in the entropy estimation and robustness against noise [82].

### 4.2.2 Auto-Mutual Information Function

The AMIF is a non-linear equivalent of the auto-correlation function, based on the Shannon entropy. The Shannon entropy of a time series  $x(t)$  is calculated by the discrete probability distribution  $p(x_i(t))$  of  $x(t)$  leading  $H_{x(t)}$  as shown in Eq. 4.1 [50].

$$H_{x(t)} = - \sum_{i=1}^I p(x_i(t)) \log_2 p(x_i(t)) \quad (4.1)$$

where  $I$  is the number of bins needed for estimating the amplitude histogram of  $x(t)$ , an approximation to the probability distribution function of the signal.

Then, the AMIF of  $x(t)$  is given by  $H_{x(t)}$ , by  $H_{x(t+\tau)}$ , obtained by shifting  $x(t)$  a time lag  $\tau$  as  $x(t+\tau)$ , and their bivariate probability distribution leading to  $H_{x(t)x(t+\tau)}$  as shown in Eq. 4.2 [50].

$$AMIF_{xx}(\tau) = H_{x(t)} + H_{x(t+\tau)} - H_{x(t)x(t+\tau)} \quad (4.2)$$

Therefore, this function describes the amount of common information between the original time series  $x(t)$  and the time shifted time series  $x(t+\tau)$ . In the case of statistically independent time series, the  $AMIF_{xx}$  is zero, otherwise positive. The AMIF is normalized to its maximum amplitude (in  $\tau = 0$ ) representing the entire information of a time series. The decay of this function over a time lag  $\tau$  represents the loss of information with respect to this prediction time, and in the case of non-linear HRV analysis, it is assumed to quantify the complexity of autonomic communication [49]. In the case of a random and unpredictable time series, the AMIF decays to 0 for all prediction times  $\tau$  apart from  $\tau = 0$ . On the contrary, in the case of a predictable time series the AMIF remains at 1 for all  $\tau$  [78].

### 4.2.3 AMIF-based measures

In order to describe HRV complexity during emotion elicitation, the evolution of the information function over the time scale  $\tau$  should be taken into consideration. The AMIF (Fig. 4.1) applied to the  $RR(t)$  time series was characterized by the following parameters:  $BD$  is the beat decay that corresponds with the AMIF decay from  $\tau = 0$  s to  $\tau_B = 0.6$  s, which represents a standard mean beat period [78]. Also,  $A_{T_{RR}}$  is the total area under the curve that has been proposed to characterize the morphology, predictability and regularity of the signal [13].

The AMIF applied to the filtered time series  $RR_{LF}(t)$ ,  $RR_{HF}(t)$  and  $RR_{SC}(t)$  was characterized by the following parameters:  $PD_{\delta}$  is the peak decay that shows the information decay at the maximum peak defined in the interval  $[\tau_a, \tau_b]$ ;  $PD_{m_{\delta}}$  is the mean peak decay within a time range  $[\tau_a, \tau_b]$  that indicates the mean information decrease between two time lags  $\tau_a$  and  $\tau_b$ ; and  $A_{T_{\delta}}$  is the total area under the curve in the same time range  $[\tau_a, \tau_b]$ , where  $\delta = \{LF, HF, SC\}$ .

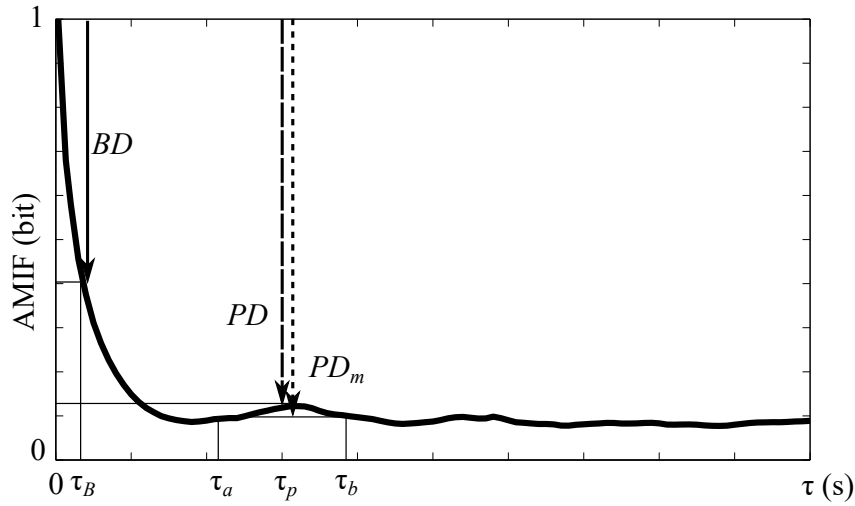


Figure 4.1: The normalized Auto-Mutual Information Function (AMIF) as function of the time scale  $\tau$ . The AMIF value at  $\tau = 0$  represents the entire information of a time series. Beat decay ( $BD$ ) indicates the AMIF decay over a standard heart beat period ( $\tau_B$ ). Mean peak decay ( $PD_m$ ) indicates the mean information decrease between  $\tau_a$  and  $\tau_b$ . Peak decay ( $PD$ ) indicates the information decay at the maximum peak ( $\tau_p$ ) defined in the interval  $[\tau_a, \tau_b]$ .

Since the information flow of oscillators has its peak starting at half the period  $\tau = (1/(2f), 1/f, 3/(2f), \dots)$ , the lower and upper time scale boundaries  $[\tau_a, \tau_b]$  within the AMIF were chosen at  $\tau = 1/(2f)$ , where  $f$  is the frequency band boundaries used in the band pass filters [49] as: (1) the traditional LF range of  $[0.04, 0.15]$  Hz corresponds to a LF prediction time range of  $\tau_{LF} = [\tau_a = 1/(2*0.15), \tau_b = 1/(2*0.04)] = [3.33, 12.5]$  s; (2) the traditional HF range corresponds to a HF prediction time range of  $[0.15, 0.40]$  Hz as  $\tau_{HF} = [\tau_a = 1/(2*0.40), \tau_b = 1/(2*0.15)] = [1.25, 3.33]$  s and (3) the SCHF band  $[a_{max}, b_{max}]$  corresponds to a SCHF prediction time range of  $\tau_{SC} = [\tau_a = 1/(2b_{max}), \tau_b = 1/(2a_{max})]$  s. In Table 4.2, the values for lower- and upper-time scale boundaries corresponding to the SCHF prediction time range of  $\tau_{SC}$  in terms of median and interquartile ranges, as first and third quartile, (Median (Q1|Q3)) are specified.

Table 4.2: Median (Q1|Q3) values for lower- ( $\tau_a$ ) and upper-time ( $\tau_b$ ) scale boundaries corresponding to the SCHF prediction time range for relax, joy, fear, sadness and anger.

Elicitation	$\tau_a$	$\tau_b$
Relax	1.25 (1.19 1.43)	2.38 (1.85 2.78)
Joy	1.22 (0.98 1.28)	2.00 (1.85 2.27)
Fear	1.25 (1.14 1.39)	2.08 (1.92 2.50)
Sadness	1.25 (1.11 1.39)	2.08 (1.85 2.50)
Anger	1.25 (1.16 1.39)	2.08 (1.85 2.38)

#### 4.2.4 Cross-Mutual Information Function

The CMIF is a non-linear equivalent of the cross-correlation function, based on the Shannon entropy similarly to the AMIF, but quantifying the coupling between two signals  $x(t)$  and  $y(t)$ . This function describes the amount of common information between a time series  $x(t)$  and a time shifted time series  $y(t+\tau)$ . Then, the CMIF of  $x(t)$  and  $y(t+\tau)$  is given by  $H_{x(t)}$ , by  $H_{y(t+\tau)}$ , and their bivariate probability distribution leading to  $H_{x(t)y(t+\tau)}$  as shown in Eq. 4.3 [50].

$$CMIF_{xy}(\tau) = H_{x(t)} + H_{y(t+\tau)} - H_{x(t)y(t+\tau)} \quad (4.3)$$

In contrast to the AMIF, the CMIF is not normalized for its analysis and it does not present a symmetric distribution around zero. Therefore, left and right sides of the CMIF around zero were analyzed. The non-linear analysis of the coupled signals using the CMIF was as described for the AMIF, i.e., the CMIF at  $\tau = 0$  represents the common maximum information of both time series and the decay of this function over a prediction time describes the loss of information over this  $\tau$  [50].

### 4.2.5 CMIF-based measures

In order to quantify and extract the amount of mutual information between the synchronized registered time series of HRV and respiration during emotion elicitation, the coupling between  $RR(t)$  and  $r(t)$ , and between  $RR_{SC}(t)$  and  $r(t)$  was investigated. Only the  $RR(t)$  and the  $RR_{SC}(t)$  series have been taken into consideration because respiratory information is not consistently contained in the LF or HF bands for all subjects.

The following parameters were calculated from the CMIF of the synchronized cardiac and respiratory signals:  $CMIF_0$  defined as the CMIF value at  $\tau = 0$  that represents the amount of common information between both time series without time lag;  $CMIF_{max}$  defined as the maximum CMIF value that shows the maximum coupling between the signals; and  $\tau_{max}$  defined as the time lag between  $CMIF_{max}$  and  $CMIF_0$ , that indicates the time lag between the amount of common information of the time series and the maximum coupling between the signals. For this analysis, the CMIF parameters were defined as follow:  $CMIF_{0\gamma}$ ,  $CMIF_{max\gamma}$  and  $\tau_{max\gamma}$  in the coupling between each  $\gamma = \{RR, SC\}$  and  $r(t)$ . In Fig. 4.2, it is presented a CMIF function.

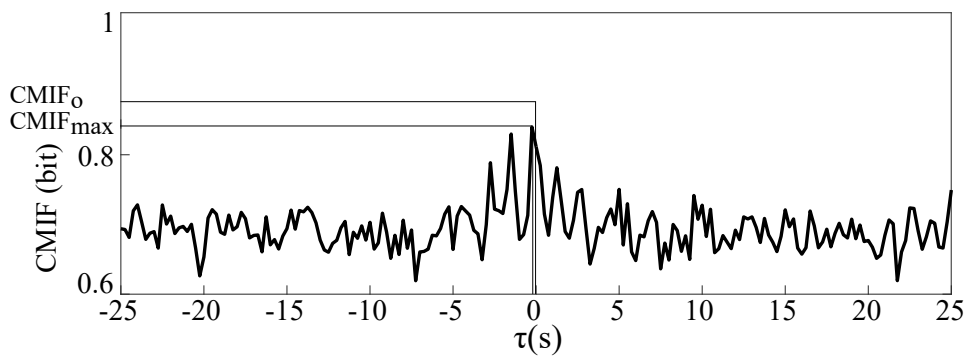


Figure 4.2: The Cross-Mutual Information Function (CMIF) of the coupling between  $RR(t)$  and  $r(t)$  as function of the time scale  $\tau$ . The CMIF value at  $\tau = 0$  ( $CMIF_0$ ) represents the amount of common information of the time series without time lag and the maximum coupling between the signals is represented by  $CMIF_{max}$ .

### 4.2.6 Selection of the number of bins

The discrete probability distribution  $p(x_i(t))$  corresponds to a partitioning of the amplitude range of each signal in a histogram, and  $I = 2^N$  represents the maximum possible information that can be obtained ( $I$  is the number of bins of the histogram and  $N$  is the number of bits).

In order to adapt the algorithms of the AMIF and the CMIF to short-term time series,  $2^N$  for  $N = \{3, 4, 5, 6, 7, 8, 9\}$  bits were considered in the calculation methodology. The number of parameters able to statistically discriminate between relax and emotions and between pairs of emotions were assessed to determine the adequate number of histogram bins  $I$ .

### 4.2.7 Statistical analysis

Normality distribution of all parameters was evaluated by Lillie test. Then, the T-test or the Wilcoxon test when necessary, depending on normality test results, was applied to evaluate differences for the followed paired conditions: relax and each emotion and also each emotion was compared with each other.

The significance statistical level was  $p\text{-value} \leq 0.05$ , since this threshold provides a reliable value for statistical discrimination [87]. Additionally, the area under the receiver operating characteristic curve (AUC) was studied to analyze the capability of the parameters to discriminate the studied elicitations and  $AUC \geq 0.70$  was used to determine statistically significant differences for each studied parameter. Furthermore, leave-one-out cross-validation method was used [72] to assess sensitivity, specificity and accuracy values for each parameter in 2-class emotion classification. These statistical parameters were required to be  $\geq 70\%$  to determine statistically significant differences for each studied parameter. These thresholds have been selected as optimal cut-points values due to sensitivity

and specificity being the closest to the value of the area under the ROC curve [98].

The number of bins  $I$  was selected as the value which yielded the highest number of parameters with statistically significant differences ( $p\text{-value} \leq 0.001$ ) between relax and each emotion and between pairs of emotions.

## 4.3 Results

### 4.3.1 Selection of the number of bins

The following analyzes have been performed to evaluate the adequate  $I$  for the AMIF and the CMIF calculation for emotion recognition using short-time HRV signals.

In Fig. 4.3, it is shown the percentage of the number of parameters that present statistically significant differences for each proposed  $I$ , when comparing relax with each emotions or between each pairs of emotions. The value  $I = 2^5$  was selected, since it presents the highest number of parameters with statistically significant differences,  $p\text{-value} \leq 0.001$  and sensitivity, specificity and accuracy  $\geq 70\%$  and AUC index  $\geq 0.70$  for both non-linear techniques.

### 4.3.2 AMIF-based measures

Those AMIF-based parameters that revealed statistically significant differences between relax and the different emotions or between pairs of emotions are presented in Fig. 4.4. In this figure, boxplots are shown in terms of median and interquartile ranges as first and third quartile:  $A_{T_\gamma}$  (Fig. 4.4a) for  $\gamma = \{RR, LF, HF, SC\}$ ;  $BD$  (Fig. 4.4b) analyzed on  $RR(t)$ ; and  $PD_{m_\delta}$  (Fig. 4.4c) for  $\delta = \{LF, HF, SC\}$ .

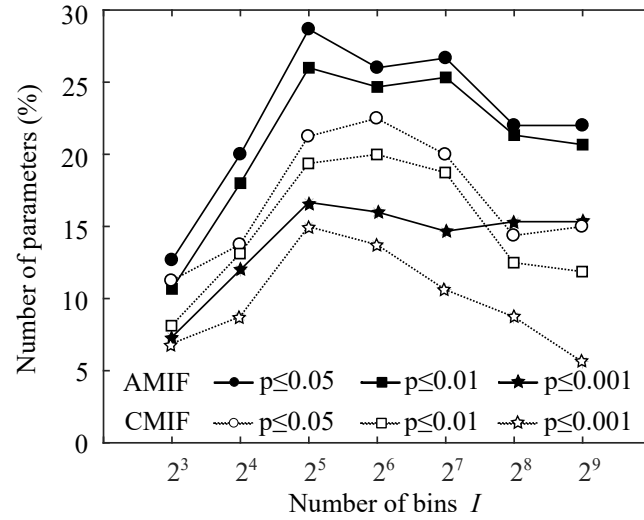


Figure 4.3: Percentage of number of parameters derived from the AMIF and the CMIF function of each proposed bin number  $I$  presenting statistically significant differences: ( $p$ -value  $\leq 0.05$ ,  $p$ -value  $\leq 0.01$  and  $p$ -value  $\leq 0.001$  when comparing relax and each emotion and between pairs of emotions. All these counted parameters also presented a sensitivity, specificity and accuracy  $\geq 70\%$  and AUC index  $\geq 0.70$ ).

In Table 4.3,  $p$ -value, AUC and accuracy values are remarked in bold type for those AMIF-based parameters that revealed statistically significant differences between the emotional states studied.

The presented emotion conditions were those which revealed statistically significant differences.

### 4.3.3 CMIF-based measures

All parameters derived from the CMIF have been evaluated, however, only those that revealed statistically significant differences for their ability to discriminate between pair of emotions are shown in Fig. 4.5. In this figure, boxplots are shown in terms of median and interquartile ranges as first and third quartile:  $CMIF_{0\gamma}$  (Fig. 4.5a);  $CMIF_{max\gamma}$  (Fig. 4.5b) and  $\tau_{max\gamma}$  (Fig. 4.5c) for the coupling between each signal  $\gamma = \{RR, SC\}$  and  $r(t)$ .

In Table 4.4,  $p$ -value, AUC and accuracy values are remarked in bold type for those CMIF-based parameters that revealed statistically significant differences between the emotional states studied.

The presented elicited conditions were those which revealed statistically significant differences.



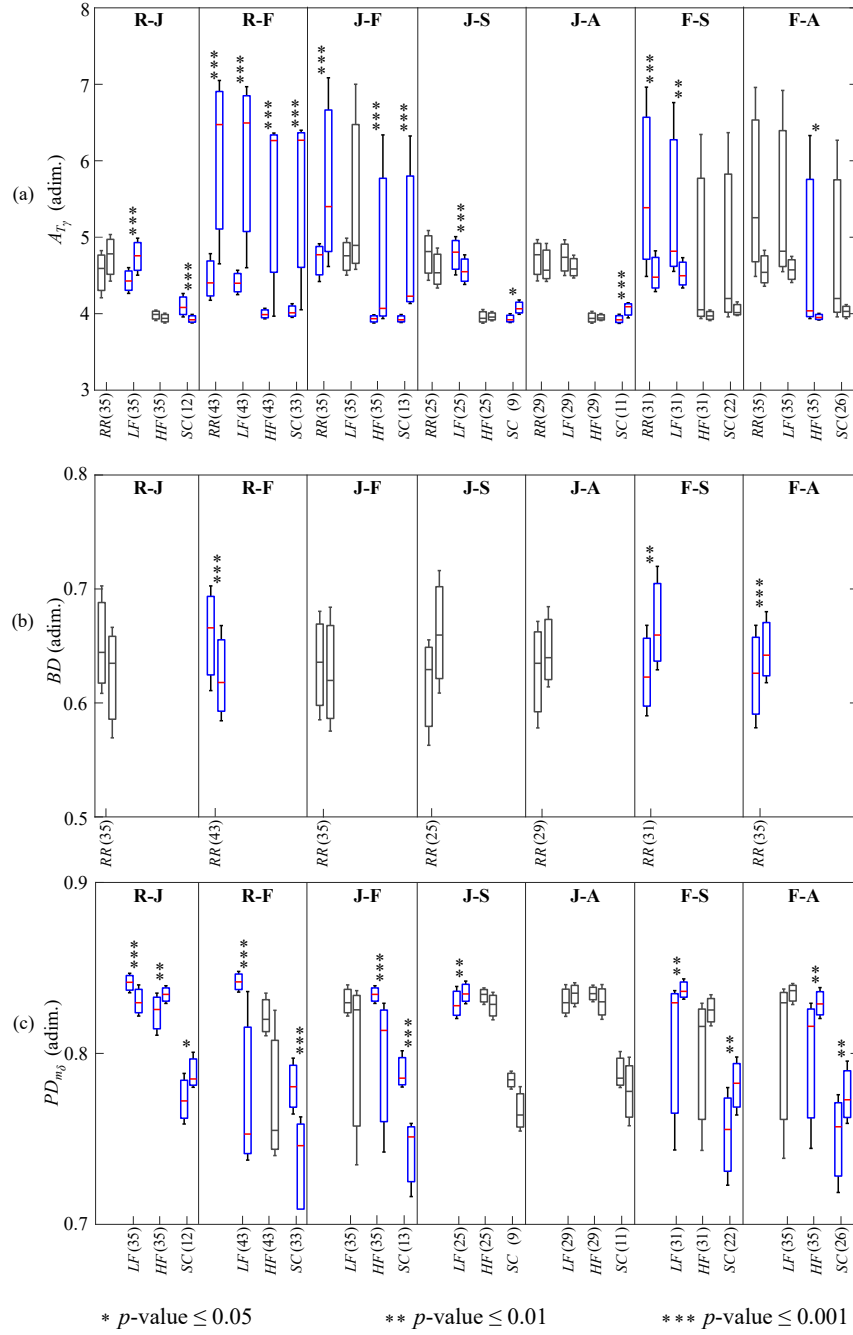


Figure 4.4: Boxplots of the parameters derived from the AMIF: (a)  $A_{T_\gamma}$  for  $\gamma = \{RR, LF, HF, SC\}$ ; (b)  $BD$  analyzed on  $RR(t)$ ; and (c)  $PD_{m_\delta}$  for  $\delta = \{LF, HF, SC\}$ . Only compared elicitations with some statistically significant differences are presented: relax and joy (R-J), relax and fear (R-F), joy and fear (J-F), joy and sadness (J-S), joy and anger (J-A), fear and sadness (F-S) and fear and anger (F-A). Statistical significance is denoted by: \* for  $p\text{-value} \leq 0.05$ , \*\* for  $p\text{-value} \leq 0.01$  and \*\*\* for  $p\text{-value} \leq 0.001$ , all showed sensitivity, specificity and accuracy values  $\geq 70\%$  and AUC index  $\geq 0.70$ . The number of the analyzed subjects is indicated in parentheses.

Table 4.3: Values of  $p$ -value, AUC and accuracy for the parameters derived from AMIF which statistically discriminate between some pair of elicitations: relax and joy (R-J), relax and fear (R-F), joy and fear (J-F), joy and sadness (J-S), joy and anger (J-A), fear and sadness (F-S) and fear and anger (F-A). The number of the analyzed subjects for each parameter and pair of elicitations is indicated in parentheses.

Parameters	R-J	R-F	J-F	J-S	J-A	F-S	F-A
$A_{T_{RR}}$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	n.s.	$\leq 0.001$	$\leq 0.001$	n.s.	n.s.	$\leq 0.001$	$\leq 0.001^\dagger$
AUC	0.62	<b>0.81</b>	<b>0.72</b>	0.63	0.55	<b>0.73</b>	0.72
Accuracy (%)	61	<b>77</b>	<b>71</b>	64	60	<b>73</b>	73
$A_{T_{LF}}$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	$\leq 0.001$	$\leq 0.001$	$\leq 0.05$	$\leq 0.001$	$\leq 0.05$	$\leq 0.01$	$\leq 0.05$
AUC	<b>0.76</b>	<b>0.82</b>	0.64	<b>0.71</b>	0.62	<b>0.73</b>	0.67
Accuracy (%)	<b>73</b>	<b>78</b>	66	<b>70</b>	62	<b>70</b>	64
$A_{T_{HF}}$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	n.s.	$\leq 0.001$	$\leq 0.001$	n.s.	n.s.	$\leq 0.001$	$\leq 0.05$
AUC	0.63	<b>0.71</b>	<b>0.77</b>	0.58	0.53	0.67	<b>0.70</b>
Accuracy (%)	64	<b>70</b>	<b>71</b>	62	57	65	<b>70</b>
$A_{T_{SC}}$	(12)	(33)	(13)	(9)	(11)	(22)	(26)
$p$ -value	$\leq 0.001$	$\leq 0.001$	$\leq 0.001$	$\leq 0.05$	$\leq 0.001$	$\leq 0.01$	$\leq 0.05$
AUC	<b>0.83</b>	<b>0.75</b>	<b>0.95</b>	<b>0.88</b>	<b>0.85</b>	0.66	0.68
Accuracy (%)	<b>75</b>	<b>74</b>	<b>92</b>	<b>78</b>	<b>77</b>	66	71
$BD$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	$\leq 0.01$	$\leq 0.001$	$\leq 0.01$	$\leq 0.01$	n.s.	$\leq 0.01$	$\leq 0.001$
AUC	0.65	<b>0.78</b>	0.68	0.67	0.62	<b>0.72</b>	<b>0.71</b>
Accuracy (%)	67	<b>77</b>	67	66	60	<b>73</b>	<b>73</b>
$PD_{m_{LF}}$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	$\leq 0.001$	$\leq 0.001$	$\leq 0.01$	$\leq 0.01$	n.s.	$\leq 0.01$	$\leq 0.05$
AUC	<b>0.76</b>	<b>0.81</b>	0.63	<b>0.71</b>	0.61	<b>0.70</b>	0.67
Accuracy (%)	<b>73</b>	<b>77</b>	69	<b>70</b>	60	<b>70</b>	63
$PD_{m_{HF}}$	(35)	(43)	(35)	(25)	(29)	(31)	(35)
$p$ -value	$\leq 0.01$	$\leq 0.001^\dagger$	$\leq 0.001$	n.s.	n.s.	$\leq 0.01$	$\leq 0.01$
AUC	<b>0.70</b>	0.71	<b>0.81</b>	0.64	0.59	0.68	<b>0.72</b>
Accuracy (%)	<b>71</b>	72	<b>80</b>	66	64	68	<b>70</b>
$PD_{m_{SC}}$	(12)	(33)	(13)	(9)	(11)	(22)	(26)
$p$ -value	$\leq 0.05$	$\leq 0.001$	$\leq 0.001$	n.s.	n.s.	$\leq 0.01$	$\leq 0.01$
AUC	<b>0.72</b>	<b>0.81</b>	<b>0.99</b>	0.79	0.64	<b>0.74</b>	<b>0.70</b>
Accuracy (%)	<b>75</b>	<b>77</b>	<b>96</b>	78	68	<b>70</b>	<b>70</b>

n.s. Stands for non-significant.

$^\dagger$  Sensitivity or specificity  $\leq 70\%$ .

Note that parameters with  $p \leq 0.05$ , AUC index  $\geq 0.70$ , sensitivity, specificity, accuracy values  $\geq 70\%$  are remarked in bold type.

## 4.4 Discussion

The AMIF and the CMIF techniques have been proposed to study the non-linear relationships between HRV and respiration for human emotion recognition. Both non-linear techniques may provide complementary information to that captured by linear techniques for emotion recognition.

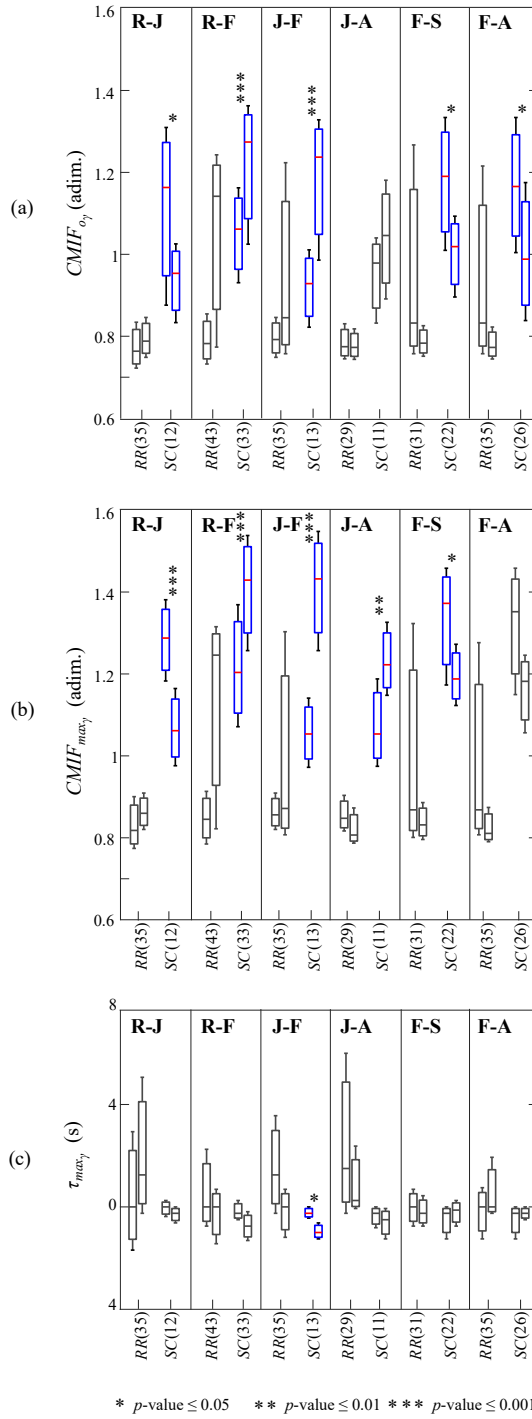


Figure 4.5: Boxplots of the parameters derived from the CMIF: (a)  $CMIF_{0\gamma}$ , (b)  $CMIF_{max\gamma}$  and (c)  $\tau_{max\gamma}$ , for the coupling between each of the signals  $\gamma = \{RR, SC\}$  and  $r(t)$  and all emotion conditions studied with statistically significant differences: relax and joy (R-J), relax and fear (R-F), joy and fear (J-F), joy and anger (J-A), fear and sadness (F-S) and fear and anger (F-A). Statistical significance is denoted by: \* for  $p\text{-value} \leq 0.05$ , \*\* for  $p\text{-value} \leq 0.01$  and \*\*\* for  $p\text{-value} \leq 0.001$ , all with sensitivity, specificity and accuracy  $\geq 70\%$  and AUC index  $\geq 0.70$ . In each x-axis the number of the analyzed subjects is indicated in parentheses.

Table 4.4: Values of  $p$ -value, AUC and accuracy for the parameters derived from CMIF which statistically discriminate between some pair of elicitations: relax and joy (R-J), relax and fear (R-F), joy and fear (J-F), joy and anger (J-A), fear and sadness (F-S) and fear and anger (F-A). The number of the analyzed subjects for each parameter and pair of elicitations is indicated in parentheses.

Parameters	R-J	R-F	J-F	J-A	F-S	F-A
$CMIF_{0RR}$	(35)	(43)	(35)	(29)	(31)	(35)
$p$ -value	n.s.	$\leq 0.001^\dagger$	$\leq 0.01$	n.s.	$\leq 0.01$	$\leq 0.05$
AUC	0.61	0.75	0.65	0.53	0.65	0.65
Accuracy (%)	61	78	70	53	66	64
$CMIF_{0SC}$	(12)	(33)	(13)	(11)	(22)	(26)
$p$ -value	<b><math>\leq 0.05</math></b>	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.001</math></b>	n.s.	<b><math>\leq 0.05</math></b>	<b><math>\leq 0.05</math></b>
AUC	<b>0.70</b>	<b>0.73</b>	<b>0.85</b>	0.69	<b>0.72</b>	<b>0.70</b>
Accuracy (%)	<b>71</b>	<b>73</b>	<b>85</b>	64	<b>70</b>	<b>70</b>
$CMIF_{maxRR}$	(35)	(43)	(35)	(29)	(31)	(35)
$p$ -value	n.s.	$\leq 0.001^\dagger$	$\leq 0.05$	n.s.	$\leq 0.01$	n.s.
AUC	0.62	0.72	0.60	0.64	0.63	0.66
Accuracy (%)	64	76	70	66	68	63
$CMIF_{maxSC}$	(12)	(33)	(13)	(11)	(22)	(26)
$p$ -value	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.001</math></b>	<b><math>\leq 0.01</math></b>	<b><math>\leq 0.01</math></b>	$\leq 0.01$
AUC	<b>0.88</b>	<b>0.74</b>	<b>0.95</b>	<b>0.79</b>	<b>0.77</b>	0.68
Accuracy (%)	<b>83</b>	<b>71</b>	<b>85</b>	<b>77</b>	<b>75</b>	69
$\tau_{maxRR}$	(35)	(43)	(35)	(29)	(31)	(35)
$p$ -value	n.s.	n.s.	n.s.	n.s.	n.s.	n.s.
AUC	0.62	0.53	0.66	0.56	0.53	0.55
Accuracy (%)	66	55	67	57	56	57
$\tau_{maxSC}$	(12)	(33)	(13)	(11)	(22)	(26)
$p$ -value	n.s.	$\leq 0.01$	<b><math>\leq 0.05</math></b>	n.s.	$\leq 0.05$	n.s.
AUC	0.62	0.68	<b>0.75</b>	0.66	0.62	0.51
Accuracy (%)	63	65	<b>77</b>	68	61	60

n.s. Stands for non-significant.

$^\dagger$  Sensitivity or specificity  $\leq 70\%$ .

Note that parameters with  $p \leq 0.05$ , AUC index  $\geq 0.70$ , sensitivity, specificity, accuracy values  $\geq 70\%$  are remarked in bold type.

The adequate number of bins  $I$  was estimated to adapt the AMIF and the CMIF algorithms to short-time signals for emotion recognition, since the values of  $I$  applied to long-term HRV may not be suitable for short-term. The value of  $I$  determines the histogram partitioning. The greater the  $I$  value is, the histogram represents more faithfully the probability density function. Nevertheless, each partitioning of the histogram needs to contain a minimum number of samples in order to capture the regularity and complexity signal contain more appropriately. Therefore, a compromise between the greatest number of partitioning of the histogram for faithfully describing the signal, and the adequate number of samples contained in each partitioning, should be taken into consideration.

In [50], the AMIF and the CMIF histogram were constructed by using  $2^5$  bins, when studying short-term RR signals according to Task Force guidelines [88, 94], in a group of patients after acute myocardial infarction and a control group. However,  $2^3$  bins were proposed in [49] for the AMIF histogram computation for short and long-term signals, to analyze the risk stratification of patients with multiple organ dysfunction syndrome, cardiac arrest patients and a control group. In this work, the highest percentage of number of parameters that presents statistically significant differences ( $p$ -value  $\leq 0.001$ ) between each pair of elicited states was obtained for  $I = 2^5$  bins, (see Fig. 4.3).

Table 4.5 displays the parameters which statistically discriminate between each pair of elicitations. The pair of elicited conditions which did not show statistically significant differences by means of any of the parameters considered in this work were: relax and sadness (R-S), relax and anger (R-A) and sadness and anger (S-A). It should be noted that no statistically significant differences between relax and emotions or between pairs of emotions were found by any parameter derived from analysis of the coupling between the signals  $RR(t)$  and  $r(t)$ . As it was found by analyzing the AMIF technique, the pair of elicitation conditions which did not show statistically significant differences in the CMIF by means of any of the parameters considered was: relax and sadness (R-S), relax and anger (R-A), joy and sadness (J-S) and sadness and anger (S-A).

Regarding the ability of the AMIF parameters to discriminate emotions, the total areas (Fig. 4.4a),  $A_{TSC}$  was the only parameter capable of statistically distinguishing joy and anger among all the studied parameters derived from the AMIF. This result shows the importance of redefining the boundary of the HF band for a correct evaluation of physiological changes of the ANS [43, 101]. Fear revealed a greater median value than any other emotion. It can be noted that an enlargement of the area under the AMIF curve indicates a better predictability of future heart beats, and therefore, a lower

Table 4.5: Parameters derived from the AMIF and the CMIF which statistically discriminate between the studied elicitations.

Compared elicited states	R-J	R-F	J-F	J-S	J-A	F-S	F-A
Parameters derived from the AMIF							
$A_{TRR}$	-	yes	yes	-	-	yes	-
$A_{TLF}$	yes	yes	-	yes	-	yes	-
$A_{THF}$	-	yes	yes	-	-	-	yes
$A_{TSC}$	yes	yes	yes	yes	yes	-	-
$BD$	-	yes	-	-	-	yes	yes
$PD_{mLF}$	yes	yes	-	yes	-	yes	-
$PD_{mHF}$	yes	-	yes	-	-	-	yes
$PD_{mSC}$	yes	yes	yes	-	-	yes	yes
Parameters derived from the CMIF							
$CMIF_{0SC}$	yes	yes	yes	-	-	yes	yes
$CMIF_{maxSC}$	yes	yes	yes	-	yes	yes	-
$\tau_{maxSC}$	-	-	yes	-	-	-	-

The nomenclature used for the elicited states is:  
relax (R), joy (J), fear (F), sadness (S) and anger (A)

complexity [13].

Evaluating the beat decay  $BD$  (Fig. 4.4b), fear presented smaller median values than any other compared elicitation. Furthermore, this parameter was able to statistically distinguish between fear and relax, sadness and anger. However, the remaining pair of compared elicited states did not show such a clear pattern as fear. Additionally,  $PD_{m\delta}$  (Fig. 4.4c) presented a similar tendency as the  $BD$  for fear with a smaller median value than any other elicitation state. The  $BD$  and  $PD_{m\delta}$  presented results with complementary information, and statistically significant values, and also adequate sensitivity, specificity, accuracy and AUC index.

The CMIF has been proposed to reveal non-linear cardiorespiratory interdependencies [50], which might be altered during emotion elicitation. For example, a significant increase in the CMIF of electroencephalographic signals has been also observed in the presence of stress [1]. In our study, the parameter  $CMIF_{0SC}$  (Fig. 4.5a) and the parameter  $CMIF_{maxSC}$  (Fig. 4.5b) provide similar information, although the slight differences in the calculation of both parameter revealed that  $CMIF_{maxSC}$

is able to discriminate with an equal or better  $p$ -value, sensitivity, specificity, accuracy and AUC index than  $CMIF_{0SC}$  in all compared elicited states, except for fear and anger. Moreover, evaluating  $CMIF_{0SC}$  and  $CMIF_{maxSC}$ , it is possible to extract a similar pattern for fear presenting a greater median value than any other elicited state.

The time lag between  $CMIF_0$  and  $CMIF_{max}$  in the SCHF band was the only parameter able to distinguish between joy and fear, and it suggested less non-linear correlation between HRV and respiration during joy. A complexity reduction is observed during fear elicitation as reflected by a lower value of parameter  $\tau_{maxSC}$ .

Furthermore, joy or fear versus sadness can be discriminated by parameters obtained from  $RR_{LF}(t)$  signals and joy or fear versus anger from  $RR_{HF}(t)$  signals. Predominant autonomic rhythms can be assessed by the complex information loss over their respective prediction time horizon [50]. In this sense, those parameters studied in the LF band reflect the complexity of vagal and sympathetic mechanisms, and those parameters studied in the HF band reflect the complexity of vagal and respiratory rhythms [50].

Comparing the results obtained from the AMIF and the CMIF techniques, it is worth noting that filtering the HRV signals into a redefined HF band presents better discrimination power for parameters derived from the AMIF than from the CMIF ones. Furthermore, applying the CMIF into the RR time series filtered into the redefined HF band provided relevant complexity information to discriminate between HRV and respiratory mechanisms in the case of fear.

A complexity reduction is observed during fear elicitation as reflected by smaller  $BD$ ,  $PD_{m_\delta}$  and  $\tau_{maxSC}$  values together with a greater total area,  $CMIF_{0SC}$  and  $CMIF_{maxSC}$ .

In [14], a physiological explanation of non-linear HRV parameters was reported. In this work, non-

linear HRV indices during ANS pharmacological blockade and body position changes were studied in order to assess their relation with sympathetic and parasympathetic activities. Parasympathetic blockade caused a significant decrease in complexity values, while sympathetic blockade produced a significant increase in the non-linear parameters. We hypothesize that the decrease in complexity observed during fear elicitation reflects vagal activity, while more random RR series during joy might reflect sympathetic activity.

The results derived from this work have been compared with a previous work on the same emotion database, where a linear-based methodology was applied [101] (Table 4.6). In both cases the HF band was analyzed after redefining it considering the HRV-respiration interaction [101]. All the elicited states able to be discriminated with linear techniques, remain discriminated with the non-linear features (Table 4.6). In addition, during fear elicitation, heart rate presents a better predictability, implying lower complexity, as compared to other elicited states, resulting in extra discriminating power between fear and relax or anger (Table 4.6) non accessible from linear features. These results may indicate that the non-linear indexes are suitable for discrimination between different emotions.

Table 4.6: Discriminating possibility in comparing between elicited states with linear and non-linear techniques.

Compared elicited states	Linear techniques [101]	Non-linear techniques (This work)
R-J	yes	yes
R-F	no	yes
R-S	no	no
R-A	no	no
J-F	yes	yes
J-S	yes	yes
J-A	yes	yes
F-S	yes	yes
F-A	no	yes
S-A	no	no

The nomenclature used for the elicited states is:  
relax (R), joy (J), fear (F), sadness (S) and anger (A)

Furthermore, other non-linear HRV parameters as the Correlation Dimension, the Approximate En-



tropy and the Sample Entropy have been investigated in the same emotional database. However, these parameters did not present the ability to separate the emotional states in this analyzed database (Table 4.7, Table 4.8). Although in some comparisons exposed in Table 4.8 the  $p$ -value  $\leq 0.05$ , AUC index  $\geq 0.7$ , or sensitivity, specificity or accuracy  $\geq 70\%$  criteria were not met.

Table 4.7: Median with the first and third interquartile ranges in terms of (m(1st|3th)) for the non-linear techniques Correlation Dimension (D2), Approximate Entropy (ApEn) and Sample Entropy (SampEn) for the elicitations: relax, joy, fear, sadness and anger.

Elicited states	D2	ApEn	SampEn
Relax	4.18 (3.72 4.63)	0.84 (0.78 0.91)	1.09 (0.96 1.29)
Joy	3.89 (3.32 4.60)	0.84 (0.71 0.93)	1.13 (0.81 1.23)
Fear	4.20 (3.69 4.87)	0.85 (0.79 0.95)	1.18 (0.93 1.33)
Sadness	4.42 (4.06 4.73)	0.87 (0.81 0.93)	1.14 (0.98 1.34)
Anger	4.21 (3.84 4.67)	0.89 (0.78 0.93)	1.15 (0.90 1.31)

In Table 4.1, there are summarized the non-linear techniques used to detect emotional stimuli based on HRV analysis. In [102], the emotional states were conceptualized in two dimensions by the terms of valence and arousal. The Dominant Lyapunov Exponent and the Approximate Entropy techniques showed differences between the neutral and the arousal elicitation. These results are in concordance with the ones obtained in this study by means of the AMIF and the CMIF techniques, since statistically significant differences between the neutral state of relax and the two high arousal elicitations of joy and fear were found. Furthermore, it was found in [102] that the Dominant Lyapunov Exponent became negative, and the mean Approximate Entropy decreased during arousal elicitation. In accordance with the Dominant Lyapunov Exponent and the Approximate Entropy, during fear elicitation the non-linear HRV parameters obtained in the present study revealed a reduced complexity level. In [13], an increment of the total area under the AMIF curve was observed revealing an indication of decreased complexity of cardiac regulation in depressed patients. However, in [112], a consistent increasing trend among most entropy measures for different depression levels was found. This suggested a reduced regularity and predictability of the depressed patients. The depression state is

considered by means of the circumplex model of affect as having negative valence with low arousal, as can be sadness [102]. Considering the parameter  $A_{TRR}$  in the comparison between fear and sadness (emotional states with the same negative valence but different arousal), it could be observed that sadness presents a lower median value, being an indicator of decreased complexity as reported in [13], and being in agreement with the results obtained by [112]. In [110], a significantly increase of the entropy measures was found during the emotional states of happiness, sadness, anger, and disgust. These results are in concordance with the ones obtained in this study for fear, which revealed increased regularity and a reduced unpredictability. In [31], significant decreases in the Entropy, the Dominant Lyapunov Exponent, and the Pointwise Correlation Dimension, and an increase in the short-term fractal-like scaling exponent of the Detrended Fluctuation Analysis were found during anxiety situations, compared with the rest period. These results suggest that an increase of anxiety was related to the decrease in the complexity. The anxiety state can be considered by means of the circumplex model of affect [102] as having negative valence with high arousal, similar to fear. Both the state of anxiety studied in [31] and the emotional state of fear, studied in this work, presented the same tendency in level of complexity. In [44], maximum changes in the Lagged Poincaré Plot measures were found during the happiness stimuli, and minimum changes were obtained during the fear inducements. These results are in agreement with the ones obtained by means the CMIF technique applied in the present study, where differences between joy and fear could be found.

There are also some limitations to note regarding this study. First, the sample size database used is small. Nonetheless, the results obtained advocated in support of using the proposed approaches, although a bigger sample size database could probably yield better statistics. Second, likewise, long-time emotional monitoring could probably provide additional information that cannot be detected in

short-time series analyzes. Although, short-term emotional analyzes are more suitable for outpatient patient monitoring and applications where the result is urgently needed. Third, there are emotions that could not be expressed by the subject all the time the videos last, but they have been treated as if the subject expresses that emotion all the time.

Despite these limitations, the parameters derived from the AMIF and the CMIF techniques which presented statistically significant differences for emotion discrimination seem to be good candidates to be implemented on a biomedical equipment, providing a tool for mental illness diagnoses. In addition, analyzing the role of mutual information-based HRV measures to explore a multi-variable approach combining with other non-linear parameters could open a door to extract new suitable parameters for emotion recognition.

Table 4.8: Values of p-value, AUC index, sensitivity, specificity and accuracy for the non-linear techniques Correlation Dimension (D2), Approximate Entropy (ApEn) and Sample Entropy (SampEn) for all elicitation compared.

Compared elicited states	Parameter	D2	ApEn	SampEn
Relax vs. Joy	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.57	0.50	0.55
	Sensitivity (%)	51	40	46
	Specificity (%)	69	77	69
	Accuracy (%)	60	59	57
Relax vs. Fear	<i>p</i> -value	n.s.	0.03	n.s.
	AUC	0.52	0.58	0.53
	Sensitivity (%)	56	44	47
	Specificity (%)	49	77	72
	Accuracy (%)	52	60	59
Relax vs. Sadness	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.54	0.53	0.53
	Sensitivity (%)	63	57	57
	Specificity (%)	57	53	57
	Accuracy (%)	60	55	57
Relax vs. Anger	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.54	0.57	0.56
	Sensitivity (%)	56	62	59
	Specificity (%)	59	59	62
	Accuracy (%)	57	60	60
Joy vs. Fear	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.56	0.54	0.56
	Sensitivity (%)	60	63	43
	Specificity (%)	52	46	74
	Accuracy (%)	56	54	59
Joy vs. Sadness	<i>p</i> -value	0.01	0.05	0.01
	AUC	0.70	0.57	0.60
	Sensitivity (%)	80	68	76
	Specificity (%)	64	52	48
	Accuracy (%)	72	60	62
Joy vs. Anger	<i>p</i> -value	n.s.	n.s.	0.04
	AUC	0.62	0.55	0.60
	Sensitivity (%)	72	55	41
	Specificity (%)	55	62	83
	Accuracy (%)	64	59	62
Fear vs. Sadness	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.58	0.49	0.52
	Sensitivity (%)	84	68	65
	Specificity (%)	45	45	45
	Accuracy (%)	65	56	55
Fear vs. Anger	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.52	0.53	0.48
	Sensitivity (%)	66	71	57
	Specificity (%)	49	40	49
	Accuracy (%)	57	56	53
Sadness vs. Anger	<i>p</i> -value	n.s.	n.s.	n.s.
	AUC	0.58	0.53	0.50
	Sensitivity (%)	60	60	44
	Specificity (%)	60	44	68
	Accuracy (%)	60	52	56

## Chapter 5

# Cluster Analysis

### Contents

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## 5.1 Introduction

New generations of human emotion recognition tools are based in classification analysis. A wide range of methods has been used to study affective states. Classifiers like Fisher Discriminant [61], Linear Discriminant Function [108], k-Nearest Neighbour [108], Multilayer Perceptron [108], Neural Networks [51,60], Support Vector Machines [51,54,61] and others are useful to detect emotional elicitation states. Some of these techniques have also been used to study relationships between HRV and respiration signals [51,108]. Table 5.1 reports a summary of different classification techniques applied to HRV parameters during diverse emotional states.

Table 5.1: Summary of classification techniques applied to HRV parameters in different emotional states.

Ref.	Emotional state	Technique	Classification rate
[51]	relax, neutral, startle, apprehension and very apprehension	ANN	77.3%
		SVM	78.5%
		RF	80.8%
		NFS	84.3%
[108]	joy, anger, sadness and pleasure	MP	88.6%
		kNN	90.9%
		LDF	92.1%
[54]	sadness, anger, stress, surprise	SVM	61.8%
[60]	sadness, anger, fear, surprise, frustration, amusement	kNN	72.3%
		LDF	75.0%
		MBP	84.1%
[61]	amusement, contentment, disgust, fear, neutrality, sadness	FD + SVM	92.0%

The nomenclature used is:

Artificial Neural Networks (ANN), Support Vector Machines (SVM), Random Forests (RF), Neuro-Fuzzy System (NFS), Linear Discriminant Function (LDF), k-Nearest Neighbour (kNN), Multilayer Perceptron (MP), Marquardt Backpropagation (MBP), Fisher Discriminant (FD)

In this chapter the classification ability of the HRV parameters presented in previous chapters is investigated using a linear discriminant analysis. The choice of linear discriminant analysis instead of other more complex approaches, such as ANN or SVM, is motivated to facilitate the interpretation of the classification model and to prevent overfitting due to the reduced number of subjects in the database. A linear classifier has been used to identify the best subset of HRV parameters to discriminate between pairs of emotions and between emotional valences.

## 5.2 Methods

The linear discriminant analysis is a statistical method used to construct a predictive model of group classification based on the characteristics observed for each case [59]. The method generates a discriminant function based on linear combinations of the prediction parameters, which allows to obtain the best classification between groups.

The use of a statistical test, such as the analysis of variance (ANO-VA, *ANalysis Of VAriance*), quantitatively determines how separate the values that each characteristic of the analysis takes in the different groups through the significance obtained in the rejection or acceptance of the null hypothesis [2, 47]. In order the results derived from the statistical study to be considered valid, it is necessary that the characteristics studied meet the normality requirement: they must present a normal or Gaussian distribution and they have equal variances in the groups.

### 5.2.1 Estimation of discriminant function

The discriminant function is generated from the values of the prediction parameters of a set of cases whose classification in the different groups is known. Then, this function can subsequently be applied to new cases where the classification is not known, from measurements of the parameters on which the prediction is based. For the classification into two groups, a unique discriminating function needs to be built. The coefficients of the discriminant function are estimated by means of the Fisher procedure. This procedure assigns weights to the parameters which maximizes the variability between the groups (variance between groups) and minimizes the variability within the groups (intragroup variance).

Once the coefficients of the discriminant function have been obtained, the discriminant scores,  $d$  ((5.1)), for each case are calculated. The scores are the basis for the classification in one of the groups.

$$d = c_0 + c_1\chi^1 + \dots + c_p\chi^p = c^T\chi \quad (5.1)$$

where  $c_j, j = 0, \dots, p$ , are the coefficients of the discriminant function and  $\chi^j$  represent the values of the  $p$  parameters selected for each case. The values of the discriminant scores  $d$  defined by the  $c_j$  coefficients should be close between cases of the same group, and differ as much as possible between cases of different groups. Therefore, this criterion maximizes the variability between the groups (maximizes the variance between groups) while minimizes the variability within the groups (intragroup variance).

Once the discriminant function has been obtained and the discriminant scores calculated for each case, a classification rule is used to make the assignment to a specific group. The classification of each case with a score of  $d$  in group  $g$  is done by means of the Bayes classification rule [80].

### 5.2.2 Parameter selection

During the process of parameter selection, all the parameters considered in this study could be included in order to have a greater number of degrees of freedom in the discriminant function, and thus obtain a better classification. However, a commonly accepted and widely used rule is that the number of classification parameters should be less than the square root of the number of cases in the smallest group. In fact, the use of an excessive number of parameters with respect to the number of



cases leads to a biased estimate of the discriminant function, which decreases their ability to classify new cases [4].

A method that allows a reduction in the number of parameters involved in discrimination is stepwise inclusion. In each step new parameters are added or excluded, so that in each step it is obtained the set of parameters with greater discriminant power according to a certain statistical criterion. Among the criteria for selecting parameters in this study the Wilks's Lambda minimization and the F statistic have been used.

Wilks's Lambda ( $\Lambda$ ) distribution is a probability distribution used especially in the context of the likelihood-ratio and multivariate analysis of variance [63].  $\Lambda$  represents the proportion of the total variability due to differences within groups or, alternatively, the proportion of variability not explained by differences between groups. It is calculated as the ratio of the intragroup covariance,  $C_I$ , which is the sum of intragroup squares, measuring the variability within each group, and the total covariance matrix,  $C_T$ , which is the sum of total squares, measuring the total variability, according to the equation (5.2) [79].

$$\Lambda = \frac{|C_I|}{|C_T|} \quad (5.2)$$

The value of Wilks's Lambda is limited between 0 and 1. Values close to 0 indicate that the means of the groups are different (the variability within the groups is small compared to the total variability) while values close to 1 indicate that the means are close. Although Wilks's Lambda criterion identifies the parameters with the greatest discriminating power, it is the F statistic that determines which parameters should be taken into account in the model [79]. The F statistic is calculated based

on the Wilks's Lambda according to the equation (5.3).

$$F = \frac{N - G - p}{G - 1} \frac{1 - \frac{\Lambda_{p+1}}{\Lambda_p}}{\frac{\Lambda_{p+1}}{\Lambda_p}} \quad (5.3)$$

$N$  is the total number of cases,  $G$  is the number of groups,  $p$  is the number of independent parameters,  $\Lambda_p$  is the Wilks's Lambda calculated before the inclusion of the variable being evaluated, and  $\Lambda_{p+1}$  is the Wilks's Lambda calculated after the inclusion of the variable. The  $F$  statistic represents the increase produced in discrimination after the inclusion of the parameter  $p + 1$  with respect to the total already reached with the  $p$  parameters previously included. The stepwise inclusion method are:

- First step: if the input criterion is met ( $F$  statistic is statistically significant ( $F > 3.84$ )) the parameter with the lowest value of the Wilks's Lambda is included.
- Second step: if the input criterion is met, the included parameter is matched with each of the remaining parameters and that pair with the highest value of the  $F$  statistic is chosen.
- Third and subsequent steps: the third and subsequent parameters are selected in a similar way, but checking after each step if the previously included parameters remain significant or if, on the contrary, they can be excluded if they meet the exit criteria ( $F < 2.1$ ). When none of the parameters included meet the input and the exit criterion the process of parameter selection ends.

### 5.2.3 Performance measures of a classifier

To improve the estimation of the correct classification rate, the cross validation technique leave-one-out method has been applied [122]. In this method, each case is classified by the discriminant

function derived from all cases except it. This method is the one used in this study because it corresponds to a more realistic situation, since the case that is classified does not intervene in the elaboration of the model [33].

In addition to the classification rate, there are other classifier performance measures interesting to analyze. If the cases are available in two groups, positive and negative, the results of the classifier can be divided into:

- True positive (TP): cases that are positive, and the classifier considers positive.
- False negatives (FN): cases that are positive, but that are classified as negative.
- True Negative (TN): cases that are negative, and the classifier considers negative.
- False positives (FP): cases that are negative, and the classifier considers positive.

The parameters that allow evaluating the performance of a classifier are defined below:

- Sensitivity (Se): it is defined as the percentage of cases classified as positive among all positive cases (5.4).

$$Se(\%) = \frac{TP}{TP + FN} 100 \quad (5.4)$$

- Specificity (Sp): it is defined as the percentage of cases considered negative by the classifier, among all the negative cases (5.5).

$$Sp(\%) = \frac{TN}{TN + FP} 100 \quad (5.5)$$

- Positive predictive value (P+): it is the percentage of cases classified as positive, which are

really positive (5.6).

$$P+ (\%) = \frac{TP}{TP+FP} 100 \quad (5.6)$$

- Negative predictive value (P-): it is the percentage of cases classified as negative, which are really negative (5.7).

$$P- (\%) = \frac{TN}{TN+FN} 100 \quad (5.7)$$

- Accuracy (Acc): it is the percentage of cases classified correctly. It is, in fact, the classification rate (5.8).

$$Acc(\%) = \frac{TP+TN}{TP+FP+TN+FN} 100 \quad (5.8)$$

In a good classifier, all values should be close to 100%. There is no point in obtaining a very high sensitivity value if the specificity is very low, and vice versa. In general, increasing sensitivity decreases specificity and vice versa, so a compromise between the two must be reached.

### 5.2.4 Parameters considered in the analysis

Only the parameters which presented statistically significant differences in chapter 3 (linear features) and in chapter 4 (non-linear features) were selected as characteristics to be investigated. Nine different subsets of parameters have been analyzed:

- Subset 1 (S1). Classic HRV analysis based on the standard definition of HF band [0.15,0.4

Hz] defined in [94]. The parameters analyzed in this group are:  $P_{HF}$ ,  $P_{LFn}$ ,  $R$  and  $F_R$ .

- Subset 2 (S2). HRV parameters based on the shifted HF band centered at  $F_R$  with fixed bandwidth: the HF band was centered at  $F_R$  and had a fixed bandwidth of 0.11 Hz ( $HF_{F_R}$ ). The parameters analyzed in this group are:  $P_{HF_{F_R}}$ ,  $P_{LFn_{F_R}}$ ,  $R_{F_R}$  and  $F_{R_{F_R}}$ .
- Subset 3 (S3). HRV parameters based on the shifted and resized HF band based on Spectrum Correlation (SCHF): the HF band is redefined based on the correlation between the power content of HRV and respiration. The parameters analyzed in this group are:  $P_{LFn_{SC}}$ ,  $R_{SC}$  and  $\rho_{max}$ .
- Subset 4 (S4). HRV parameters derived from the Auto-Mutual Information Function analysis of HRV: the parameters analyzed in this group are:  $A_{T_{RR}}$ ,  $A_{T_{LF}}$ ,  $A_{T_{HF}}$ ,  $PD_{m_{LF}}$  and  $PD_{m_{HF}}$ .
- Subset 5 (S5). HRV parameters derived from the Auto-Mutual Information Function analysis of HRV and respiration: the parameters analyzed in this group are:  $A_{T_{SC}}$  and  $PD_{m_{SC}}$ .
- Subset 6 (S6). HRV parameters derived from the Cross-Mutual Information Function analysis of HRV: the parameters analyzed in this group are:  $CMIF_{0_{RR}}$ ,  $CMIF_{max_{RR}}$  and  $\tau_{max_{RR}}$ .
- Subset 7 (S7). HRV parameters derived from the Cross-Mutual Information Function analysis of HRV and respiration: the parameters analyzed in this group are:  $CMIF_{0_{SCHF}}$ ,  $CMIF_{max_{SC}}$  and  $\tau_{max_{SC}}$ .
- Subset 8 (S8). The best characteristics: those parameters which classify between the groups S1, S2, S3, S4, S5, S6 and S7.
- Subset 9 (S9). The best characteristics which only consider the HRV information: those parameters which classify between the groups S1, S2, S3, S4, S5, S6 and S7, but only take

into account the HRV information.

All these nine subsets have been performed into three analyzes attending to the elicitations considered as well as to the normalization of the HRV parameters. And within each analysis, two groups of elicitations (G1 = Group 1; G2 = Group 2) are analyzed as presented below, and are schematized in Table 5.2:

- Analysis 1: classification between relax and emotions which comprises: relax vs. all emotions, relax vs. positive valence (joy), relax vs. all negative valences (fear, sadness and anger), relax vs. fear, relax vs. sadness and relax vs. anger. In this analysis, HRV parameters were considered without any normalization.
- Analysis 2: classification between positive and negative valences and between negative valences which comprise positive valence (joy) vs. all negative valences (fear, sadness and anger), joy vs. fear, joy vs. sadness, joy vs. anger, fear vs. sadness, fear vs. anger and sadness vs. anger. In this analysis, HRV parameters were considered without any normalization.
- Analysis 3: classification between positive and negative valences and between negative valences. In this analysis, HRV parameters were normalized by their value during the relax session which preceded each emotion.

Table 5.2: Relationship between analyzes and groups of elicitations (G1 = Group 1; G2 = Group 2).

Analysis 1		Analysis 2		Analysis 3 (*)	
G1	G2	G1	G2	G1	G2
relax	all emotions	joy	all negative valences	joy	all negative valences
relax	joy	joy	fear	joy	fear
relax	all negative valences	joy	sadness	joy	sadness
relax	fear	joy	anger	joy	anger
relax	sadness	fear	sadness	fear	sadness
relax	anger	fear	anger	fear	anger
		sadness	anger	sadness	anger

(\*) HRV parameters were normalized by their value in the preceding relax session.

## 5.3 Results

In Table 5.3, 5.4 and 5.5, there are shown the number of comparison between each group (G1 for the first group and G2 for the second group), sensitivity, specificity, positive and negative predictive value and accuracy from the parameter set S1 to S9 when comparing between relax and emotions, between emotions and between emotions normalized by the basal condition, respectively.

It can be noted that when sensitivity, specificity and accuracy are all greater than 70% the results are remarked in bold type.

### 5.3.1 Evaluation of the analysis 1

Regarding the results obtained by the analysis 1 (Table 5.3), it can be observed that only the comparison between relax and joy can be classified by the set of parameters S8 with a sensitivity, sensitivity and accuracy greater than 80%. In the S8 analysis, it was considered the best classified characteristics derived from all set of parameters (i.e. S1, S2, S3, S4, S5, S6 and S7 analysis), therefore the resulting classified parameters are derived from the lineal and the non-linear analysis. The characteristics that classified relax vs. joy were:  $F_R$ ,  $F_{R_{FR}}$  and  $R_{SC}$  for linear analysis and  $A_{T_{SC}}$  and  $PD_{m_{HF}}$  for the non-linear analysis. It can be noted that all these parameters take into account the respiratory signal except  $PD_{m_{HF}}$ . However, it also accounts for the respiratory frequency band information.

### 5.3.2 Evaluation of the analysis 2

The results regarding the analysis 2 (Table 5.4) are presented by means of the comparisons between positive and negative valences or between negative valences. It can be observed that joy vs. fear

could be classified by the sets of parameters S5, S7 and S8, and joy vs. sadness and joy vs. anger by means of the set of parameters S7. It can be noted that the classified characteristics of the S5 and S7 analyzes are based in the SCHF methodology which take into account the respiratory signal information of each subject, and they are also derived from the non-linear methodology, the AMIF and the CMIF, respectively.

The characteristics which best classify joy and fear are:  $F_R$  derived from the linear analysis,  $PD_{m_{SC}}$  derived from the AMIF non-linear technique and considering the  $HF_{SC}$  band, and  $CMIF_{max_{SC}}$  derived from the CMIF non-linear technique and also considering the  $HF_{SC}$  band. The characteristic which best classify joy vs. sadness and joy vs. anger is  $CMIF_{max_{SC}}$ . Therefore, the common characteristic which classify among all these groups is  $CMIF_{max_{SC}}$ .

#### 5.3.3 Evaluation of the analysis 3

It can be observed that in Table 5.5 that positive vs. all negative valences, joy vs. fear, joy vs. sadness, joy vs. anger and fear vs. sadness can be all classified by the set of parameters S7, which is derived from the CMIF non-linear technique and also it considers the SCHF method, with a sensitivity, sensitivity and accuracy greater than 80%. It needs to be pointed out that both methodologies, the CMIF and the SCHF combined, consider the cardiorespiratory coupling between the HRV and respiratory signals. It can be observed that the characteristic able to classify between all these groups is the parameter  $CMIF_{max_{SC}}$ .

Each of the comparisons is analyzed in detail below. Related to the comparison between joy with all negative valences together (fear, sadness and anger) the best results are obtained from the sets of parameters S7, S8, and S9. The resulting classificatory characteristics are:  $CMIF_{max_{SC}}$  for S7;



$R$ ,  $F_{R_{F_R}}$ ,  $R_{F_R}$ ,  $\rho_{max}$  and  $CMIF_{max_{SC}}$  for S8; and  $R$  and  $PD_{m_{HF}}$  for S9. With regard to analyzing joy with each single negative valence, the results obtained are the following. About joy vs. fear, the best classificatory characteristics are derived from S3, S7, S8 and S9 analysis. The resulting classificatory characteristics are:  $\rho_{max}$  for S3;  $CMIF_{max_{SC}}$  for S7;  $F_R$  and  $CMIF_{max_{SC}}$  for S8; and  $R$  and  $PD_{m_{HF}}$  for S9. In respect of joy vs. sadness, the sets of characteristics which are good candidates to classify between both groups are  $\rho_{max}$  for S3;  $CMIF_{max_{SC}}$  for S7; and  $\rho_{max}$ ,  $A_{T_{LF}}$  and  $CMIF_{max_{SC}}$  for S8. As regard joy vs. anger, again the analysis S3, S7 and S8 presents the best set of characteristics which discriminates between both emotions as  $\rho_{max}$  for S3;  $CMIF_{max_{SC}}$  for S7; and  $\rho_{max}$ ,  $PD_{m_{LF}}$  and  $CMIF_{max_{SC}}$  for S8. Analyzing fear vs. sadness, it can be observed that only the S7 analysis can provide a classificatory characteristic:  $CMIF_{max_{SC}}$ .

Table 5.3: Classification results obtained by the analysis 1: number of comparison between group 1 (G1) and group 2 (G2), sensitivity, specificity, positive and negative predictive value, accuracy and characteristics classified from the analysis S1 to S9.

	S1		S2		S3		S4		S5		S6		S7		S8		S9	
	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2
Number of comparisons	88	153	79	136	71	112	88	153	71	112	88	153	71	112	71	112	88	153
Se(%) / Sp(%)	—	—	—	—	45.1	64.3	80.7	41.8	87.3	24.1	73.9	32.7	63.4	41.1	78.4	45.8	80.7	41.8
P+(%) / P-(%)	—	—	—	—	44.4	64.9	44.4	79.0	42.2	75.0	38.7	68.5	40.5	63.9	45.4	78.7	44.4	79.0
Acc(%)	—	—	—	—	56.8	—	56.0	—	48.6	—	47.7	—	49.7	—	57.7	—	56.0	—
Characteristics	—	—	—	—	$P_{FNSC}$	—	$A_{TIF}$	—	$A_{TSC}$	—	$CMIF_{0GR}$	—	$CMIF_{maxSC}$	—	$A_{TIF}$	—	$P_{LFNSC}, A_{TIF}$	—
Relax vs. Joy																		
Number of comparisons	88	36	79	25	71	13	88	36	71	13	88	36	71	13	71	13	88	36
Se(%) / Sp(%)	77.3	55.6	74.7	56.0	83.1	23.1	63.6	77.8	63.4	84.6	73.9	47.2	67.6	76.9	<b>81.7</b>	<b>84.6</b>	65.9	69.4
P+(%) / P-(%)	81.0	50.0	84.3	41.2	85.5	20.0	87.5	46.7	95.7	29.7	77.4	42.5	94.1	30.3	96.7	45.8	84.1	45.5
Acc(%)	71.0	—	70.2	—	73.8	—	67.7	—	66.7	—	66.1	—	69.0	—	<b>82.1</b>	—	66.9	—
Characteristics	$R, F_R$	—	$R_{FR}, F_{RFR}$	—	$R_{SC}$	—	$A_{TGR}, A_{TIF}, PD_{MHF}$	—	$A_{TSC}$	—	$CMIF_{maxGR}$	—	$CMIF_{maxSC}$	—	$F_R, F_{RFR}, R_{SC}, A_{TSC}, PD_{MHF}$	—	$R, PD_{MHF}$	—
Relax vs. all negative valences																		
Number of comparisons	88	117	79	111	71	99	88	117	71	99	88	117	71	99	88	117	88	117
Se(%) / Sp(%)	—	—	—	—	—	—	80.7	35.9	93.0	26.3	77.3	33.3	59.2	50.5	79.5	38.5	80.7	35.9
P+(%) / P-(%)	—	—	—	—	—	—	48.6	71.2	47.5	83.9	46.6	66.1	46.2	63.3	49.3	71.4	48.6	71.2
Acc(%)	—	—	—	—	—	—	55.1	—	54.1	—	52.2	—	54.1	—	56.1	—	55.1	—
Characteristics	—	—	—	—	—	—	$A_{TIF}$	—	$A_{TSC}$	—	$CMIF_{0GR}$	—	$CMIF_{0SC}, CMIF_{maxSC}$	—	$A_{TIF}$	—	$A_{TIF}$	—
Relax vs. Fear																		
Number of comparisons	88	46	79	45	71	41	88	46	71	41	88	46	71	41	71	41	88	46
Se(%) / Sp(%)	—	—	—	—	—	—	96.6	54.3	100.0	53.7	88.6	58.7	71.8	63.4	100.0	53.7	96.6	54.3
P+(%) / P-(%)	—	—	—	—	—	—	80.2	89.3	78.9	100.0	84.4	73.0	77.3	56.5	78.9	100.0	80.2	89.3
Acc(%)	—	—	—	—	—	—	82.1	—	83.0	—	78.4	—	68.8	—	83.0	—	82.1	—
Characteristics	—	—	—	—	—	—	$A_{TIF}$	—	$A_{TSCF}$	—	$CMIF_{0GR}$	—	$CMIF_{0SC}, CMIF_{maxSC}, \tau_{maxSC}, \tau_{maxHF}$	—	$A_{TSC}$	—	$A_{TIF}$	—
Relax vs. Sadness																		
Number of comparisons	88	34	79	32	71	28	88	34	71	28	88	34	71	28	—	—	—	—
Se(%) / Sp(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
P+(%) / P-(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Acc(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Characteristics	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Relax vs. Anger																		
Number of comparisons	88	37	79	34	71	30	88	37	71	30	88	37	71	30	71	30	71	30
Se(%) / Sp(%)	—	—	—	—	47.9	70.0	53.4	59.5	—	—	—	—	—	—	47.9	70.0	47.9	70.0
P+(%) / P-(%)	—	—	—	—	79.1	36.2	75.8	34.9	—	—	—	—	—	—	79.1	36.2	79.1	36.2
Percentage <sup>2</sup>	—	—	—	—	54.5	—	55.2	—	—	—	—	—	—	—	54.5	—	54.5	—
Characteristics	—	—	—	—	$P_{LFNSC}$	—	$PD_{MHF}$	—	—	—	—	—	—	—	$P_{LFNSC}, PD_{MHF}$	—	$P_{LFNSC}, PD_{MHF}$	—

It can be noted that when sensitivity, specificity and accuracy are all greater than 70% the results are remarked in bold type.

Table 5.4: Classification results obtained by the analysis 2: number of comparison between group 1 (G1) and group 2 (G2), sensitivity, specificity, positive and negative predictive value, accuracy and characteristics classified from the analysis S1 to S9.

	S1		S2		S3		S4		S5		S6		S7		S8		S9	
	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2
Positive valence vs. Negative valences																		
Number of comparisons	36	117	25	111	13	99	36	117	13	99	36	117	13	99	13	99	36	117
Se(%) / Sp(%)	58.3	83.8	56.0	77.5	23.1	83.8	80.6	59.8	100.0	29.3	77.8	33.3	76.9	65.7	69.2	88.9	61.1	70.9
P+(%) / P-(%)	52.5	86.7	35.9	86.7	15.8	89.2	38.2	90.9	15.7	100.0	26.4	83.0	22.7	95.6	45.0	95.7	39.3	85.6
Acc(%)	77.8		73.5		76.8		64.7		37.5		43.8		67.0		86.6		68.6	
Characteristics	$R, F_R$		$R_{F_R}, F_{R_R}$		$R_{SC}$		$A_{TIF}, PD_{mIF}$		$A_{TSC}$		$CMIF_{T0R}$		$CMIF_{maxSC}$		$F_R, R_{SC}, CMIF_{maxSC}$		$R, PD_{mIF}$	
Joy vs. Fear																		
Number of comparisons	36	46	25	45	13	41	36	46	13	41	36	46	13	41	13	41	36	46
Se(%) / Sp(%)	55.6	78.3	56.0	80.0	23.1	85.4	100.0	54.3	<b>92.3</b>	<b>75.6</b>	91.7	58.7	<b>84.6</b>	<b>75.6</b>	<b>86.6</b>	<b>85.4</b>	100.0	53.3
P+(%) / P-(%)	66.6	69.2	60.9	76.6	33.3	77.8	63.1	100.0	54.5	96.9	63.5	90.0	52.4	94.0	64.7	94.6	63.2	100.0
Acc(%)	68.3		71.4		70.4		74.4		<b>79.6</b>		73.2		<b>77.8</b>		<b>85.2</b>		74.4	
Characteristics	$P_{LFn}, F_R$		$R_{F_R}, F_{R_R}$		$R_{SC}$		$PD_{mIF}$		$PD_{nSC}$		$CMIF_{T0R}$		$CMIF_{maxSC}$		$F_R, CMIF_{maxSC}$		$PD_{mIF}$	
Joy vs. Sadness																		
Number of comparisons	36	35	25	32	13	28	36	34	13	28	36	34	13	28	13	28	36	34
Se(%) / Sp(%)	58.3	91.1	—	—	—	—	61.1	64.4	76.9	60.7	—	—	<b>76.9</b>	<b>75.0</b>	53.8	92.9	50.0	85.3
P+(%) / P-(%)	87.5	67.4	—	—	—	—	64.7	61.1	47.6	85.0	—	—	58.8	87.5	77.8	81.3	78.3	61.7
Acc(%)	74.3		—	—	—	—	62.9		65.9		—	—	<b>75.6</b>		80.5		67.1	
Characteristics	$R, F_R$		—	—	—	—	$A_{TIF}$		$A_{TSC}$		—	—	$CMIF_{maxSC}$		$R, F_R, A_{TSC}$		$R$	
Joy vs. Anger																		
Number of comparisons	36	37	25	34	13	30	36	37	13	30	36	37	13	30	13	30	36	37
Se(%) / Sp(%)	52.8	75.7	—	—	—	—	58.3	62.2	76.9	56.7	—	—	<b>76.9</b>	<b>70.0</b>	61.5	76.7	58.3	62.2
P+(%) / P-(%)	67.9	62.2	—	—	—	—	60.0	60.5	43.5	85.0	—	—	52.6	87.5	53.3	82.1	60.0	60.5
Acc(%)	64.4		—	—	—	—	60.3		62.8		—	—	<b>72.1</b>		72.1		60.3	
Characteristics	$F_R$		—	—	—	—	$A_{TIF}$		$A_{TSC}$		—	—	$CMIF_{maxSC}$		$F_R, A_{TSC}$		$A_{TIF}$	
Fear vs. Sadness																		
Number of comparisons	46	34	45	32	41	28	46	34	41	28	46	34	41	28	41	28	46	34
Se(%) / Sp(%)	—	—	—	—	—	—	54.3	97.1	53.7	100.0	58.7	88.2	68.3	75.0	53.7	100.0	54.3	97.1
P+(%) / P-(%)	—	—	—	—	—	—	96.2	61.1	100.0	59.6	87.1	61.2	80.0	61.8	100.0	59.6	96.2	61.1
Acc(%)	—	—	—	—	—	—	72.5		72.5		71.3		71.0		72.5		72.5	
Characteristics	—	—	—	—	—	—	$A_{TIF}$		$A_{TSC}$		$CMIF_{T0R}$		$CMIF_{maxSC}$		$A_{TSC}$		$A_{TIF}$	
Fear vs. Anger																		
Number of comparisons	46	37	45	34	41	30	46	37	41	30	46	37	41	30	41	30	46	37
Se(%) / Sp(%)	50.0	64.9	—	—	—	—	60.9	97.3	53.7	96.7	58.7	94.6	68.3	80.0	53.7	96.7	58.7	94.6
P+(%) / P-(%)	63.9	51.1	—	—	—	—	96.6	66.7	95.6	60.4	93.1	64.8	82.4	64.9	95.7	60.4	93.1	64.8
Acc(%)	56.6		—	—	—	—	77.1		71.8		74.7		73.2		71.8		74.7	
Characteristics	$P_{LFn}$		—	—	—	—	$A_{TIF}$		$A_{TSC}$		$CMIF_{T0R}$		$CMIF_{maxSC}$		$A_{TSC}$		$P_{LFn}, A_{TIF}$	
Sadness vs. Anger																		
Number of comparisons	34	37	32	34	28	30	34	37	28	30	34	37	28	30	—	—	—	—
Se(%) / Sp(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
P+(%) / P-(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Acc(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Characteristics	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—

It can be noted that when sensitivity, specificity and accuracy are all greater than 70% the results are remarked in bold type.

Table 5.5: Classification results obtained by the analysis 3: number of comparison between group 1 (G1) and group 2 (G2), sensitivity, specificity, positive and negative predictive value, accuracy and characteristics classified from the analysis S1 to S9.

	S1		S2		S3		S4		S5		S6		S7		S8		S9	
	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2	G1	G2
Positive valence vs. Negative valences																		
Number of comparisons	35	107	23	94	12	81	35	107	12	81	35	107	12	81	12	81	35	107
Se(%) / Sp(%)	57.1	91.6	52.2	85.1	66.7	91.4	60.0	71.0	66.7	60.5	—	—	83.0	<b>79.0</b>	<b>83.3</b>	<b>85.2</b>	<b>71.4</b>	<b>73.8</b>
P+(%) / P-(%)	69.0	86.7	46.2	87.9	53.5	94.9	40.4	84.4	20.0	92.5	—	—	37.0	97.0	45.5	97.2	47.2	88.8
Acc(%)	83.1	—	78.6	—	88.2	—	68.3	—	61.3	—	—	—	<b>79.6</b>	—	<b>84.9</b>	—	<b>73.2</b>	—
Characteristics	$R, F_k$	$R_{F_k}, F_{R_{F_k}}$	$R_{SC}, \rho_{max}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Joy vs. Fear																		
Number of comparisons	35	43	23	38	12	33	35	43	12	33	35	43	12	33	12	33	35	43
Se(%) / Sp(%)	57.1	88.4	52.2	84.2	<b>75.0</b>	<b>81.8</b>	94.3	51.2	100.0	54.5	91.4	53.5	<b>91.7</b>	<b>81.8</b>	<b>75.0</b>	<b>78.8</b>	<b>85.7</b>	<b>70.0</b>
P+(%) / P-(%)	80.0	71.7	66.7	74.4	60.0	90.0	61.1	91.7	44.4	100.0	61.5	88.5	64.7	96.4	56.3	89.7	69.8	85.7
Acc(%)	74.4	—	72.1	—	<b>80.0</b>	—	70.5	—	66.7	—	70.5	—	<b>84.4</b>	—	<b>71.8</b>	—	<b>76.9</b>	—
Characteristics	$R, F_k$	$R_{F_k}, F_{R_{F_k}}$	$\rho_{max}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Joy vs. Sadness																		
Number of comparisons	35	30	23	27	12	22	35	30	12	22	35	30	12	22	12	22	35	30
Se(%) / Sp(%)	60.0	96.7	—	—	<b>83.3</b>	<b>77.3</b>	65.7	73.3	66.7	77.3	—	—	<b>75.0</b>	<b>72.7</b>	<b>100.0</b>	<b>77.3</b>	68.6	83.3
P+(%) / P-(%)	95.5	67.4	—	—	66.7	89.5	74.2	64.7	61.5	81.0	—	—	60.0	84.2	70.6	100.0	82.8	69.4
Acc(%)	76.9	—	—	—	<b>79.4</b>	—	69.2	—	73.5	—	—	—	<b>73.5</b>	—	<b>85.3</b>	—	75.4	—
Characteristics	$R, F_k$	$R_{F_k}, F_{R_{F_k}}$	$\rho_{max}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Joy vs. Anger																		
Number of comparisons	35	34	23	29	12	26	35	34	12	26	35	34	12	26	12	26	35	34
Se(%) / Sp(%)	54.3	79.4	—	—	<b>83.3</b>	<b>80.8</b>	60.0	73.5	66.7	73.1	57.1	52.9	<b>75.0</b>	<b>84.6</b>	<b>83.3</b>	<b>84.6</b>	60.0	73.5
P+(%) / P-(%)	73.1	62.8	—	—	66.7	91.3	70.0	64.1	53.3	82.6	55.6	54.5	69.2	88.0	71.4	91.7	70.0	64.1
Acc(%)	66.7	—	—	—	<b>81.6</b>	—	66.7	—	71.1	—	55.1	—	<b>81.6</b>	—	<b>84.2</b>	—	66.7	—
Characteristics	$P_{F_{F_k}}, F_{R_{F_k}}$	$\rho_{max}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Fear vs. Sadness																		
Number of comparisons	43	30	38	27	33	22	43	30	33	22	43	30	33	22	33	22	43	30
Se(%) / Sp(%)	—	—	—	—	—	—	51.2	100.0	54.5	100.0	53.5	93.3	<b>70.0</b>	<b>77.3</b>	54.5	100.0	51.2	48.8
P+(%) / P-(%)	—	—	—	—	—	—	100.0	58.8	100.0	59.5	92.0	58.3	82.1	63.0	100.0	59.5	100.0	58.8
Acc(%)	—	—	—	—	—	—	71.2	—	72.7	—	69.9	—	<b>72.7</b>	—	72.7	—	71.2	—
Characteristics	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Fear vs. Anger																		
Number of comparisons	43	34	38	29	33	26	43	34	33	26	43	34	33	26	33	26	43	34
Se(%) / Sp(%)	—	—	—	—	—	—	58.1	100.0	54.5	96.2	53.5	100.0	66.7	76.9	54.5	96.2	58.1	100.0
P+(%) / P-(%)	—	—	—	—	—	—	100.0	65.4	94.7	62.5	100.0	63.0	78.6	64.5	94.7	62.5	100.0	65.4
Acc(%)	—	—	—	—	—	—	76.6	—	72.9	—	74.0	—	71.2	—	72.9	—	76.6	—
Characteristics	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$
Sadness vs. Anger																		
Number of comparisons	30	34	27	29	22	26	30	34	22	26	30	34	22	26	—	—	—	—
Se(%) / Sp(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
P+(%) / P-(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Acc(%)	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—	—
Characteristics	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$	$A_{T_{F_k}}, PD_{m_{F_k}}$

It can be noted that when sensitivity, specificity and accuracy are all greater than 70% the results are remarked in bold type.

## 5.4 Discussion

The results derived from the three analyzes have been evaluated as shown below.

Regarding the results obtained by the analysis 1 (Table 5.3), it can be observed that only the comparison between relax and joy permits good classifications of the subjects by means of the characteristics:

$F_R$ ,  $F_{R_{FR}}$ ,  $R_{SC}$ ,  $A_{T_{SC}}$  and  $PD_{m_{HF}}$ . Comparing these results with the linear analysis exposed in chapter 3, the statistics of the parameter  $R_{SC}$  are in concordance with the ones presented in chapter 3 where it was obtained that a  $p$ -value  $\leq 0.05$  and sensitivity, specificity and accuracy  $\geq 70\%$  and AUC index  $\geq 0.70$ . By another hand, the parameters  $F_R$  and  $F_{R_{FR}}$  did not show significant statistical differences between this pair of elicitations but could classify as part of the parameter set S8. In addition, as in this classification analysis, no linear parameters were able to discriminate between relax and negative valences. In the non-linear analysis, exposed in chapter 4, among all parameters that presented statistically significant differences between relax and joy,  $A_{T_{SC}}$  and  $PD_{m_{HF}}$  both resulted in a  $p$ -value  $\leq 0.01$  and sensitivity, specificity and accuracy  $\geq 70\%$  and AUC index  $\geq 0.70$ . Furthermore, by means of the non-linear analysis, it was possible to extract parameters which differentiated between relax and fear.

Although in [61], different classifier methods are used compared to the ones applied in this work, it could be observed a classification rate of 92% among the basal state of neutrality against amusement, contentment, disgust, fear or sadness.

Regarding the results obtained by the analysis 2 (Table 5.4), it can be observed that subjects comparing joy vs. fear, joy vs. sadness and joy vs. anger can be classified with a common characteristic:

$CMIF_{max_{SC}}$ . Comparing these results with the non-linear analysis, exposed in chapter 4,  $CMIF_{max_{SC}}$

resulted in a  $p$ -value  $\leq 0.001$ , sensitivity and specificity  $\geq 70\%$ , accuracy  $\geq 85\%$  and AUC index  $\geq 0.95$  for joy vs. fear. In addition, the parameter  $CMIF_{max_{SC}}$  resulted in a  $p$ -value  $\leq 0.01$ , sensitivity and specificity  $\geq 70\%$ , accuracy  $\geq 75\%$  and AUC index  $\geq 0.77$  for joy vs. sadness and joy vs. anger.

The results regarding the analysis 3 are presented in Table 5.5 which shows that subjects can be well classified when positives vs. all negative valences, joy vs. fear, joy vs. sadness, joy vs. anger and fear vs. sadness are studied.

It can be observed that the parameter  $CMIF_{max_{SC}}$ , which considers the non-linear coupling between the HRV and the respiratory information in a HF band redefined by the SCHF method, is the recurrent characteristic that appear in all classifications between positive and all negative valences together, between joy and each single negative valence and between fear and sadness. Another interesting parameter to be mentioned is  $\rho_{max}$ , due to it was able to classify between joy vs. all negative valences, joy vs. fear, joy vs. sadness and joy vs. anger. It can be noted that  $\rho_{max}$  also takes into account the common information between HRV and respiration.

Unfortunately, it is difficult to make comparisons between these results and the studies found in the bibliography because all differ on the database recording criteria that directly affect on the classification accuracy as happens with the number of participants, the emotion elicitation, the duration of the affective elicitation, the signals recorded and the classifier method [23]. Nonetheless, in Table 5.1 it has reported studies close to the study developed in this thesis, that have taken into account HRV signals with visual or music elicitation, although with an elicitation with smaller duration or with different size database used. In [108], the same classifier technique than in the present thesis was performed to discriminate among joy, anger, sadness and pleasure with an overall result of

92.1%. In the present thesis, the percentage of original grouped cases correctly classified obtained comparing joy and all negative valences together was 84.9%, for joy vs. fear it was 84.4%, for joy vs. sadness it was 85.3%, for joy vs. anger it was 84.2% and fear vs. sadness it was 72.7%. Although [51, 54, 60, 61] used different classifier methods than those used in the present thesis, it could be observed that the best results are obtained for those studies which considered positive and negative valences, as it was reported here.

In some studies, more sophisticated methodologies have been used which have managed to improve the classification results in front of the linear methods. However, in [108], a linear methodology LDF has been used to distinguish between human emotions and it has offered a better result than the more sophisticated methodologies. This fact supports the choice of using a linear classifier to analyze between groups of human emotions.

There are some limitations to note regarding the classificatory study. The use of a linear classifier which is based on LDF makes results not optimal, since the features do not follow the assumption of normality and they are not independent. In addition, the sample size database used is small, together with there are many emotions to classify and a high variability in the signals. Due to this, it has been selected a LDF algorithm in order to avoid an overtraining which could lead to a positive bias of the result and to avoid a size reduction of the analyzed subject subset.

The results extracted from this chapter suggest that although the analysis based on the analysis 2 has been able to obtain characteristics that classify between joy vs. fear, joy vs. sadness and joy vs. anger, the results obtained by the analysis 3 may be more reliable since it considers the emotions normalized by their baseline state and therefore eliminates the variability that these signals present. Furthermore, to take into account the relationship between the HRV and the respiratory

#### 5.4. DISCUSSION

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information combined with lineal and non-lineal methodologies increases the reliability for human emotion recognition.



## Chapter 6

# Conclusions

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Interest in emotion recognition has increased in recent years as a useful tool for diagnosing psycho-neural illnesses. In this dissertation, linear and non-linear methods based on the analysis of HRV were proposed for human emotion recognition.

For the linear analysis methodology, it was proposed the joint analysis of HRV and respiration to improve human emotion characterization. With this purpose, the HF band was defined based on the maximum spectral correlation between HRV and respiration. The  $\rho_{max}$  itself was proposed as an index to identify emotions. The hypothesis was that this index could add relevant information to HRV analysis to describe human emotions.

Regarding to the non-linear analysis methodologies, the AMIF technique was applied to HRV signals to study complex interdependencies, and the CMIF technique was considered to quantify the complex coupling between HRV and respiratory signals. Both algorithms were adapted to short term RR time series. Traditional band pass filtering was applied to the RR series at LF and HF band, and also the redefined HF based on the maximum spectral correlation between HRV and respiration was investigated. Both the AMIF and the CMIF algorithms were calculated with regard to different time scales as specific complexity measures.

The ability of the parameters derived from the linear and non-linear techniques was evaluated on the database of video-induced emotion elicitation.

### 6.1 Conclusions for linear analysis methodology

In chapter 3, human emotion recognition was assessed by HRV analysis. To increase the reliability of HRV measurements, a novel methodology based on spectral correlation of HRV signal and

respiration was proposed.

The new proposed method, the Spectrum Correlation for High Frequency band, revealed an improvement in the reliability for sympathovagal balance estimation capable of discriminating between relax vs. joy, joy vs. each of the negative valences and fear vs. sadness.

This method provided the novel index,  $\rho_{max}$ , which offers additional information for emotion recognition, based on the relationship between HRV and respiration.

## **6.2 Conclusions for non-linear analysis methodology**

The results extracted from chapter 4 suggested that the non-linear AMIF and the CMIF techniques characterized the negative valence of fear, by reflecting a lower complexity than the other emotions. Parameters derived from the AMIF allowed extending the description of the complexity of vagal and sympathetic autonomic rhythms. Parameters derived from the CMIF at the respiration-based bandwidth provided relevant information related to non-linear mechanisms between vagal and respiratory activity, especially for fear.

Furthermore, filtering the HRV signals into a redefined HF band provided a better discrimination for parameters derived from the AMIF between relax and joy, relax and fear, joy and all remaining emotion conditions as well as fear and all remaining emotion conditions.

The non-linear AMIF and CMIF techniques provided complementary information to other linear and non-linear methods.

### 6.3 Conclusions for the cluster analysis

The results extracted from chapter 5 suggested that relax vs. joy, positive vs. all negative valences, joy vs. fear, joy vs. sadness, joy vs. anger and fear vs. sadness can be all classified.

Although the analysis based on the analysis 2 has been able to obtain characteristics that classify between joy vs. fear, joy vs. sadness and joy vs. anger, the results obtained by the analysis 3 may be more reliable since it considers the emotions normalized by their baseline state and therefore eliminates the variability that these signals present.

The parameter  $CMIF_{max_{SC}}$ , which considers the non-linear coupling between the HRV and the respiratory signal information in a HF band redefined by the SCHF method, is the recurrent characteristic that appear in all classifications between positive and all negative valences together, and between joy and each single negative valence. Another interesting parameter to be mentioned is  $\rho_{max}$ , since it was able to classify between joy vs. all negative valences, joy vs. sadness and anger. It can be noted that  $\rho_{max}$  also take into account the common information between HRV and respiration.

### 6.4 Future extensions

The current clinical practice for diagnosing patients affected by psychological or psychiatric disorders is based solely on verbal interviews and on specific questionnaire scores, and there are no reliable and objective psychophysiological markers that are taken into account. For these reason, the characterization of emotional patterns can have an impact in the treatment of certain psychological pathologies.

In future works, it will be proposed to implement the algorithms and indices derived from this re-

search within a hardware like a biomedical equipment, an app or a remote server which sends the signal to a health professional to be analyzed. This tool opens the door to help in identifying emotional behaviors in people suffering from mental pathologies. However, further studies are needed to test the validity and reliability of the proposed index outside laboratory settings.

Another future extension to be considered is the outpatient monitoring, which consist on tracking changes in the health status of patients outside the classical hospital environment. Outpatient monitoring might be crucial after surgery, heart failure, diabetes, mental illness, among others to monitor emergency patients before they arrive at the hospital. This enables to improve the care patients receive and also their diagnosis.

For these reason, the algorithms and indices derived from this research could be implemented on mobile devices which record and transmit medical data, being a low cost and easy solution to obtain continuous and long term dynamic physiological data. This tool could provide an intelligent monitoring of outpatient individuals with mental illnesses with the purpose of designing individualized therapies. The importance of monitoring by means of an ambulatory system, individuals with depression or anxiety, between other mental illness, comes from the fact that it could alert during or before emergency crisis and also, it could maintain their attention on modulating their emotional responses.

In addition, analyzing the role of mutual information-based HRV measures to explore a multi-variable approach combining with other non-linear parameters could open a door to extract new suitable parameters for emotion recognition.

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## Chapter 7

# Conclusiones

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El interés en el reconocimiento de emociones ha aumentado en los últimos años por ser una herramienta útil para diagnosticar enfermedades psico-neurales. En esta disertación se han propuesto métodos basados en análisis lineales y no lineales para analizar la variabilidad del ritmo cardíaco con la finalidad de reconocer emociones humanas.

Para el análisis lineal se propuso analizar conjuntamente la variabilidad del ritmo cardíaco y la respiración para así mejorar la caracterización de las emociones humanas. Con este propósito, la banda de alta frecuencia se definió mediante la correlación espectral máxima entre la variabilidad del ritmo cardíaco y la respiración. Además,  $\rho_{max}$  fue propuesta como un índice para identificar emociones, con la hipótesis de que este índice podría agregar información relevante al análisis de la variabilidad del ritmo cardíaco para describir las emociones humanas.

Con respecto al análisis no lineal, la Función de Auto Información Mutua se aplicó a las señales de variabilidad del ritmo cardíaco para estudiar las interdependencias complejas, y se consideró la Función de Información Mutua Cruzada para cuantificar el acoplamiento complejo entre la variabilidad del ritmo cardíaco y las señales respiratorias. Ambos algoritmos se adaptaron a series temporales RR de corta duración. Se aplicó un filtro pasabanda tradicional a la serie RR en las bandas de baja y alta frecuencia, y también se investigó la banda de alta frecuencia redefinida según la correlación espectral máxima entre la variabilidad del ritmo cardíaco y la respiración. Los algoritmos de la Función de Auto Información Mutua y de la Función de Información Mutua Cruzada se calcularon con respecto a diferentes escalas de tiempo como medidas de complejidad específicas.

Se evaluó la capacidad de los parámetros derivados de las técnicas lineales y no lineales en la base de datos de emociones inducidas mediante videos.

### 7.1 Conclusiones del análisis lineal

En el capítulo 3, se evaluó el reconocimiento de emociones humanas mediante el análisis de variabilidad del ritmo cardíaco. Para aumentar la fiabilidad de las mediciones de variabilidad del ritmo cardíaco, se propuso una nueva metodología basada en la correlación espectral máxima entre la señal de variabilidad del ritmo cardíaco y la respiración.

Este nuevo método propuesto, la correlación espectral en la banda de alta frecuencia, mejoró la estimación del equilibrio simpaticovagal capaz de discriminar entre la relajación versus alegría, alegría versus cada una de las valencias negativas y miedo versus tristeza.

Además este método proporcionó un nuevo parámetro,  $\rho_{max}$ , que ofrece información adicional para el reconocimiento de emociones, basado en la relación entre la variabilidad del ritmo cardíaco y la respiración.

### 7.2 Conclusiones del análisis no lineal

Los resultados extraídos del capítulo 4 sugirieron que las técnicas no lineales Función de Auto Información Mutua y Función de Información Mutua Cruzada caracterizan la valencia negativa del miedo, al reflejar una menor complejidad que las otras emociones. Los parámetros derivados de la Función de Auto Información Mutua permitieron ampliar la descripción de la complejidad de los ritmos autónomos vagales y simpáticos. Los parámetros derivados de la Función de Información Mutua Cruzada en la banda de alta frecuencia basada en la respiración proporcionaron información relevante relacionada con mecanismos no lineales entre la actividad vagal y respiratoria, especialmente para el miedo.



Además, filtrar las señales de variabilidad del ritmo cardíaco en una banda de alta frecuencia redefinida proporcionó una mejor discriminación de los parámetros derivados de la Función de Auto Información Mutua entre relajación y alegría, relajación y miedo, alegría y todas las condiciones emocionales restantes, así como el miedo y todas las condiciones emocionales restantes.

Las técnicas no lineales Función de Auto Información Mutua y Función de Información Mutua Cruzada proporcionaron información complementaria a otros métodos lineales y no lineales.

### 7.3 Conclusiones del análisis de clasificación

Los resultados extraídos del capítulo 5 sugirieron que ha sido posible clasificar relajación versus alegría, alegría versus todas las valencias negativas juntas, alegría versus miedo, alegría versus tristeza, alegría versus ira y miedo versus tristeza.

Si bien el estudio basado en el análisis 2 ha podido obtener características que clasifican entre alegría versus miedo, alegría versus tristeza, alegría versus ira, los resultados obtenidos por el análisis 3 puede ser más confiable ya que considera las emociones normalizadas por su estado basal y, por lo tanto, elimina la variabilidad que presentan estas señales.

El parámetro  $CMIF_{max_{SC}}$ , que considera el acoplamiento no lineal entre la variabilidad del ritmo cardíaco y la información respiratoria en una banda de alta frecuencia redefinida por el método SCHF, ha sido una característica recurrente que aparece en todas las clasificaciones entre alegría versus todas las valencias negativas juntas, entre alegría versus cada valencia negativa individual, y entre miedo versus tristeza. Otro parámetro interesante a mencionar es  $\rho_{max}$ , ya que ha sido capaz de clasificar entre alegría versus miedo, alegría versus tristeza y alegría versus ira. Cabe señalar

que  $\rho_{max}$  también tiene en cuenta la información común entre la variabilidad del ritmo cardíaco y la respiración.

### 7.4 Extensiones futuras

La práctica clínica actual para diagnosticar pacientes afectados por trastornos psicológicos o psiquiátricos se basa únicamente en entrevistas verbales y en puntajes de cuestionarios específicos, y no hay marcadores psicofisiológicos adecuados y objetivos que se tengan en cuenta. Por esta razón, la caracterización de los patrones emocionales puede tener un impacto en el tratamiento de ciertas patologías psicológicas.

En trabajos futuros, se propondrá implementar los algoritmos y parámetros derivados de esta investigación dentro de un hardware como por ejemplo puede ser un equipo biomédico, una aplicación o un servidor remoto que envíe la señal a un profesional de la salud para su posterior análisis. Esta herramienta abre la puerta para ayudar a identificar comportamientos emocionales en personas que sufren patologías mentales. Sin embargo, se necesitan más estudios para probar la validez y confiabilidad de los parámetros propuestos fuera de los entornos de laboratorio.

Otra extensión futura a considerar es la monitorización ambulatoria, que consiste en rastrear los cambios en el estado de salud de los pacientes fuera del entorno hospitalario clásico. El monitoreo ambulatorio puede ser crucial después de una cirugía, insuficiencia cardíaca, diabetes, enfermedades mentales, entre otros, para monitorear a los pacientes ante una emergencia antes de llegar al hospital. Esto permite mejorar la atención que reciben los pacientes y también su diagnóstico.

Por esta razón, los algoritmos y parámetros derivados de esta investigación podrían implementarse

en dispositivos móviles que registran y transmiten datos médicos, siendo una solución fácil y de bajo coste para obtener datos fisiológicos dinámicos continuos y a largo plazo. Esta herramienta podría proporcionar un monitoreo inteligente de pacientes ambulatorios con enfermedades mentales con el propósito de diseñar terapias individualizadas. La importancia del monitoreo por medio de un sistema ambulatorio a individuos con depresión o con ansiedad, entre otras enfermedades mentales, viene del hecho de que podría alertar durante o antes de una crisis de emergencia y también, podría mantener su atención en la modulación de sus respuestas emocionales.

Además, analizar el papel de las medidas de variabilidad del ritmo cardíaco basadas en la información mutua para explorar un enfoque de múltiples variables que se combina con otros parámetros no lineales podría abrir una puerta para extraer nuevos parámetros adecuados para el reconocimiento de emociones.

# Chapter 8

# Appendix

## Contents

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## 8.1 Scientific contributions

The methodologies and results presented in this dissertation and elaborated during my PhD studies have been published in the following works.

### International Journals:

- [101] Valderas, M.T., Bolea, J., Orini, M., Laguna, P., Orrite, C., Vallverdú, M. and Bailón, R., Human emotion characterization by heart rate variability analysis guided by respiration, *IEEE Journal of Biomedical and Health Informatics*, 2019, DOI: 10.1109/JBHI.2019.2895589.
- [99] Valderas, M.T., Bolea, J., Laguna, P., Bailón, R. and Vallverdú, M., Mutual information between heart rate variability and respiration for emotion characterization, *Physiological Measurements*, Volume 40, Number 8, 2019, DOI: 10.1088/1361-6579/ab310a.

### International conferences:

- [100] Valderas, M.T., Bolea, J., Laguna, P., Vallverdú, M. and Bailón, R., Human emotion recognition using heart rate variability analysis with spectral bands based on respiration, *37th International Conference on IEEE EMBS International Conference on Engineering in Medicine and Biology Society*, 2015, 6674-6677, DOI: 10.1109/EMBC.2015.7319792.

## 8.2 Acronyms

In this section a glossary with the most used abbreviations and parameters, with nomenclature and definition, is presented.

### 8.2.1 List of abbreviations

- $\mu$ : mean.
- $\sigma$ : standard deviation.
- A: anger.
- AMIF: Auto-Mutual Information Function.
- ANN: Artificial Neural Networks.
- ANOVA: analysis of variance.
- ANS: autonomic nervous system.
- ApEn: Approximate Entropy.
- ARMA model: time-varying autoregressive moving average model.
- AUC: receiver operating characteristic curve.
- BNE: Basic Negative Emotion.
- BP: blood pressure.
- bpm: beats per minute.
- BPE: Basic Positive Emotion.
- CFME<sub>n</sub>: Cross Fuzzy Measure Entropy.
- CMIF: Cross-Mutual Information Function.
- CSE<sub>n</sub>: Cross Sample Entropy.
- DFA: Detrended Fluctuation Analysis.

- DLEs: Dominant Lyapunov Exponents (DLEs).
- ECG: electrocardiography.
- EEG: electroencephalography.
- F: fear.
- FD: Fisher Discriminant.
- FMEn: Fuzzy Measure Entropy.
- GSR: galvanic skin response.
- HF: high frequency.
- $HF_{F_R}$ : shifted HF band centered at  $F_R$  with fixed bandwidth.
- $HF_{SC}$ : redefined HF band based in the Spectrum Correlation HF method.
- HRV: heart rate variability.
- IPFM model: integral pulse frequency modulation model.
- J: joy.
- kNN: k-Nearest Neighbour.
- LDF: Linear Discriminant Function.
- LF: low frequency.
- LLP: Lagged Poincaré Plot.
- MBP: Marquardt Backpropagation.
- MP: Multilayer Perceptron.

- MRE: mean relative error.
- NFS: Neuro-Fuzzy System.
- PANAS-X: the Positive and Negative Affect Schedule - Expanded Form.
- PD2: Pointwise Correlation Dimension.
- PE: Permutation Entropy.
- PME: Permutation Min-Entropy.
- PSD: power spectrum density.
- Q1: interquartile ranges in the first quartile.
- Q3: interquartile ranges in the third quartile.
- R: relax.
- RF: Random Forests.
- RSA: respiratory sinus arrhythmia.
- S: sadness.
- SA node: sinoatrial node.
- SCHF method: Spectrum Correlation HF method.
- SEn: Sample Entropy.
- ST: skin temperature variation.
- SVM: Support Vector Machines.
- ULF: ultra low frequency.



- VLF: very low frequency.

### 8.2.2 List of parameters

- $\rho_{max}$ : maximum spectral correlation between HRV and respiration.
- $\tau$ : prediction time or time lag of the AMIF or the CMIF.
- $\tau_a$ : lower-time scale boundary corresponding to the SCHF prediction time range.
- $\tau_b$ : upper-time scale boundary corresponding to the SCHF prediction time range.
- $\tau_{maxRR}$ : time lag between  $CMIF_{max}$  and  $CMIF_0$  studied in the  $RR(t)$  series.
- $\tau_{maxSC}$ : time lag between  $CMIF_{max}$  and  $CMIF_0$  studied in the  $(RR_{SC}(t))$ , which is the  $RR(t)$  series filtered in the  $HF_{SC}$  band.
- $\Delta HF$ : distance between the lower and the upper limit of the  $HF_{SC}$  band.
- $\Lambda$ : Wilks's Lambda.
- $a_{max}$ : lower limit of the  $HF_{SC}$  band.
- $A_{T_{RR}}$ : total area under the curve  $RR(t)$  series.
- $A_{T_{LF}}$ : total area under the curve  $RR_{LF}(t)$  series.
- $A_{T_{HF}}$ : total area under the curve  $RR_{HF}(t)$  series.
- $A_{T_{SC}}$ : total area under the curve  $RR_{SC}(t)$  series.
- Acc: accuracy.
- $b_{max}$ : upper limit of the  $HF_{SC}$  band.

- $BD$ : beat decay.
- $CMIF_{0_{RR}}$ : CMIF value at  $\tau = 0$  of the  $RR(t)$  series.
- $CMIF_{0_{SC}}$ : CMIF value at  $\tau = 0$  of the  $RR_{SC}(t)$  series.
- $CMIF_{max_{RR}}$ : maximum CMIF value of the  $RR(t)$  series.
- $CMIF_{max_{SC}}$ : maximum CMIF value of the  $RR_{SC}(t)$  series.
- $d_{HR}(t)$ : instantaneous heart rate.
- $d_{HRM}(t)$ : time-varying mean heart rate.
- $\overline{d_{HRM}}$ : mean of  $d_{HRM}(t)$ .
- $F_R$ : respiratory frequency.
- $F_{R_{F_R}}$ : respiratory frequency of the recordings which accomplishes the restriction of  $F_R \geq 0.10$  Hz.
- $F_{R_{SC}}$ : respiratory frequency of the recordings which accomplishes all the restrictions imposed in Section 3.2.2 *Frequency band definition*.
- FN: false negatives.
- FP: false positives.
- $H_{x(t)}$ : Shannon entropy.
- $I$ : Number of bins.
- $m(t)$ : modulating signal.
- P-: negative predictive value.

- $P_+$ : positive predictive value.
- $P_{HF}$ : power content in the HF band.
- $P_{HF_{F_R}}$ : power content in the  $HF_{F_R}$  band.
- $P_{HF_{S_C}}$ : power content in the  $HF_{S_C}$  band.
- $P_{LF}$ : power content in the LF band.
- $P_{LF_n}$ : normalized power in the LF band.
- $P_{LF_{n_{F_R}}}$ : normalized power in the LF band considering the  $HF_{F_R}$  band.
- $P_{LF_{n_{S_C}}}$ : normalized power in the LF band considering the  $HF_{S_C}$  band.
- $PD$ : Peak decay.
- $PD_m$ : mean peak decay.
- $PD_{m_{LF}}$ : mean peak decay of the  $RR_{LF}(t)$  series.
- $PD_{m_{HF}}$ : mean peak decay of the  $RR_{HF}(t)$  series.
- $PD_{m_{S_C}}$ : mean peak decay of the  $RR_{S_C}(t)$  series.
- $r(t)$ : respiratory signal.
- $R$ : ratio LF/HF.
- $R_{F_R}$ : ratio LF/ $HF_{F_R}$ .
- $R_{S_C}$ : ratio LF/ $HF_{S_C}$ .
- $RR(t)$ : RR time series.
- $RR_{LF}(t)$ :  $RR(t)$  series filtered in the LF band.

- $RR_{HF}(t)$ :  $RR(t)$  series filtered in the HF band.
- $RR_{SC}(t)$ :  $RR(t)$  series filtered in the  $HF_{SC}$  band.
- Se: sensitivity.
- Sp: specificity.
- $S_{attentiveness}$ : attentiveness scale.
- $S_{fatigue}$ : fatigue scale.
- $S_{fear}$ : fear scale.
- $S_{guilt}$ : guilt scale.
- $S_{hostility}$ : hostility scale.
- $S_{joviality}$ : joviality scale.
- $S_{sadness}$ : sadness scale.
- $S_{self-assurance\ scale}$ : self-assurance scale.
- $S_{serenity}$ : serenity scale.
- $S_{shyness}$ : shyness scale.
- $S_m(f)$ : power spectrum density of  $m(t)$ .
- $S_r(f)$ : power spectrum density of  $r(t)$ .
- $S_{surprise}$ : surprise scale.
- TN: true negatives.
- TP: true positive.



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