

1 Development and validation of a computational model
2 for steak double-sided pan cooking

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10 **Abstract**

The objective of this study was to develop and validate a numerical model to adequately simulate the double-sided pan cooking of beef in a domestic environment. The proposed model takes into account the heat flow from the pan to the meat and the moisture transfer, simultaneously with the meat deformation. The model considers the swelling pressure gradient caused by the shrinkage of the meat fibers and connective tissue due to the denaturation of proteins and the loss of the water holding capacity during cooking. The model results were successfully verified with experimental data of the central temperature and weight loss recorded during cooking for three degrees of doneness. The measured experimental temperatures at the center of the meat were 30 ± 3 °C (very rare), 44 ± 3 °C (rare) and 57 ± 2 °C (done) for a 19 mm steak thickness. Meanwhile, their water losses were 4 ± 2 %, 8 ± 1 % and 11 ± 2 %, respectively. The root mean squared errors of the model predictions were 2.16 °C (very rare), 3.56 °C (rare) and 4.57 °C (done) for the central temperature and 1.48 %, 2.08 % and 2.40 %, respectively for

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the water loss. The model also correctly predicts cooking times for steaks of different thicknesses, taking weight loss as a reference to set this time. The proposed model is postulated as a useful cooking assistance tool to estimate the optimal cooking time according to consumer preferences.

11 *Keywords:* Cooking, food model, beef meat, shrinkage, finite elements

12 **1. Introduction**

13 There is increasing interest in developing accurate numerical models of
14 meat cooking processes with the aim of achieving a high degree of knowledge
15 and control of the complex heat and mass transfer phenomena involved.
16 Knowledge of meat behavior during cooking is very important for optimizing
17 and controlling the final quality of the product. The physical phenomena
18 that underlie the meat cooking process can basically be considered by the
19 coupling of heat and moisture transfer in a deforming porous medium (Datta,
20 2007). The state of the art models differ in their degrees of approximation
21 and therefore in their complexity. Some exclusively consider conductive heat
22 transfer and the diffusive transport of matter. Other models incorporate
23 the convective heat transport by the liquid moisture flow and also describe
24 the moisture transport by the Flory-Rehner theory (van der Sman, 2015;
25 Feyissa et al., 2013; Ahmad et al., 2015; Nelson et al., 2020). However, little
26 information has been provided on meat deformation during cooking as a solid
27 mechanics problem, with some exceptions such as the research conducted by
28 Dhall and Datta (2011), Feyissa et al. (2013) and Blikra et al. (2019). When
29 meat is heated, water migrates through the surface either in the form of liquid
30 or in the form of vapor whilst the temperature and water content inside the

31 meat vary in space and time at the same time that the meat volume changes.
32 During cooking, meat proteins denature and cause structural changes, such
33 as the shrinkage of muscle fibers and connective tissue, and the formation of
34 larger pores in parts closer to the surface, being smaller in parts closer to the
35 center (Feyissa et al., 2013). These changes in porosity lead to an increase
36 in water permeability in the outer parts of the meat and consequently in
37 the water transport. Not considering this shrinkage could lead to errors in
38 the estimation of the weight loss of the meat (Datta, 2016). These structural
39 changes also decrease the water holding capacity of the meat. The mechanical
40 force exerted by the contracting protein network on the interstitial fluid,
41 denoted swelling pressure, leads to the expulsion of the moisture from the
42 meat (Tornberg, 2005). In water loss, swelling pressure is a more important
43 mechanism than surface evaporation, accounting for up to 80 % of the water
44 losses during double-sided pan cooking of beef burgers (Tornberg, 2013). In
45 these cases, Darcy’s law is used to associate the hydraulic pressure with the
46 moisture transport (Rabeler and Feyissa, 2018).

47 Many recent meat cooking models have focused on baking or frying (Ah-
48 mad et al., 2015; Bansal et al., 2015; Feyissa et al., 2013; Isleroglu and
49 Kaymak-Ertekin, 2016; Kondjoyan et al., 2013; Rabeler and Feyissa, 2018;
50 van der Sman, 2007; van Koerten et al., 2017) and only a few on pan cooking
51 (Dhall and Datta, 2011; Eberth et al., 2012; Rocca-Poliméni et al., 2019)
52 despite being a very common cooking method in the domestic environment.
53 This may be due to the added complexity of tracking the heat transfer phe-
54 nomena between the pan surface and the meat. The real contact surface be-
55 tween the meat and the pan is smaller than what is apparent because it can

56 be considered as interspersed contact spots between gaps (Rocca-Poliméni
57 et al., 2019). Another challenge of pan cooking modeling is the need to turn
58 the meat over. Previous studies have been limited to the analysis of one-
59 sided pan cooking of the meat, when typically the meat is turned several
60 times during cooking (Myhrvold, 2017).

61 The main objective of this work was to define and validate a computa-
62 tional model that, in addition to describing the coupled transfer of heat and
63 humidity during the domestic pan cooking of beef meat, takes into account:
64 i) the deformation of the meat as a solid mechanical problem, ii) includes the
65 turn over process, and iii) addresses some key aspects of pan cooking as the
66 contact heating interface between the pan and the meat. In order to validate
67 the model, an experimental protocol was developed to gather information
68 during meat cooking and to obtain some of the beef meat properties that the
69 model needs as inputs. The computational results were verified by compar-
70 ing the temperature and the weight loss evolution of beef with the results
71 obtained by experimentation. Another objective of this study was to check
72 the adaptability of the proposed model for use as assistance to cooking in a
73 domestic environment. For this reason, the cooking times predicted by the
74 model for different thicknesses of the meat piece were experimentally verified.

75 **2. Mathematical model**

76 The pan-cooking of beef can be described as a flow and transport prob-
77 lem in a deforming solid matrix during thermal processing. In this study,
78 the mathematical model that describes these phenomena was implemented
79 in the software COMSOL Multiphysics 5.2a while making the following as-

80 sumptions: (1) Meat was considered as a continuum biphasic (liquid-solid)
 81 porous material. For simplicity, the structure of the meat was assumed to be
 82 homogeneous, since in this case, the majority of the meat does not reach very
 83 high temperatures so that the existence of larger pores on the surface can be
 84 neglected. (2) Due to the rubbery nature of the meat, it was addressed as
 85 a hyper-elastic material in which the total volume change was equal to the
 86 volume of moisture loss and consequently the solid matrix remained satu-
 87 rated. (3) The temperature was assumed to be the same for the two phases.
 88 (4) The moisture flow due to the pressure gradient caused by the shrinking
 89 connective tissue on the aqueous solution in the extracellular void followed
 90 Darcy's law, (5) Water evaporates on the surface of the meat which is in
 91 contact with the pan.

92 It is convenient, at this point, to introduce the volume fraction ϕ_α for
 93 each phase:

$$\phi_\alpha = \lim_{V \rightarrow 0} \frac{V_\alpha}{V}, \quad \alpha = s, f \quad (1)$$

94 where V_α is the volume occupied by the α phase and $V = V_s + V_f$ is
 95 the total volume. The volume fractions ϕ_α in (1) satisfy the volume fraction
 96 condition $\phi_s + \phi_f = 1$. The density of the solid and fluid phase is related to
 97 its true (or, intrinsic) density $\bar{\rho}_\alpha$ as follows:

$$\rho_\alpha = \bar{\rho}_\alpha \phi_\alpha, \quad \alpha = s, f \quad (2)$$

98 To describe the kinematics or motion of the biphasic media, let $\mathbf{x} =$
 99 $\chi(\mathbf{X}, t) : \Omega_0 \times \mathbb{R} \rightarrow \mathbb{R}^3$ denotes the motion mapping and let \mathbf{F} be the associ-
 100 ated deformation gradient. Here \mathbf{X} and \mathbf{x} define the respective positions of

101 a particle in the reference Ω_0 and current Ω configurations such that $\mathbf{F} = \frac{d\mathbf{x}}{d\mathbf{X}}$
102 represents a measure of the deformation. Further, let $J \equiv \det \mathbf{F}$ be the Jaco-
103 bian of the motion that provides the ratio between the volume in the present
104 configuration and the volume in the reference configuration.. To properly de-
105 fine volumetric and deviatoric responses in the nonlinear range, we introduce
106 the following kinematic decomposition (Flory, 1961):

$$\mathbf{F} = J^{\frac{1}{3}} \bar{\mathbf{F}}, \quad \bar{\mathbf{F}} = J^{-\frac{1}{3}} \mathbf{F} \quad (3)$$

$$\mathbf{C} = \mathbf{F}^T \mathbf{F}, \quad \bar{\mathbf{C}} = J^{-\frac{2}{3}} \mathbf{C} = \bar{\mathbf{F}}^T \bar{\mathbf{F}} \quad (4)$$

107 where $J^{\frac{1}{3}}$ and $\bar{\mathbf{F}}$ represent the volumetric and distortional components,
108 respectively. $\bar{\mathbf{F}}$ and $\bar{\mathbf{C}}$ are denoted as the modified deformation gradient and
109 the modified right Cauchy-Green tensors.

110 [Figure 1 about here.]

111 Assuming that the deformation of the meat due to temperature effects is
112 small and therefore can be neglected, the moisture loss and deformation of
113 the meat can be modelled as two fictitious processes (Vujosevic and Lubarda,
114 2002; Dhall and Datta, 2011) as can be observed in Fig. 1. Using a multi-
115 plicative decomposition of the deformation gradient tensor \mathbf{F} :

$$\mathbf{F} = \mathbf{F}_f \mathbf{F}_s \quad (5)$$

116 The current deformation gradient is the product of the deformation as-
117 sociated with water volume changes (\mathbf{F}_f) and the elastic deformation of the
118 solid phase (\mathbf{F}_s). The volumetric part of the elastic tensor could be written

119 as a function of the deviatoric part taking the Jacobian as $\mathbf{F}_s = J_s^{1/3} \bar{\mathbf{F}}_s$,
 120 whereas the water loss implies only a pure volumetric process $\mathbf{F}_f = J_f^{1/3} \mathbf{I}$,
 121 being \mathbf{I} the identity matrix. Strain measures can be obtained for both solid
 122 and fluid phases in the same way as in Eq. (4). The modified right Cauchy-
 123 Green tensor for the solid phase $\bar{\mathbf{C}}_s = \bar{\mathbf{F}}_s^T \bar{\mathbf{F}}_s$ will be used later for constitutive
 124 modelling.

125 In the absence of body forces and accelerations, conservation of the lin-
 126 ear momentum for the bulk material results in the quasi-static equilibrium
 127 equation $\nabla \boldsymbol{\sigma} = 0$, with $\boldsymbol{\sigma}$ being the total Cauchy stress. Conservation of
 128 the angular momentum yields the symmetry of this stress tensor that can be
 129 expressed as the sum of the partial solid stress and the partial fluid stress:

$$\boldsymbol{\sigma} = \hat{\boldsymbol{\sigma}}_s + \hat{\boldsymbol{\sigma}}_f \quad (6)$$

130 where

$$\hat{\boldsymbol{\sigma}}_s = \phi_s \boldsymbol{\sigma}_s \quad \text{and} \quad \hat{\boldsymbol{\sigma}}_f = \phi_f \boldsymbol{\sigma}_f = -\phi_f p_f \mathbf{I} \quad (7)$$

131 p_f being the pore fluid pressure.

132 In this study, the behaviour of meat during the cooking process has, due
 133 to its rubbery nature, been approximated using the isotropic Neo-Hookean
 134 material model. This model, for the best numerical performance, takes this
 135 particular quasi-incompressible form of the strain energy function:

$$\Psi_s(\mathbf{C}_s) = \Psi_s(J_s, \bar{\mathbf{C}}_s) = \frac{K}{2} (J_s - 1)^2 + \frac{G'}{2} (\bar{I}_1 - 3) \quad (8)$$

136 where K and G' are the bulk and the shear elastic modulus and $\bar{I}_1 = \text{tr} \bar{\mathbf{C}}_s$
 137 is the first invariant of the modified (deviatoric) right Cauchy-Green tensor.

138 Applying the entropy inequality, the second Piola-Kirchhoff stress tensor
 139 is obtained as the derivative of the strain energy in a non-dissipative process:

$$\mathbf{S}_s = 2 \frac{\partial \Psi(J_s, \bar{\mathbf{C}}_s)}{\partial \bar{\mathbf{C}}_s} = \mathbf{S}_{s,vol} + \bar{\mathbf{S}}_s = J_s p_s \mathbf{C}_s^{-1} + J_s^{-\frac{2}{3}} \left(\mathbb{I} - \frac{1}{3} \mathbf{C}_s^{-1} \otimes \mathbf{C}_s \right) : \tilde{\mathbf{S}}_s \quad (9)$$

140 where $\mathbf{S}_{s,vol}$ and $\bar{\mathbf{S}}_s$ are the volumetric and deviatoric parts of the sec-
 141 ond Piola-Kirchhoff stress tensor, p_s is the hydrostatic pressure and $\tilde{\mathbf{S}}_s$ the
 142 modified second Piola-Kirchhoff stress tensor:

$$p_s = \frac{d\Psi_{s,vol}(J_s)}{dJ_s} \quad \tilde{\mathbf{S}}_s = 2 \frac{\partial \bar{\Psi}_s(\bar{\mathbf{C}}_s)}{\partial \bar{\mathbf{C}}_s} \quad (10)$$

143 For the Neo-Hookean model the explicit expression for the second Piola-
 144 Kirchhoff stress tensor, as a function of the defined invariant, \bar{I}_1 , is:

$$\mathbf{S}_s = J_s p_s \mathbf{C}_s^{-1} + 2 \left[\frac{\partial \bar{\Psi}_s}{\partial \bar{I}_1} \mathbf{I} - \frac{1}{3} \left(\frac{\partial \bar{\Psi}_s}{\partial \bar{I}_1} \bar{I}_1 \right) \mathbf{C}_s^{-1} \right] \quad (11)$$

145 The Cauchy stress tensor $\boldsymbol{\sigma}_s$ is $1/J_s$ times the push-forward of \mathbf{S}_s ($\boldsymbol{\sigma}_s =$
 146 $J_s^{-1} \boldsymbol{\chi}_*(\mathbf{S}_s)$) so, from (9), we obtain

$$\boldsymbol{\sigma}_s = p_s \mathbf{I} + \frac{2}{J_s} dev \left[\bar{\mathbf{F}}_s \frac{\partial \bar{\Psi}_s(\bar{\mathbf{C}}_s)}{\partial \bar{\mathbf{C}}_s} \bar{\mathbf{F}}_s^T \right] = p_s \mathbf{I} + \frac{2}{J_s} \left(\frac{\partial \bar{\Psi}_s}{\partial \bar{I}_1} \bar{\mathbf{b}}_s - \frac{1}{3} \frac{\partial \bar{\Psi}_s}{\partial \bar{I}_1} \bar{I}_1 \mathbf{I} \right) \quad (12)$$

147 with \mathbf{I} being the second-order identity tensor and dev the deviator opera-
 148 tor in the spatial description and $\bar{\mathbf{b}}_s = \bar{\mathbf{F}}_s^T \bar{\mathbf{F}}_s$ the modified left Cauchy-Green
 149 tensor.

150 The product density in the deformed configuration $\rho = \rho(t)$ is:

$$\rho = \phi_s \bar{\rho}_s + \phi_f \bar{\rho}_f = \rho_s + \rho_f \quad (13)$$

151 The mass balance for both phases becomes:

$$\frac{\partial(\phi_s \bar{\rho}_s)}{\partial t} + \nabla(\phi_s \bar{\rho}_s \mathbf{v}_s) = 0 \quad (14)$$

$$\frac{\partial(\phi_f \bar{\rho}_f)}{\partial t} + \nabla(\phi_f \bar{\rho}_f \mathbf{v}_s) + \nabla \mathbf{n}_f = 0 \quad (15)$$

152 where \mathbf{v}_s corresponds to the absolute velocity of the solid phase and \mathbf{n}_f
 153 is the water mass flux, described later. Note that no evaporation effect is
 154 considered in Eq. (15) since water evaporates only on the surface.

155 In the absence of external loads, the meat only shrinks depending on the
 156 moisture lost. $V(t)$ being the total volume of the product and $\phi_{f,0}$ the initial
 157 volume fraction of the fluid, the following balance could be established:

$$V(t) - V_0 = \phi_f V(t) - \phi_{f,0} V_0 \quad (16)$$

158 Since the solid matrix is always saturated with water, the product porosity
 159 coincides with the volumetric fraction of water ϕ_f . For this reason, the
 160 porosity value can be calculated at each instant of time considering the solid
 161 skeleton of the product incompressible or quasi-incompressible ($J_s \approx 1$):

$$\phi_f(t) = 1 - \frac{1 - \phi_{f,0}}{V(t)/V_0} = 1 - \frac{1 - \phi_{f,0}}{J(t)} \quad (17)$$

162 In this way, the Jacobian associated with fluid or water loss $J(t)$ is a state
 163 function depending on the fluid content in the meat.

164 The heat transfer process inside the product, assuming the same temper-
 165 ature for all phases, can be modeled with a unique energy balance equation
 166 for the entire product.

$$(\rho C_p) \frac{\partial T}{\partial t} + (\mathbf{n}_f \cdot \nabla(C_{p,w}T)) = \nabla \cdot (k_p \nabla T) \quad (18)$$

167 C_p and $C_{p,w}$ are the specific heat of the product and the water, respec-
 168 tively, whereas k_p is the thermal conductivity of the product.

169 Darcy's law, states that water flows in a porous medium due to the pres-
 170 sure gradient inside the solid matrix and gravity. Thus, the water mass flux
 171 can be written as:

$$\mathbf{n}_f = -\rho_f \frac{\kappa}{\mu} (\nabla p_f - \rho_f \mathbf{g}) \quad (19)$$

172 where κ is the permeability of the medium and μ its dynamic viscosity.
 173 Considering the gravity effect insignificant and p_f being the swelling pressure
 174 proportional to the difference between the actual ρ_f and the equilibrium
 175 water concentration $\rho_{f,eq}(T)$ (Dhall and Datta, 2011):

$$p_f = \vartheta(\rho_f - \rho_{f,eq}(T)) \quad (20)$$

176 where ϑ is a constant of proportionality. Introducing this relation in (19):

$$\mathbf{n}_f = -(D_f \nabla \rho_f - D_{f,T} \nabla T) \quad (21)$$

177 $D_f = \rho_f \frac{\kappa}{\mu} \vartheta$ is the diffusivity due to the water gradient concentration and
 178 $D_{f,T} = \rho_f \frac{\kappa}{\mu} \vartheta \frac{\partial \rho_{f,eq}}{\partial T}$ is the diffusivity due to the temperature gradient, both
 179 taken as parameters determined through the model.

180 Once the swelling pressure is defined and the relevant simplifications are
 181 made, the evaporation front is limited to the surface of the material, so there

182 is no internal steam generation. Therefore, the mass conservation equations
183 are reduced only to that of liquid water:

$$\frac{\partial \phi_f \bar{\rho}_f}{\partial t} + \nabla (\phi_f \bar{\rho}_f \mathbf{v}_s) = \nabla \cdot (D_f \nabla (\phi_f \bar{\rho}_f) + D_{f,T} \nabla T) \quad (22)$$

184 3. Materials and methods

185 *Longissimus dorsi* muscles from two Asturiana de los Valles heifers (1
186 year old) 7 days post mortem were obtained the same day on which the
187 experimental tests were performed. For the cooking tests, the middle parts
188 of these loins were cut perpendicular to the longitudinal axis resulting into
189 a total of eighteen steaks of three different thicknesses (19 ± 2 mm, 26 ± 2
190 mm and 34 ± 2 mm). From each steak, three pieces approximately 81 ± 21
191 mm long and 26 ± 1 mm of wide were obtained cutting the steaks parallel
192 to the grain. The weights of these pieces were 43.7 ± 6.7 g, 51.9 ± 12.9 g and
193 71.9 ± 16.3 g for the thicknesses of 19, 26 and 34 mm, respectively.

194 In order to determine the water holding capacity and to do the rheological
195 measurements, the loin was sliced (4 mm thickness) and then cut into pieces
196 of about 8 g.

197 3.1. Meat properties

198 The density, the heat capacity and the heat conductivity of the solid
199 phase of the meat were calculated as a function of temperature and compo-
200 sition (Choi and Okos, 1986). This composition was determined by the mass
201 fractions of the protein x_{prot} and fat x_{fat} . The meat density was calculated
202 as function of temperature and composition as follows (Nesvadba, 2014):

$$\bar{\rho}_s(T) = \left(\frac{x_{\text{prot}}}{\bar{\rho}_{\text{prot}}(T)} + \frac{x_{\text{fat}}}{\bar{\rho}_{\text{fat}}(T)} \right)^{-1} \quad (23)$$

203 The specific heat of the meat $C_{p,s}(T)$ was defined for each component and
 204 then calculated using a mass fractions average mixing rule:

$$C_{p,s}(T) = x_{\text{prot}}C_{p_{\text{prot}}}(T) + x_{\text{fat}}C_{p_{\text{fat}}}(T) \quad (24)$$

205 Isotropic thermal conductivity is assumed for the product lying between
 206 two limiting values. The lower limit is given by a perpendicular model with all
 207 the constituents in layers perpendicular to the flow of heat $\frac{1}{k_{\perp}(T)} = \sum_i \frac{\phi_i}{k_i(T)}$.
 208 The upper limit is the parallel model, in which the constituents are arranged
 209 as parallel layers $k_{\parallel}(T) = \sum_i \phi_i k_i(T)$. The thermal conductivity of the prod-
 210 uct is estimated as:

$$k_p(T) = gk_{\perp}(T) + (1 - g)k_{\parallel}(T) \quad (25)$$

211 where g is a number between zero and one (Nesvadba, 2014; van der
 212 Sman, 2013).

213 3.2. Water holding capacity

214 Water holding capacity (WHC) describes the ability of the meat to resist
 215 the removal of liquid caused by protein denaturation during cooking. The
 216 WHC was measured following the procedure described by Goñi and Salvadori
 217 (2010). The effect of temperature on the WHC was determined by immersing
 218 slices of meat packaged into plastic bags in a thermostatic bath (Digiterm
 219 S-150, JP Selecta, Abrera, Spain) at a given temperature (from 30 °C to
 220 100 °C), and waiting for equilibrium (30 min until there was no more weight

221 loss). The final water content in the meat was defined as the WHC. Ten
222 replicas were used for each temperature and the results were expressed as kg
223 water/kg dry material.

224 *3.3. Rheological measurement*

225 Rheological characteristics of circular beef samples with a thickness of
226 4 ± 0.5 mm and a diameter of 50 ± 2 mm were measured using a Physica MRC
227 301 rheometer (Anton Paar GmbH, Graz, Austria), equipped with serrated
228 parallel plate geometry (50 mm, 4 mm gap) and a temperature controller
229 (± 0.5 °C). Dynamic oscillating analyses were performed at a frequency of
230 2 Hz and a constant stress of 3 Pa. The constant value for frequency and
231 stress were chosen within the linear viscoelastic region that was determined
232 by performing frequency sweeps (0.1–10 Hz) and stress sweeps (0.1–1000 Pa).
233 The tests were carried out increasing the sample temperature from 25 °C to
234 100 °C with steps of 5 °C, holding each temperature step for 3 min (enough to
235 ensure no further changes in the measurement). The evolution of the storage
236 modulus (G') and phase angle, the ratio of loss modulus to storage modulus
237 (ϕ), with temperature were recorded by the rheometer software using five
238 replicas.

239 *3.4. Cooking procedure*

240 Each piece of meat (at 20 °C) was individually cooked on a multilayer 210
241 mm diameter, 5.5 cm deep round frying pan (WMF, WMF Group GmbH,
242 Geislingen an der Steige, Germany). The bottom of the pan consisted of three
243 layers: 0.6 mm of steel at the bottom, 3.5 mm of aluminium in the middle,
244 and 0.8 mm of steel with a Teflon non stick coating at the top (Fig. 2.a).

245 An induction hob (BOSCH Schott Ceran PXY675DW4E/01 model, BSH,
246 Munich, Germany) was used for cooking (frying sensor at level 5). Once the
247 hob is turned on, there is a transition period of approximately 110 s until a
248 stable temperature at the pan surface is reached. When the thermographic
249 images taken with an infrared thermal imager (875-2 model, Testo, Lenzkirch,
250 Germany) indicated that a stable temperature of 215 ± 3 °C has been reached,
251 the meat was added to the pan. From that moment on, the temperature drops
252 slightly and recovers quickly, which makes it possible to consider that cooking
253 takes place at a constant temperature at the pan surface of 215 °C. The meat
254 was cooked at three degrees of doneness: very rare, medium rare and done,
255 corresponding to cooking times of 180 s, 300 s, and 420 s, respectively, for
256 the pieces of 19 mm thickness. For the pieces of 26 and 34 mm thickness, the
257 cooking times were established by the model predictions. The samples were
258 turned over at two thirds of the total cooking time. Six pieces obtained from
259 steaks located in the loin at different longitudinal positions were cooked for
260 each degree of doneness and thickness.

261 The meat weight was continuously measured by a balance placed under
262 the induction hob (DS30K0.1L, Kern & Sohn, Balingen-Frommern, Germany)
263 with a precision of 0.1 g. Data was recorded every 1s in a measurement range
264 up to 30 kg. The core temperature was measured by a penetration *T type*,
265 1.5 mm diameter thermocouple connected to a data logger (177-T4, Testo,
266 Lenzkirch, Germany), as shown in Fig. 2. The data were presented as the
267 mean \pm standard deviation.

268 [Figure 2 about here.]

269 4. Finite element model

270 A 3D computational model was developed to reproduce the cooking pro-
271 cess. This model includes two different parts: an aluminium pan with a
272 diameter of 210 mm and 5 mm thickness and a beef steak (see Fig. 3). The
273 beef sample was modeled as a 3D rectangular cuboid object. To reproduce
274 the turning over of the steak two pans were considered. First, the bottom
275 face of the steak is heated in a pan. Secondly, the top face of the same steak
276 is heated in a second pan. This method of simulating the turn over process
277 is possible due to the insignificant relevance of gravity in this problem. In
278 addition, in order to simplify the process, it has been considered that the
279 steak surface remains flat during the entire cooking time.

280 The model recreates a quarter of this geometry. It was meshed with
281 hexahedral elements using a quadratic approximation for mass transfer and
282 temperature for the meat, and with tetrahedral elements for the pan. Mesh
283 sensitivity analysis was carried out to establish the mesh size. The total
284 number of degrees of freedom and elements is 5 and 366, respectively (300
285 elements for the beef sample).

286 [Figure 3 about here.]

287 The simulation time was fixed as the experimental cooking time for each
288 degree of doneness. The boundary conditions on the top and bottom surfaces
289 were reversed after turning over by activating the upper pan and deactivating
290 the lower one.

291 *4.1. Initial and boundary conditions*

292 An initial temperature condition of 215 °C which remains constant through-
 293 out the cooking time is set on the surface of the pan to simulate the exper-
 294 imental procedure, as well as a uniform temperature for the meat of 20 °C.
 295 The contact equation between the pan and the meat and the heat transfer
 296 general equation for the two faces are defined as:

$$-k_{pan} \left. \frac{\partial T}{\partial z} \right|_{z_{pan}=0} = -k_p \left. \frac{\partial T}{\partial z} \right|_{z_{meat}=0} = H_c (T_{pan} - T_{surf}) \quad (26)$$

$$q_{surf} = h(T_{amb} - T_{surf}) - \lambda n_{f,surf} - \mathbf{n}_f C_{p,w} T \cdot \mathbf{N}_{surf} \quad (27)$$

297 where T_{pan} , T_{surf} are the temperature of the pan and the temperature of
 298 the meat on the surface where the boundary condition is being evaluated,
 299 k_{pan} is the conductivity of the pan and \mathbf{N}_{surf} is the surface normal. The
 300 parameter H_c refers to the thermal conductance between both surfaces. This
 301 parameter, which has been obtained computationally, regulates the heat flow
 302 received by the meat through the contact heating surface. Its value is crucial
 303 for this cooking method, so it has been one of the highlighted objectives of
 304 the study. h is the thermal convection coefficient. T_{amb} is the temperature
 305 of the air surrounding the meat, λ is the vaporization latent heat and $n_{f,surf}$
 306 the magnitude of the evaporation flux. The meat around the heating surface
 307 increases its temperature very quickly so that the water holding capacity
 308 falls at a faster rate than water loss by evaporation, causing the dripping
 309 phenomenon (Hughes et al., 2014). Both, phase change to steam and the
 310 dripping of liquid water, were included as boundary condition on the surface
 311 of the meat in contact with the pan. On the surface in contact with the pan

312 both, phase change to steam and the dripping of liquid water, were included,
 313 while on the side walls only the dripping was considered. Neither of these
 314 two phenomena occur on the upper face. This was reflected in the heat fluxes
 315 on the surfaces. The steam flow in the evaporation process is given in Eq.
 316 (28) and the drip losses in Eq. (29):

$$n_{f,surf E} = h_m(\rho_{v,surf} - \rho_{v,amb}) \quad (28)$$

$$n_{f,surf D} = \mathbf{n}_f \cdot \mathbf{N}_{surf} - h_m(\rho_{v,surf} - \rho_{v,amb}) \quad (29)$$

317 where h_m is the mass transfer coefficient by convection and $\rho_{v,surf}$ and
 318 $\rho_{v,amb}$ are the vapor density on the surface of the meat and the vapor density
 319 in the surrounding air, respectively, obtained by the ideal gas law.

320 4.2. Parameters

321 The input parameters used in this model are shown in Table 1. These
 322 parameters were obtained through experimental tests measurements or from
 323 bibliography, while others were optimized through the model in order to fit
 324 the experimental results.

325 5. Results and Discussion

326 Firstly, the results of the meat parameters obtained by experimentation
 327 and necessary for the development of the model are explained. Validation of
 328 the model by comparing the central point temperature of the steak and the
 329 average moisture content is then shown. Lastly, the settings of the cooking

Name and description	Value	Source
Problem parameters		
T_{amb} surrounding air temperature [°C]	25	Measured
T_{pan} pan temperature [°C]	215	Measured
P_{amb} environment pressure [kPa]	$1.013 \cdot 10^2$	Measured
H_c thermal conductance of pan-meat contact [W/(m ² K)]	120	Computational
g thermal conductivity parameter	0.45	Computational
Water properties		
$\bar{\rho}_f$ water density [kg/m ³]	997.2	Choi and Okos (1986)
D_f water diffusivity [m ² /s]	$1 \cdot 10^{-9}$	Computational
$D_{f,T}$ water diffusivity due to temperature gradient [kg/(m s K)]	$D_f \cdot \frac{\partial \rho_{f,wa}}{\partial T}$	Computational
$C_{p,f}$ water specific heat [kJ/(kg °C)]	$4.1289 - 9.0864 \cdot 10^{-5} \cdot T + 5.4731 \cdot 10^{-6} \cdot T^2$	Choi and Okos (1986)
k_f water thermal conductivity [W/(m K)]	0.57	Choi and Okos (1986)
λ vaporization latent heat [J/kg]	$2.26 \cdot 10^6$	Straub (1985)
h_m mass transfer coefficient [m/s]	0.008	Computational
Meat properties		
$C_{p,s}$ meat specific heat [J/(kg K)]	$2.0082 + 1.2089 \cdot 10^{-3} \cdot T - 1.3129 \cdot 10^{-6} \cdot T^2$	Choi and Okos (1986)
k_p product thermal conductivity [W/(m K)]	$1.7881 \cdot 10^{-1} + 1.1958 \cdot (10^{-3}) \cdot T - 2.7178 \cdot (10^{-6}) \cdot T^2$	Choi and Okos (1986)
WHC water holding capacity [kg water/kg dry material]	Fig. 4	Measured
C' storage modulus [kPa]	Fig. 5	Measured

Table 1: Model input parameters.

330 times for the different thicknesses of meat based on the previous results are
331 given.

332 5.1. Effect of heating on meat properties

333 5.1.1. Water holding capacity

334 The effect of temperature on the WHC is shown in Fig.4. As expected,
335 the WHC diminishes as the temperature increases since the thermal denatu-
336 ration of the proteins during cooking is the cause of the reduction of the water
337 retention capacity of the meat. The evolution of WHC with temperature fol-
338 lows a sigmoidal shape, as previously described by Goñi and Salvadori (2010)
339 and van der Sman (2007). The experimental values of WHC, determined
340 using the Association of Official Analytical Chemists (AOAC) method no.

341 950.46, are quite similar to those found by these authors for beef, although
 342 the values can vary from one type of muscle to another (Kondjoyan et al.,
 343 2013). The sarcomere length is known to have a deep effect on WHC. The
 344 mechanisms behind shortening of the sarcomere are complex and continue
 345 to be discussed (Ertbjerg and Puolanne, 2017). The following function was
 346 fitted to the experimental data:

$$\text{WHC}(T) = c_i - \frac{a_1}{1 + a_2 \exp(-a_3(T - T_4))} \quad (30)$$

347 where $c_i = 2.986$, $a_1 = 1.69$, $a_2 = 0.56$, $a_3 = 0.08309$ and $T_4 = 66.76$ °C
 348 were estimated by a non-linear regression using the Levenberg-Marquardt
 349 method and with a R-squared of 0.9853. In this way, the equilibrium wa-
 350 ter concentration is related to the WHC through the equation $\rho_{f,eq}(T) =$
 351 $\text{WHC}(T)\rho_s$.

352 [Figure 4 about here.]

353 5.1.2. Rheological properties

354 The temperature dependence of the storage modulus G' and the phase
 355 angle ϕ for the beef, as shown in Fig. 5, were obtained from the experimental
 356 tests described in section 3.3. The storage modulus decreases slightly until
 357 reaching a minimum value at 55 °C. However, it increases markedly up to 40
 358 kPa from 65 °C to 80 °C, and decreases at temperatures above 80 °C. The
 359 contraction of the connective tissue, which occurs mainly above 65 °C, results
 360 in an increase in the elasticity of the meat, which leads to an increase in the
 361 storage modulus. The phase angle diminishes over the whole temperature
 362 range tested but more noticeable decrease is observed from 50 °C to 60 °C

363 down to a plateau at around 65 °C. Tornberg (2005) and Rabeler and Feyissa
 364 (2018) obtained similar trends in the 30-80 °C range for *M. biceps femoris*
 365 beef and chicken breast, respectively, but the values found by these authors
 366 differ from those shown in Fig. 5 because they correspond to different muscles
 367 and species.

368 [Figure 5 about here.]

369 The storage modulus, for temperatures between 30 °C and 100 °C, can
 370 be defined by a piecewise Eq. (31) :

$$G'(T) = \begin{cases} G_a \cdot T + G_b & \text{if } 30^\circ C \leq T < 55^\circ C \\ G_c + \frac{G_d}{(1+\exp(-G_e(T-G_f)))} & \text{if } 55^\circ C \leq T < 80^\circ C \\ G_g \cdot T^2 + G_h \cdot T + G_i & \text{if } 80^\circ C \leq T < 100^\circ C \end{cases} \quad (31)$$

371 where $G_a = -0.8816 \text{ kPa } ^\circ\text{C}^{-1}$, $G_b = 82.06 \text{ kPa}$, $G_c = 36.40 \text{ kPa}$, $G_d =$
 372 85.32 kPa , $G_e = 0.3386$, $G_f = 68.04$, $G_g = 0.05647 \text{ kPa } ^\circ\text{C}^{-2}$, $G_h = -12.74$
 373 $\text{kPa } ^\circ\text{C}^{-1}$ and $G_i = 781.8 \text{ kPa}$, values obtained by adjusting the experimental
 374 results obtaining a R-squared of 0.9998. Fig. 5 shows the experimental value
 375 of the storage modulus and its fitting.

376 5.2. Temperature and water loss for pieces of 19 mm

377 Fig. 6 compares the temperature at the central point obtained with the
 378 model and the experimental results for the three degrees of doneness. In
 379 the experimental measuring, the sensor may suffer deviations in its position,

380 which could produce differences in temperature measurements. These differ-
381 ences are reflected by the gray bands, which reflect the standard deviation
382 of these measurements like in Figs. 6 to 9. Therefore, the accuracy of this
383 initial thermocouple position was estimated as ± 1 mm. For this reason, com-
384 putational digressions were calculated considering this displacement of the
385 location of the probe (see Fig. 6 d.). In every case a linear behavior was
386 observed after 80 s of cooking. The maximum temperatures reached in the
387 center of the steak for the different times were 33 °C, 47 °C and 58 °C for
388 180 s (very rare), 300 s (medium rare) and 420 s (done), respectively. The
389 Root Mean Squared Error, RMSE, for each case was calculated as square
390 root of the sum of the squared differences between the predicted and exper-
391 imental values divided by the number of data. The RMSE obtained were:
392 2.16 °C (very rare), 3.56 °C (medium rare) and 4.57 °C (done). These tem-
393 peratures are very far from those obtained through the procedures described
394 by the American Meat Science Association, AMSA (1995), for the different
395 degrees of meat doneness, (55 °C-very rare, 60 °C-rare, 63 °C-medium rare,
396 71 °C-medium, 77 °C-done and 82 °C-well done). Leaving aside microbiolog-
397 ical considerations, from the point of view of consumer acceptance it is very
398 difficult to establish a relationship between the internal cooking tempera-
399 ture and the perception of the degree of cooking which depends on consumer
400 preferences (López Osornio et al., 2008). Fig. 6.d shows the temperature
401 distribution in a cross section for different times of medium rare cooking de-
402 gree. The temperature of the face in contact with the pan rises quickly and
403 stabilizes after a few seconds. Contrary to the temperature of the meat core,
404 this temperature is much higher (120 °C). After turning the steak over, a

405 reduction in this temperature is observed as this face is no longer in contact
406 with the heat source. It is now the other face which suffers an increase in
407 temperature. The cooking process was stopped the moment at which the
408 difference in temperature between the central point inside the steak and the
409 central point on the surface in contact with the pan was similar to the differ-
410 ence of temperature at the moment of turning over the steak (97 °C - very
411 rare, 93 °C - medium rare, 87 °C - done). Therefore, the time of turning over
412 the steak coincides with two thirds of the total cooking time.

413 As regards shrinkage, Fig. 6.d shows the volume reduction of the steak
414 and its change of shape for the medium rare degree of cooking. At the
415 beginning, the greatest deformation appears near the pan, while in the central
416 part of the steak there is hardly any deformation as this is the coldest area of
417 the piece of meat. As time progresses, this deformation extends to the central
418 part. At the moment of turning over the steak, the maximum deformation
419 occurs again in the face in contact with the pan. At 40 s the volume reduction
420 is around 1 % while at the end of the cooking (300 s) it is around 9 %. In
421 the case of the done degree of cooking (420 s), the final volume reduction
422 is about 12 %. The evolution of shrinkage during cooking is a consequence
423 of an increasing rigidity of the myofibrillar structure due to the thermal
424 denaturation of proteins. At temperatures from 40 °C to 60 °C transverse
425 shrinkage occurs in the miofibrils attributed principally to myosin, and in
426 the temperature range from 70 °C to 80 °C it is longitudinal and attributed
427 fundamentally to actin (Hughes et al., 2014; Purslow et al., 2016). The juice
428 expelled by the protein denaturation and contraction is associated with the
429 water loss during cooking that occurs from 45 °C to 75 °C - 80 °C, and

430 above 80 °C the cooking loss diminishes gradually (Tornberg, 2005). The
431 water loss evolution of the meat for the different cooking degrees is shown
432 in Fig. 7. The cooking losses for the different cooking times were 4 %, 7
433 % and 10 % for 180 s (very rare), 300 s (medium rare) and 420 s (done),
434 respectively. The computational results fit optimally with experimentation,
435 demonstrating a linear behavior with time. The RMSE for each case in our
436 study is: 1.48 % (very rare), 2.08 % (medium rare) and 2.40 % (done). The
437 above-mentioned research of Dhall and Datta (2011) shows that a water loss
438 of 7 % can be obtained for a cooking time of 300 s in patties, quite similar to
439 our medium rare degree of cooking. It is not surprising that similar results
440 are obtained between minced meat and whole meat since there is evidence of
441 the minor role of collagen in the loss of water during cooking (Hughes et al.,
442 2014; Tornberg, 2005).

443 [Figure 6 about here.]

444 [Figure 7 about here.]

445 *5.3. Cooking times prediction for different thicknesses of meat: water loss as* 446 *indicator*

447 One of the possible applications of the modeling of pan cooking is to pro-
448 vide assistance during cooking, and so it is important to know how the model
449 can be adapted to different real cooking conditions. One of the parameters
450 that can most influence meat cooking results is the thickness of the steak. In
451 order to predict how the cooking time changes depending on the thickness
452 of the meat, weight loss has been established as a control variable. In the
453 same manner as with the 19 mm thickness, experimental cooking tests were

454 carried out with thicknesses of 26 mm and 34 mm. The time of turning over
455 the steak and the final time of cooking were fixed at the moment when the
456 meat reached the same water loss than as the 19 mm piece in each degree
457 of cooking. Thus, the times for the 26 mm thickness were modified to 225 s
458 (very rare), 450 s (medium rare) and 720 s (done), and the times for 34 mm
459 were 265 s (very rare), 495 s (medium rare) and 770 s (done). The times
460 for turning over the steak were kept at two thirds of the total time. Once
461 the model for the 19 mm thickness had been verified, it was checked whether
462 this model could adjust the temperature in the center of the steak and the
463 water loss for these new thicknesses. These results are shown in Fig. 8 and
464 in Fig. 9. The model successfully adjusts both the 26 and 34 mm cases. In
465 the same way as for the 19 mm pieces, a displacement deviation of 5 % in the
466 location of the temperature probe was applied in each case. The maximum
467 temperatures reached in the center of the steak for each thickness and time
468 are quite similar to those obtained with the 19 mm thickness steak: 26 mm
469 (31 °C - very rare, 45 °C - medium rare, 58 °C - done) and 34 mm (32 °C
470 - very rare, 46 °C - medium rare, 58 °C - done). This verification could be
471 taken as evidence of an appropriate functioning of the model. As a conclu-
472 sion of these results, we can confirm that this model may predict cooking
473 times according to the weight loss of the meat during cooking.

474 [Figure 8 about here.]

475 [Figure 9 about here.]

476 *5.4. Analyzing the effect of the steak thickness*

477 The thickness of the fillets is not uniform and some uncertainties are
478 present in the measurement process. Small variations in the thickness of the
479 meat could cause changes in the expected temperature reached in the steak.
480 Changes in temperature in the presence of variations in thickness can be
481 known by means of a sensitivity analysis carried out with the Monte Carlo
482 method. This technique has been applied to the 3D model of the steak of
483 19 mm of thickness considering the three cooking degrees. The results are
484 shown in Fig. 10 for the done degree where a population of one hundred
485 models was analyzed considering a uniform distributed thickness between
486 $\pm 10\%$ the mean value. In order to reduce the computational cost, the model
487 was simplified by disabling the effect of shrinkage, hence the small differences
488 in temperature and weight loss compared with those analyzed in section 5.2
489 for thicknesses of 19 mm. The temperature at the central point is represented
490 as a mean value and a standard deviation (Fig. 10.a) and takes values of 35 ± 2
491 $^{\circ}\text{C}$, 47 ± 4 $^{\circ}\text{C}$ and 63 ± 5 $^{\circ}\text{C}$ at 180 s (very rare), 300 s (medium rare) and 420
492 s (done), respectively. A sensitivity analysis was also conducted on the meat
493 water loss (Fig. 10.b) obtaining values of 4 ± 0.3 %, 7 ± 0.4 % and 10 ± 0.5
494 % at 180 s (very rare), 300 s (medium rare) and 420 s (done), respectively.
495 These dispersion values obtained with the Monte Carlo technique are very
496 close to those obtained in the experimental tests.

497 [Figure 10 about here.]

498 6. Conclusions

499 A 3D computational model was developed that considers the phenom-
500 ena of heat and moisture flow transfer and the deformation of meat during
501 the double-sided pan cooking of beef steaks. The equations were solved by
502 the finite element method. The evolution over time of the temperature at
503 the central point and the weight loss predicted by the model were compared
504 with the experimental results for different cooking times and meat thick-
505 nesses. The good agreement between the predicted and experimental results
506 allowed the model to be verified and the assumptions made to be considered
507 appropriate.

508 The simulation results provided a better and more detailed insight into
509 steak pan cooking allowing the accurate prediction of the cooking time re-
510 quired to reach a certain temperature in the center of the meat, that is, to
511 achieve the desired degree of doneness regardless of the steak thickness; this
512 being of utmost importance for successful cooking. The choice of weight loss
513 as the reference parameter to estimate the cooking times of steaks of different
514 thicknesses is a promising option for several reasons: the core temperatures
515 thus obtained for the different thickness are similar (± 2 °C), the measure-
516 ment of the weight may be implemented in induction hobs in the future,
517 the difficulty of measuring the temperature exactly at the geometric center
518 of the steak is overcome, and a small deviation in fillet thickness involves a
519 change in temperature prediction at the center of the same order of magni-
520 tude as that between some degrees of doneness. However, since the water
521 retention capacity depends on the muscle and the quality of the meat, the
522 use of weight loss as the only reference parameter to establish the cooking

523 time has its limitations for uncharacterized pieces of meat, but it can still be
524 considered a complementary parameter to the central temperature.

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534 **8. Declaration of Interest Statement**

535 The authors have no competing interests to declare

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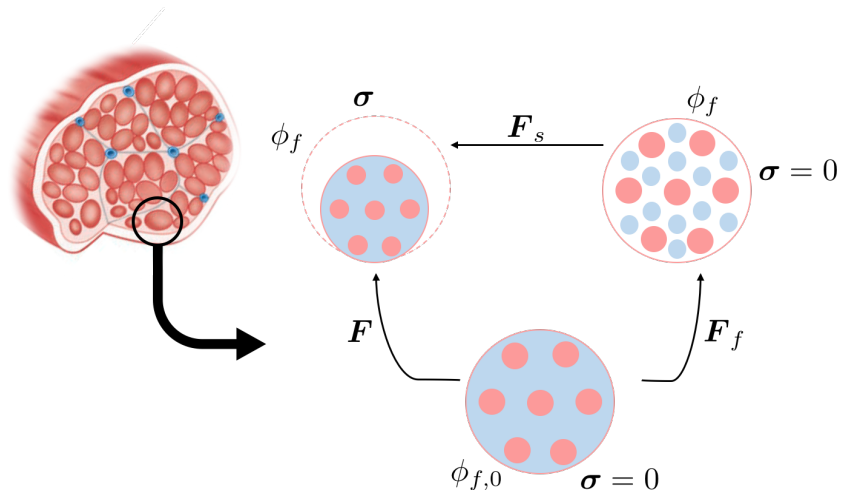


Figure 1: Modeling the moisture loss and deformation of the meat using a fictitious intermediate step. Quasi-static equilibrium was considered ($\nabla \boldsymbol{\sigma} = 0$ with $\boldsymbol{\sigma}$ being the Cauchy stress tensor) and the deformation gradient tensor \mathbf{F} was decomposed multiplicatively in two parts associated with the water volume change, \mathbf{F}_f , and the elastic deformation of the solid phase \mathbf{F}_s .

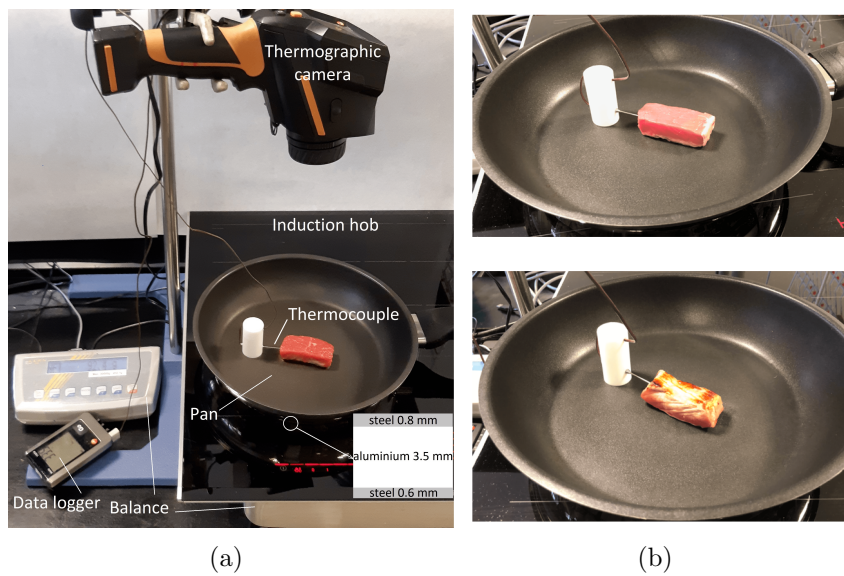


Figure 2: a) Experimental setup for temperature and weight loss measurement during the cooking process. b) Evolution of the geometry of the steak along the test comparing the beginning of the process (top) and the end (bottom) for a done doneness degree.

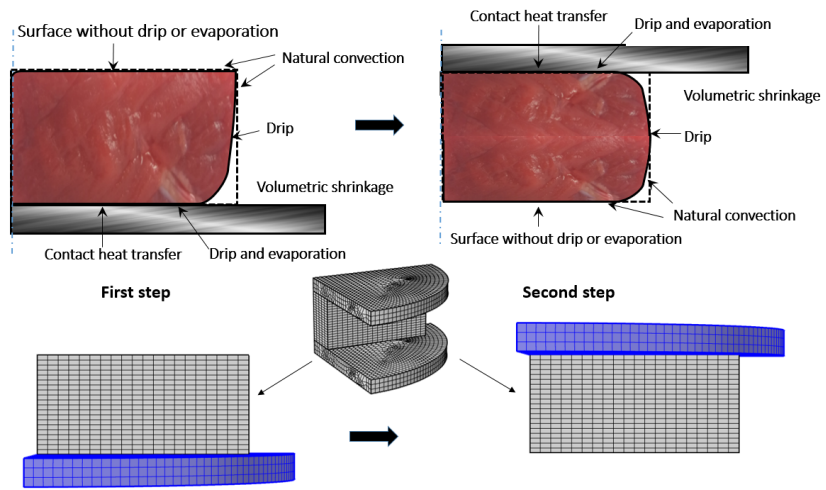


Figure 3: Finite element model and strategy defined for the turned over meat.

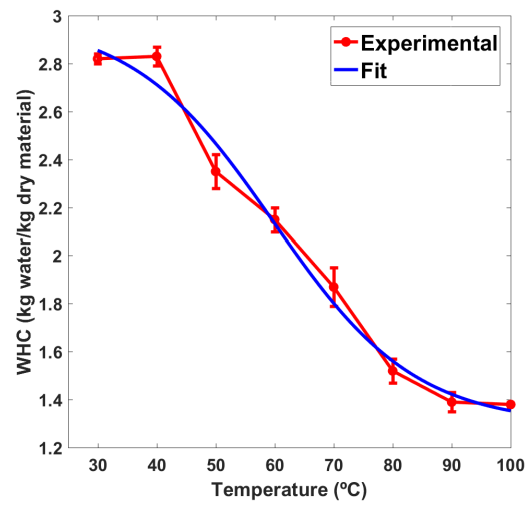


Figure 4: Water Holding Capacity as a function of temperature T for beef meat.

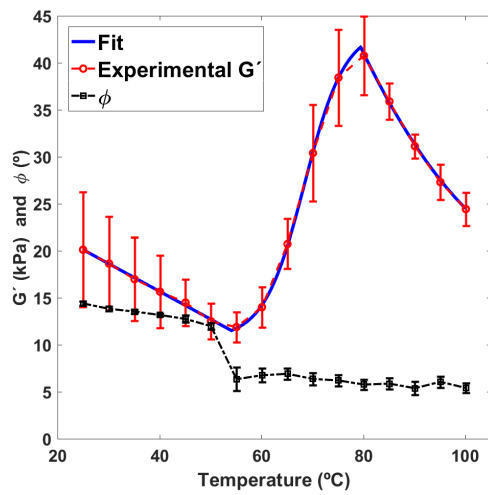


Figure 5: Storage modulus, G' (kPa), and phase angle, ϕ (°), for beef *M. Longissimus dorsi* as a function of cooking temperature. Experimental values indicated by symbols and estimated values by the blue line.

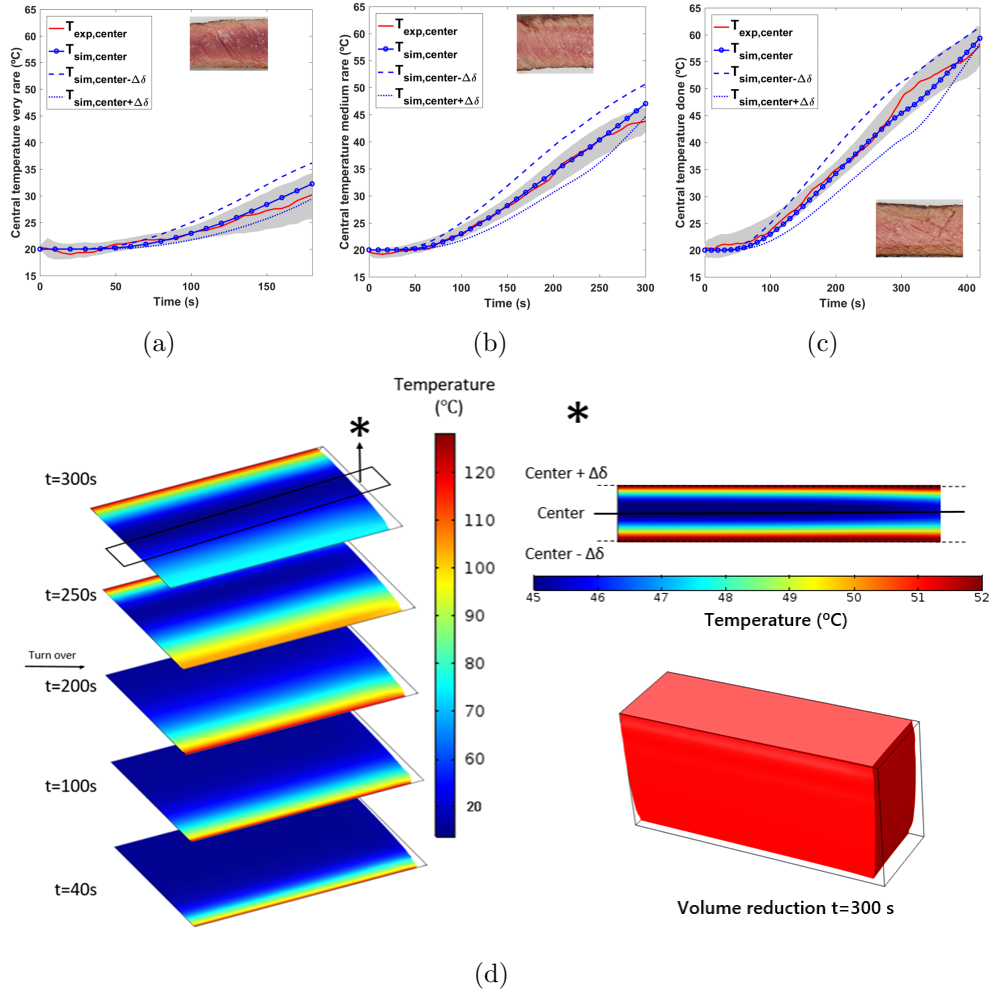


Figure 6: Central temperature evolution for 19 mm of thickness: a) very rare, b) medium rare, c) done cooking degree. d) Temperature distribution in a cross section for different times in case of medium rare cooking degree, central section temperature gradient considering the sensor located at $\Delta\delta = \pm 1$ mm, and volume reduction.

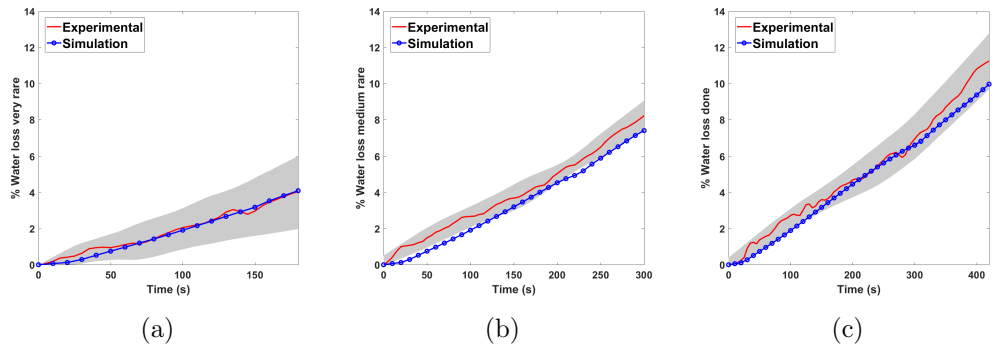


Figure 7: Water loss evolution for 19 mm of thickness: a) very rare, b) medium rare, c) done cooking degrees.

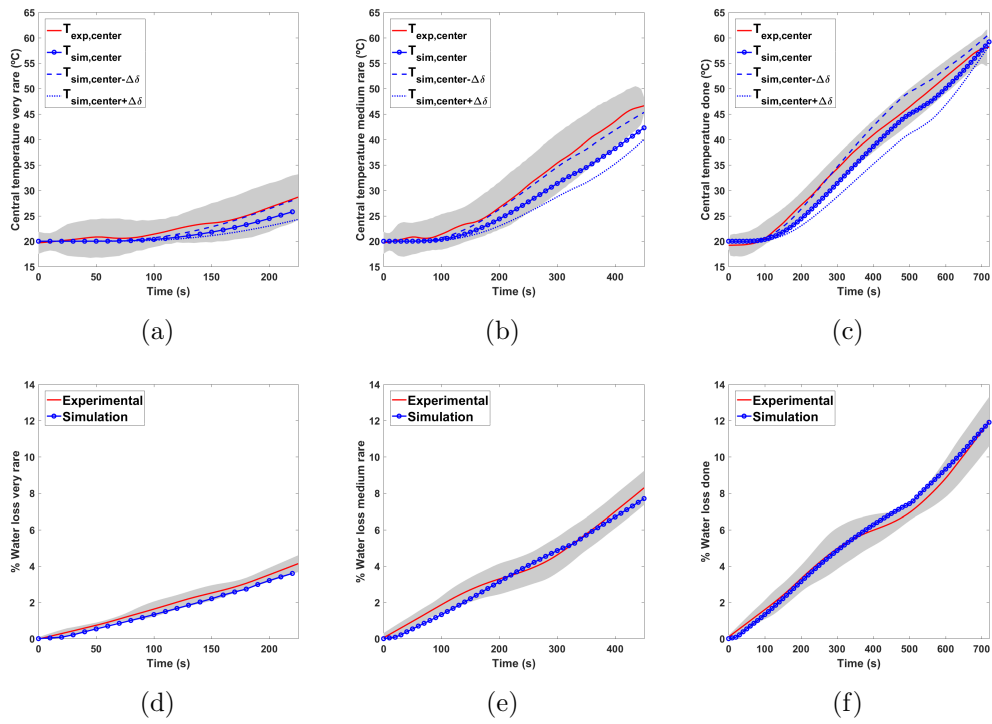


Figure 8: Central temperature evolution for 26 mm thickness: a) very rare, b) medium rare, c) done cooking degrees. Water loss evolution for d) very rare, e) medium rare, f) done.

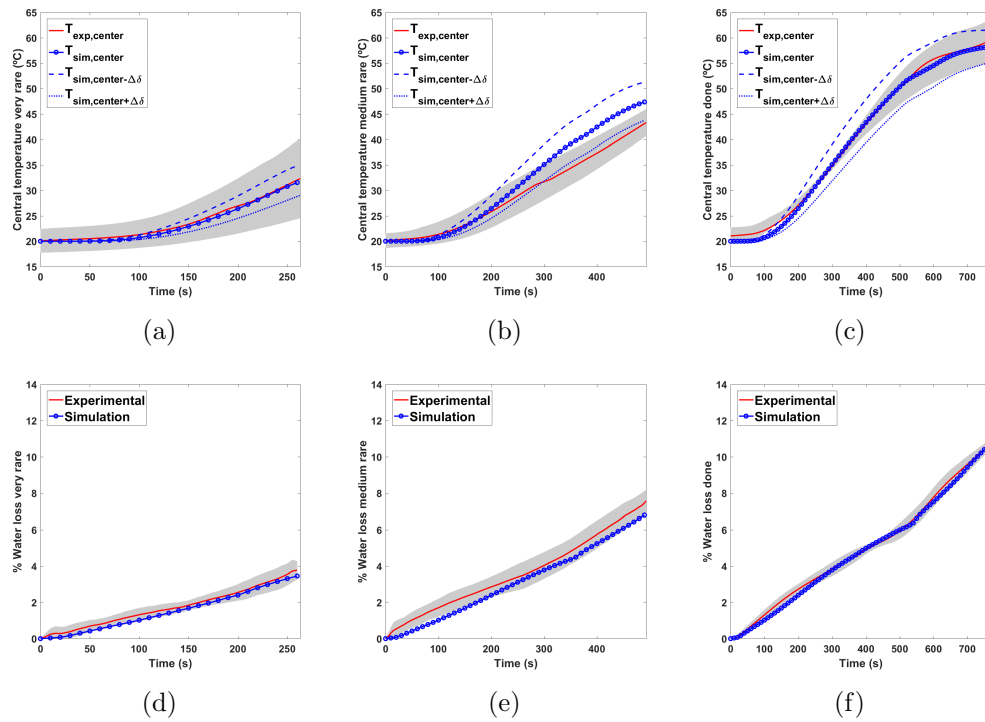
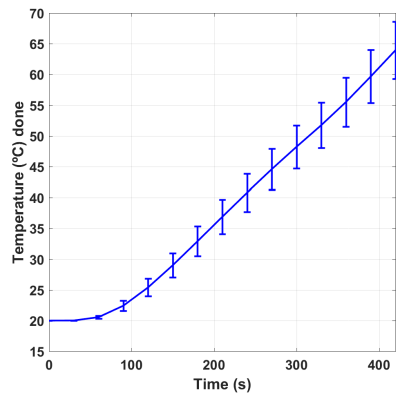
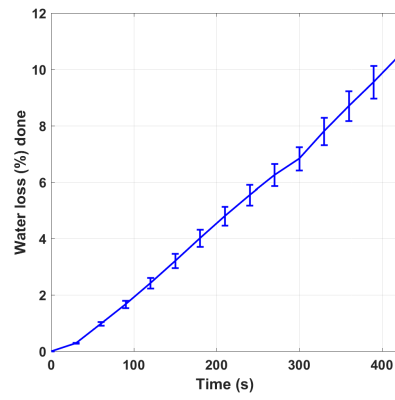


Figure 9: Central temperature evolution for 34 mm thickness: a) very rare, b) medium rare, c) done cooking degrees. Water loss evolution for d) very rare, e) medium rare, f) done.



(a)



(b)

Figure 10: Sensitivity analysis of a) central temperature and b) water loss regarding variations in thickness for the done degree.