

Materials for Quantum Technology



PERSPECTIVE

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Nanoscale direct-write fabrication of superconducting devices for application in quantum technologies

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Abstract

In this Perspective article, we evaluate the current state of research on the use of focused electron and ion beams to directly fabricate nanoscale superconducting devices with application in quantum technologies. First, the article introduces the main superconducting devices and their fabrication by means of standard lithography techniques such as optical lithography and electron beam lithography. Then, focused ion beam patterning of superconductors through milling or irradiation is shown, as well as the growth of superconducting devices by means of focused electron and ion beam induced deposition. We suggest that the key benefits of these resist-free direct-growth techniques for quantum technologies include the ability to make electrical nanocontacts and circuit edit, fabrication of high-resolution superconducting resonators, creation of Josephson junctions and superconducting quantum interference device (SQUIDs) for on-tip sensors, patterning of high- T_c SQUIDs and other superconducting circuits, and the exploration of fluxtronics and topological superconductivity.

1. Superconducting devices in quantum technologies and their fabrication

Superconductivity, discovered in 1911 by H K Onnes, is a relative rare emergent phenomenon, quantum in nature and with macroscopic implications such as the lack of electrical resistance to the passage of electrical current [1]. Superconductors, beyond representing an excellent playground to investigate fundamental physical phenomena [2], are crucial materials in today's and future's technology [3, 4]. In quantum technologies, superconductors have found applications in quantum computing and in quantum sensing. At the very heart of quantum computing, one can find Josephson junctions (JJs), in which two close superconductors (S) are separated either by an insulator (I), SIS, a normal metal (N), SNS, or a different superconductor (s), SsS [5, 6]. Described for the first time by B D Josephson in 1962, JJs display a rich variety of physical phenomena, with the existence of an electrical supercurrent as one of the key features [7]. Central to the interest of superconductors for quantum technologies is the fact that the ground state of a superconductor is a coherent state with a single phase [8]. In the BCS theory of superconductivity, the electrical current is carried by Cooper pairs that condense into the same ground (quantum) state. Cooper pairs can flow through a JJ, and the electrical behaviour of the JJ is determined by the value of the superconducting phase on both sides of the junction. In addition, a JJ has a strong interaction with microwave radiation [7, 9]. In the scientific literature, one can find a rich variety of quantum devices based on superconductors, which can be classified according to their final application into (a) superconducting circuits for quantum computing and (b) quantum sensors based on superconductors.

In the (a) category, JJs contribute to realize qubits thanks to the fact that the JJs endow the circuit with non-linearity without introducing dissipation or dephasing [10–12]. The non-linearity leads to non-equidistant energy levels, as required for qubits. Various practical implementations of superconducting-based qubits have been built, including the transmon, the fluxonium, the quntronium and the hybrid qubits [12, 13]. Besides, in these and other qubit architectures, superconducting materials can

provide key-enabling circuit features such as the realization of high-frequency resonators and bias lines [14, 15]. Moreover, proposals of Majorana-based quantum computing based on topological superconductivity induced by proximity effects have been put forward [16, 17]. On the other hand, an intense research activity is under way to overcome the materials challenges existing for the realization of practical quantum computers [18]. In the (b) category, one can find superconducting sensors such as superconducting quantum interference device (SQUIDs) [19–21], transition-edge detectors [22, 23], nanowire single-photon detectors [24, 25] and kinetic inductance detectors [26].

The fabrication of superconducting devices call for the use of micro- and nano-fabrication techniques, leveraged from their use in semiconductor industry or in micro/nano-technology. In general, these techniques are based on top-down multi-step lithography processes that can be additive or subtractive and are used in combination with thin-film deposition techniques. Aluminum (Al) and niobium (Nb) are frequently used as superconducting materials due to their good behaviour at the typical working temperature, in the mK range. The technology of fabrication of JJs based on these two materials is mature, which facilitates its application to circuits designed for quantum computing [27, 28]. However, defects at the surface of the devices or on the substrate are important sources of decoherence [29–32]. For quantum sensors and key-enabling features, there is a broader choice of superconducting materials beyond Al and Nb. One of the most popular superconducting materials is YBCO ($\text{YBa}_2\text{Cu}_3\text{O}_{7-x}$), which stands out for its high T_C (~ 90 K) and allows for JJs and SQUIDs up to temperatures close to T_C [19]. The patterning of exotic superconductors such as LAO/STO interfaces [33] and proximitized graphene [34] into JJs has also been achieved, as well as JJs and SQUIDs based on proximitized topological insulators [35].

For the fabrication of these superconducting devices, various lithographic techniques have been successfully applied. A few representative examples can be cited, without pretending to cover an immense topic that is not the main focus of the current article:

- Photolithography has been used for integrating superconducting routing levels on a Si-based interposer with the aim of electrically coupling spin qubit arrays with cryo-CMOS control and read-out circuits [36].
- Electron beam lithography is a very popular fabrication technique in quantum technologies and has been applied to fabricate Josephson persistent-current qubits [37], flux qubits [38], phase qubits [39], etc. The Sycamore processor, based on an array of transmon qubits, has been fabricated by means of 14 lithography layers utilizing both, optical and electron beam lithography [28].
- Stencil mask plus shadow evaporation technique has been used to fabricate artificial topological superconductors showing Majorana bound states [40].
- Direct-write techniques have been utilized in various ways for quantum technologies and will be the focus of the next section, which constitutes the central discussion point of the current perspective article.

2. Nanoscale direct-write fabrication of superconducting devices

In sharp contrast to optical or electron beam lithography, nanoscale direct-write fabrication techniques do not require the use of sacrificial resists or etching/lift-off steps, avoiding contamination issues arising from organic residues. The level of maturity reached by optical and electron beam lithography is higher than that of direct-write fabrication, which justifies their preferred use at this moment. However, in some applications requiring nanoscale superconductors, standard optical or electron beam lithography techniques may not meet the requirements in terms of resolution, substrate compatibility, geometry, etc, which opens up the possibility of using alternative nanofabrication strategies based on focused electron and ion beams. In the following, we will examine some examples published in recent years where these alternative techniques have been successfully applied.

2.1. Focused ion beam (FIB) patterning of superconductors

FIB is well suited for high-resolution removal of material through local sputtering, which has been widely applied to pattern superconductors and fabricate various types of superconducting micro/nano-structures and devices. The following strategies can be found in literature:

- By means of Ga^+ -FIB milling on superconducting MgB_2 with $T_C \sim 40$ K [41], planar JJ [42–44] as well as SQUIDs [45] were fabricated. JJ patterning was also achieved by Ga^+ -FIB milling of high- T_C superconductors such as BISCCO [46] and YBCO [47–50]. On YBCO, it is possible to use Ga^+ -FIB milling to create nanowires [51] and sub-micron features [52] as well as full SQUID nanodevices [53].
- In a different approach, Ga^+ -FIB patterning of single crystals has been achieved, allowing the investigation of anisotropic superconducting properties in $\text{SmFeAs}(\text{F}, \text{O})$, with $T_C = 54$ K [54], the spontaneous emergence of JJs in homogeneous rings of single-crystal Sr_2RuO_4 [55] and tailored superconducting landscapes [56].

- In the quest for advanced scanning-SQUID sensors, Ga⁺-FIB patterning of a thin Nb layer grown on a cantilever has been performed. The resulting SQUID-on-tip (SOT) sensor has been used to image small magnetic signals with high lateral resolution [57]. Moreover, such SOT sensors have been applied to image the magnetic flux arising from a superconducting qubit [58].
- Superconducting microwave resonators in the proximity of qubits are of great interest to control them, which can be fabricated by Ga⁺-FIB [59, 60] as well as by Ne⁺-FIB with a better resolution [61]. For milling purposes, Ga⁺-FIB is capable of higher throughput compared to Ne⁺-FIB and He⁺-FIB, but the use of these light ions is preferred for high resolution given the smaller ion beam spot and the weaker interaction with the material to mill [62].

Remarkably, He⁺-FIB irradiation using low doses have been used to create planar JJs and SQUIDs on YBCO [63]. The procedure allows reaching 10 nm resolution in the patterning of JJs [64, 65]. Using this technology, a low-power high-T_C superconducting single flux quantum circuit has been achieved [66], with potential applications for memory, mixers, digital sensor readouts, switches for routers, and high-speed computing.

2.2. Direct growth of superconducting devices by focused electron and ion beam induced deposition (FEBID and FIBID)

FEBID and FIBID respectively, are direct-write resist-free nanolithography techniques that enable the growth of high-resolution nano- and micro-structures [67, 68]. They rely on a gas precursor that is injected into the area of interest and decomposed by a focused electron or ion beam, giving rise to deposits exhibiting functional properties such as tunable electrical conductivity (insulating, semiconducting or conducting behaviour) [69, 70], ferromagnetism [71, 72], nano-optical or photonic behaviour [73, 74], superconductivity [75, 76], robust structural and mechanical properties [77, 78], etc.

Since 2004, when superconductivity ($T_C = 5.2$ K) was discovered in W-C deposits by FIBID using the W(CO)₆ precursor [75], a high number of publications have reported the use of FEBID and FIBID for growing superconducting structures, as recently reviewed in detail by our group [79]. The reader is invited to read that publication in order to find all types of reports on the topic, whereas here, we will focus on applications of superconducting deposits by FEBID and FIBID in the field of quantum technologies. In the following, we will highlight a few results within this domain:

- On W-C nanowires grown by FIBID, magnetotransport results below T_C have been interpreted as due to the presence of phase slips and quantum phase transitions [80]. Interestingly, a laterally-applied gate voltage in W-C nanowires allows tuning a superconducting to normal-state transition [81].
- In the arena of fluxtronics, a rich and far-reaching literature has reported the behaviour of superconducting vortices on W-C FIBID deposits. Whereas the first publications focused on the properties of the Abrikosov vortex lattice against changes in temperature and magnetic field [82, 83] and the effects caused by the built-in disorder [84–86], subsequent studies addressed the formation of a single row of vortices in ultra-narrow W-C nanowires [87] and its manipulation by means of Lorentz forces [88, 89], including the discovery of ultra-fast vortex movement on Nb-C nanowires [90].
- More recently, the fabrication of JJs and SQUIDs based on FEBID and FIBID deposits has been achieved. By using W-C deposits grown by FEBID under high and low electron current, superconducting electrodes connected by normal electrodes have been created, with Shapiro steps confirming the formation of JJs [91]. Also, arrays of Nb-C JJs have been deposited by FIBID [92]. In addition, nanoSQUIDs based on W-C deposits grown by FIBID have been fabricated with Dayem-bridge-type geometry [93]. Such nanoSQUIDs are expected to be directly grown on cantilevers for scanning-on-tip devices, which would allow sensing small magnetic fields, currents and dissipation with high lateral resolution, as mentioned in the previous section [57]. Interestingly, W-C deposits have been applied to the editing of superconducting circuits based on other superconductors [94].
- W-C FIBID deposits have been frequently used to induce superconductivity by proximity effect on other materials such as graphene [95], bismuth [96, 97], copper and cobalt [98], gold [99] and Bi₂Se₃ [100]. In the last case, topological superconductivity was searched for Majorana-based quantum computing applications. In this topic, it is interesting to note that the critical magnetic field B_{C2} is very high in W-C FIBID deposits, with reports showing values up to 11 T [101].
- FEBID and FIBID excel in the growth of three-dimensional nanostructures [102, 103], which in general is not possible with other nanolithography techniques. In this topic, our group has successfully shown that superconducting W-C deposits with nanotube [104] and nanohelix [105] geometries can be grown, leading to a noticeable interplay of the vortex lattice with these unconventional geometries. In this regard, a perspective article has been recently published on superconductivity in curved 3D nanoarchitectures [106].

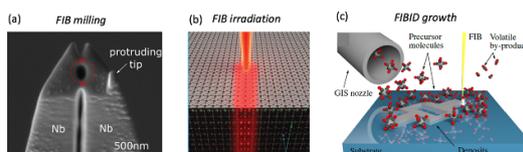


Figure 1. (a) NanoSQUID fabricated on a commercial AFM cantilever through FIB milling of a deposited 50 nm Nb film. Reprinted figure with permission from [57], Copyright (2022) by the American Physical Society. (b) Sketch illustrating the local irradiation of a high- T_c YBCO film by means of a He^+ -FIB in order to directly create a JJ. Reproduced from [63], with permission from Springer Nature. (c) Sketch of the direct growth of a nanoSQUID using the FIBID technique. A detailed description of the process has been published in Sigloch *et al*, *Nanoscale Advances* 4, 4628 (2022) [93].

In figure 1, three of the devices discussed in section 2 are shown as examples of the current capabilities of direct-write fabrication of superconducting devices for quantum technologies.

3. Outlook

Optical and electron beam lithography techniques are mature techniques for the fabrication of reproducible and reliable Al-based and Nb-based superconducting devices applied in quantum technologies. Despite these being the preferred lithography techniques and the preferred superconducting materials in this domain, the use of focused electron and ion beams for nanoscale direct-write fabrication of superconducting devices is nevertheless increasing. In this regard, several strategies can be used, such as FIB milling, FIB irradiation and FEBID/FIBID growth of superconductors. This set of techniques (FIB, FEBID, FIBID) is particularly well suited for obtaining devices with high lateral resolution and for building devices that rely on unusual geometries and unconventional substrates. Thus, they represent a convenient approach to create a nanopatterned superconducting material on a targeted location without the burden of conventional multi-step processes and avoiding the residues caused by the use of sacrificial resists. On the other hand, ion implantation, especially if Ga^+ -FIB is used, can be disadvantageous when used on particular materials [107]. Although these techniques present an intrinsic difficulty for wafer-scale patterning given the slow movement of the ion and electron beams, in the current state of the quantum technology some opportunities exist. Here below, we summarize some niches within the field of quantum technologies in which direct patterning by focused electron and ion beams could make an impact, as well as some of the foreseeable challenges that will be encountered.

- (1) *Electrical nanocontacting and circuit edit.* Similarly to the case of semiconductor industry [108, 109], the direct use of focused electron and ion beams to remove or to add materials locally is applicable to create or reconfigure electrical connections in a superconducting circuit. The fact that superconducting materials themselves can be directly grown by FEBID/FIBID represents an added value. Challenges here are the relatively high electrical resistance of the grown materials and the reproducibility of the composition and physical properties of the deposited materials [79].
- (2) *High-resolution superconducting resonators.* FIB milling is appropriate to define constriction-type weak links on superconductors for frequency-tunable magnetic-field-resilient high-quality resonators in the microwave range, which are of interest in hybrid superconducting-spin systems [59, 61]. The limited milling resolution provided by Ga^+ FIB sources can be overcome by the use of He^+ - Ne^+ FIB sources and other new ion sources. It is nevertheless foreseeable that commercial quantum devices based on this hybrid approach would call for a wafer-scale process being fully compatible with optical and/or electron beam lithography.
- (3) *JJs and SQUIDs for on-tip sensors.* FIB-based milling [57], irradiation [63] and deposition [93] seem convenient to create superconducting sensors on tips and cantilevers, in particular JJs and SQUIDs, with the potential to investigate relevant physical properties of materials and devices at the nanoscale [58]. These specialized sensors could represent a niche for FIB-based processing given that the use of standard lithography might be possible here, but difficult for up-scaling [110, 111]. However, further developments are still needed to create a marketable product with sufficient number of end users.
- (4) *High- T_c SQUIDs and other superconducting circuits.* Whereas the use of very low temperatures is recommended for quantum computing in order to minimize decoherence, other applications such as sensing do not have this limitation. In this latter case, YBCO-based SQUIDs patterned either by FIB milling [53] or by FIB irradiation [65] have been demonstrated. Moreover, the reported high- T_c superconducting single flux quantum circuit is promising for quantum logic above liquid helium

- temperature [66]. However, this approach is restricted to a few research groups and still far from the maturity and fabrication throughput required by industry.
- (5) *Fluxtronics*. The fact that a superconducting vortex embodies a single flux quantum and behaves as a particle when submitted to an electric current opens the way for sensing and logic applications based on vortices [112, 113]. FIB-based devices have demonstrated their potential in this field, including the long-range (10 μm) coherent vortex transfer [88], the ultra-fast vortex displacement [90] and the fabrication of 3D fluxtronic circuits [105], but further work is needed to substantiate the true competitiveness of fluxtronics in quantum applications.
 - (6) *Topological superconductivity*. With topological superconductivity being a holy grail for Majorana-based quantum computing [16, 17], the use of FEBID/FIBID-grown superconducting deposits capable of inducing local superconductivity by proximity effect is valuable, as already demonstrated in literature [96, 97]. On the other hand, FEBID/FIBID techniques are not appropriate to achieve high-quality epitaxial interfaces between semiconductor nanowires and superconductors, as standard lithography techniques have recently demonstrated [114].

As a concluding remark, let us suggest that we consider direct-write techniques such as FIB milling, FIB irradiation and FEBID/FIBID valuable for quantum technologies in the following domains: prototyping (*electrical nanocontacting and circuit edit, high-resolution superconducting resonators, high-Tc SQUIDs and other superconducting circuits*), exploration of new effects (in *fluxtronics* and in *topological superconductivity*) and niche fabrication (*JJs and SQUIDs for on-tip sensors*).

Data availability statement

No new data were created or analysed in this study.

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References

- [1] Van Delft D and Kes P 2010 The discovery of superconductivity *Phys. Today* **63** 38–43
- [2] Fradkin E, Kivelson S A and Tranquada J M 2015 Colloquium: theory of intertwined orders in high temperature superconductors *Rev. Mod. Phys.* **87** 457–82
- [3] Aarnink R and Overweg J 2012 Magnetic resonance imaging: a success story for superconductivity *Europhys. News* **43** 26–29
- [4] Huguet M 1997 The ITER magnet system *Fusion Eng. Des.* **36** 23–32
- [5] Gross R, Alff L, Beck A, Proehlich M, Koelle D and Marx A 1997 Physics and technology of high temperature superconducting Josephson junctions *IEEE Trans. Appl. Supercond.* **7** 2929–35
- [6] Tafuri F and Kirtley J R 2005 Weak links in high critical temperature superconductors *Rep. Prog. Phys.* **68** 2573–663
- [7] Josephson B D 1964 Coupled superconductors *Rev. Mod. Phys.* **36** 216–20
- [8] Martinis J M, Devoret M H and Clarke J 1985 Energy-level quantization in the zero-voltage state of a current-biased Josephson junction *Phys. Rev. Lett.* **55** 1543–6
- [9] Shapiro S 1963 Josephson currents in Superconducting tunneling: the effect of microwaves and other observations *Phys. Rev. Lett.* **11** 80–82
- [10] Devoret M H and Schoelkopf R J 2013 Superconducting circuits for quantum *Science* **339** 1169–75
- [11] Wendin G 2017 Quantum information processing with superconducting circuits: a review *Rep. Prog. Phys.* **80** 106001
- [12] Kockum A F and Nori F 2019 Quantum bits with Josephson junctions *Springer Ser. Mater. Sci.* **286** 703–41
- [13] Kjaergaard M, Schwartz M E, Braumüller J, Krantz P, Wang J I J, Gustavsson S and Oliver W D 2020 Superconducting qubits: current state of play *Annu. Rev. Condens. Matter Phys.* **11** 369–95
- [14] Clarke J and Wilhelm F K 2008 Superconducting quantum bits *Nature* **453** 1031–42
- [15] Klein N 2002 High-frequency applications of high-temperature superconductor thin films *Rep. Prog. Phys.* **65** 1387–425
- [16] Lutchyn R M, Bakkers E P A M, Kouwenhoven L P, Krogstrup P, Marcus C M and Oreg Y 2018 Majorana zero modes in superconductor-semiconductor heterostructures *Nat. Rev. Mater.* **3** 52–68

- [17] Sau J D, Lutchyn R M, Tewari S and Das Sarma S 2010 Generic new platform for topological quantum computation using semiconductor heterostructures *Phys. Rev. Lett.* **104** 040502
- [18] Goh K E J, Krivitsky L A and Polla D L 2022 Quantum technologies for engineering: the materials challenge *Mater. Quantum Technol.* **2** 013002
- [19] Koelle D, Kleiner R, Ludwig F, Dantsker E and Clarke J 1999 High-transition-temperature superconducting quantum interference devices *Rev. Mod. Phys.* **71** 631–86
- [20] Granata C and Vettoliere A 2016 Nano superconducting quantum interference device: a powerful tool for nanoscale investigations *Phys. Rep.* **614** 1–69
- [21] Faley M I, Dammers J, Maslennikov Y V, Schneiderman J F, Winkler D, Koshelets V P, Shah N J and Dunin-Borkowski R E 2017 High-Tc SQUID biomagnetometers *Supercond. Sci. Technol.* **30** 083001
- [22] Cabrera B, Clarke R M, Colling P, Miller A J, Nam S and Romani R W 1998 Detection of single infrared, optical, and ultraviolet photons using superconducting transition edge sensors *Appl. Phys. Lett.* **73** 735–7
- [23] Lita A E, Reddy D V, Verma V B, Mirin R P and Nam S W 2022 Development of superconducting single-photon and photon-number resolving detectors for quantum applications *J. Light Technol.* **40** 7578–97
- [24] Chang J *et al* 2021 Detecting telecom single photons with $99.5\text{--}2.07 + 0.5\%$ system detection efficiency and high time resolution *APL Photonics* **6** 036114
- [25] Steinhauer S, Gyger S and Zwiller V 2021 Progress on large-scale superconducting nanowire single-photon detectors *Appl. Phys. Lett.* **118** 100501
- [26] Szypryt P *et al* 2017 Large-format platinum silicide microwave kinetic inductance detectors for optical to near-IR astronomy *Opt. Express* **25** 25894
- [27] Takeuchi N, Nagasawa S and Ando T 2017 Adiabatic quantum-flux-parametron cell library designed using a 10kA cm^{−2} niobium fabrication process *Supercond. Sci. Technol.* **30** 035002
- [28] Arute F *et al* 2019 Quantum supremacy using a programmable superconducting processor *Nature* **574** 505–11
- [29] Oliver W D and Welander P B 2013 Materials in superconducting quantum bits *MRS Bull.* **38** 816–25
- [30] Giustino F *et al* 2022 The 2021 quantum materials roadmap *J. Phys. Mater.* **3** 042006
- [31] de Graaf S E, Un S, Shard A G and Lindström T 2022 Chemical and structural identification of material defects in superconducting quantum circuits *Mater. Quantum Technol.* **2** 032001
- [32] McRae C R H, Wang H, Gao J, Vissers M R, Brecht T, Dunswoth A, Pappas D P and Mutus J 2020 Materials loss measurements using superconducting microwave resonators *Rev. Sci. Instrum.* **91** 091101
- [33] Singh G, Lesne E, Winkler D, Claeson T, Bauch T, Lombardi F, Caviglia A D and Kalaboukhov A 2021 Nanopatterning of weak links in superconducting oxide interfaces *Nanomaterials* **11** 398
- [34] Huang K F, Ronen Y, Mélin R, Feinberg D, Watanabe K, Taniguchi T and Kim P 2022 Evidence for 4e charge of cooper quartets in a biased multi-terminal graphene-based Josephson junction *Nat. Commun.* **13** 3032
- [35] Kurter C, Finck A D K, Hor Y S and Van Harlingen D J 2015 Evidence for an anomalous current-phase relation in topological insulator Josephson junctions *Nat. Commun.* **6** 7130
- [36] Thomas C *et al* 2022 Superconducting routing platform for large-scale integration of quantum technologies *Mater. Quantum Technol.* **2** 035001
- [37] Mooij J E, Orlando T P, Levitov L and Tian L 1999 Josephson persistent-current qubit *Science* **285** 1036–40
- [38] Yan F *et al* 2016 The flux qubit revisited to enhance coherence and reproducibility *Nat. Commun.* **7** 12964
- [39] Lecocq F, Pop I M, Peng Z, Matei I, Crozes T, Fournier T, Naud C, Guichard W and Buisson O 2011 Junction fabrication by shadow evaporation without a suspended bridge *Nanotechnology* **22** 315302
- [40] Schüffelgen P *et al* 2019 Selective area growth and stencil lithography for *in situ* fabricated quantum devices *Nat. Nanotechnol.* **14** 825–31
- [41] Canfield P C and Crabtree G W 2003 Magnesium diboride : better late with a superconducting transition temperature of 40 K *Phys. Today* **56** 34–40
- [42] Burnell G, Kang D J, Lee H N, Moon S H, Oh B and Blamire M G 2001 Planar superconductor-normal-superconductor Josephson junctions in MgB₂ *Appl. Phys. Lett.* **79** 3464–6
- [43] Bell C, Burnell G, Kang D J, Hadfield R H, Kappers M J and Blamire M G 2003 Fabrication of nanoscale heterostructure devices with a focused ion beam microscope *Nanotechnology* **14** 630–2
- [44] Burnell G, Kang D J, Ansell D A, Lee H N, Moon S H, Tarte E J and Blamire M G 2002 Directly coupled superconducting quantum interference device magnetometer fabricated in magnesium diboride by focused ion beam *Appl. Phys. Lett.* **81** 102–4
- [45] Brinkman A, Veldhuis D, Mijatovic D, Rijnders G, Blank D H A, Hilgenkamp H and Rogalla H 2001 Superconducting quantum interference device based on MgB₂ nanobridges *Appl. Phys. Lett.* **79** 2420–2
- [46] Kim S J, Latyshev Y I and Yamashita T 1999 Submicron stacked-junction fabrication from Bi₂Sr₂CaCu₂O_{8+δ} whiskers by focused-ion-beam etching *Appl. Phys. Lett.* **74** 1156–8
- [47] Kang D J *et al* 2002 Realization and properties of YBa₂Cu₃O_{7-δ} Josephson junctions by metal masked ion damage technique *Appl. Phys. Lett.* **80** 814–6
- [48] Testa G, Monaco A, Esposito E, Sarnelli E, Kang D J, Mennema S H, Tarte E J and Blamire M G 2004 Midgap state-based π-junctions for digital applications *Appl. Phys. Lett.* **85** 1202–4
- [49] Testa G, Monaco A, Sarnelli E, D’Agostino A, Kang D J, Tarte E J, Mennema S H, Bell C and Blamire M G 2004 Submicron YBa₂Cu₃O_{7-x} bicrystal grain boundary junctions by focused ion beam *Supercond. Sci. Technol.* **17** 287–90
- [50] Warburton P A, Kuzhakhmetov A R, Bell C, Burnell G, Blamire M G, Wu H, Grovenor C R M and Schneidewind H 2003 Sub-micron thin film intrinsic Josephson junctions *IEEE Trans. Appl. Supercond.* **13** 821–4
- [51] Rouco V, Massarotti D, Stornaiuolo D, Papari G P, Obradors X, Puig T, Tafuri F and Palau A 2018 Vortex lattice instabilities in YBa₂Cu₃O_{7-x} nanowires *Materials* **11** 211
- [52] Rouco V, Córdoba R, De Teresa J M, Rodríguez L A and Navau C 2017 Competition between superconductor—ferromagnetic stray magnetic fields in YBa₂Cu₃O_{7-x} films pierced with Co nano-rods *Sci. Rep.* **7** 5663
- [53] Schwarz T, Wölbling R, Reiche C F, Müller B, Martínez-Pérez M J, Mühl T, Büchner B, Kleiner R and Koelle D 2015 Low-noise YBa₂Cu₃O₇ nano-SQUIDs for performing magnetization-reversal measurements on magnetic nanoparticles *Phys. Rev. Appl.* **3** 044011
- [54] Moll P J W, Puzniak R, Balakirev F, Rogacki K, Karpinski J, Zhitadlo N D and Batlogg B 2010 High magnetic-field scales and critical currents in SmFeAs(O,F) crystals *Nat. Mater.* **9** 628–33

- [55] Yasui Y, Lahabi K, Becerra V F, Fermin R, Anwar M S, Yonezawa S, Terashima T, Milošević M V, Aarts J and Maeno Y 2020 Spontaneous emergence of Josephson junctions in homogeneous rings of single-crystal Sr_2RuO_4 *npj Quantum Mater.* **5** 21
- [56] Bachmann M D 2019 Spatial control of heavy-fermion superconductivity in CeIrIn_5 *Science* **366** 221–6
- [57] Wyss M, Bagani K, Jetter D, Marchiori E, Vervelaki A, Gross B, Ridderbos J, Gliga S, Schönenberger C and Poggio M 2022 Magnetic, thermal, and topographic imaging with a nanometer-scale SQUID-on-lever scanning probe *Phys. Rev. Appl.* **17** 034002
- [58] Marchiori E, Ceccarelli L, Rossi N, Romagnoli G, Herrmann J, Besse J C, Krinner S, Wallraff A and Poggio M 2022 Magnetic imaging of superconducting qubit devices with scanning SQUID-on-tip *Appl. Phys. Lett.* **121** 052601
- [59] Jenkins M D, Naether U, Ciria M, Sesé J, Atkinson J, Sánchez-Azqueta C, Del Barco E, Majer J, Zueco D and Luis F 2014 Nanoscale constrictions in superconducting coplanar waveguide resonators *Appl. Phys. Lett.* **105** 162601
- [60] Gimeno I *et al* 2020 Enhanced molecular spin-photon coupling at superconducting nanoconstrictions *ACS Nano* **14** 8707–15
- [61] Kennedy O W, Burnett J, Fenton J C, Constantino N G N, Warburton P A, Morton J J L and Dupont-Ferrier E 2019 Tunable Nb superconducting resonator based on a constriction nano-SQUID fabricated with a Ne focused ion beam *Phys. Rev. Appl.* **11** 014006
- [62] Bruchhaus L, Mazarov P, Bischoff L, Gierak J, Wieck A D and Hövel H 2017 Comparison of technologies for nano device prototyping with a special focus on ion beams: a review *Appl. Phys. Rev.* **4** 011302
- [63] Cybart S A, Cho E Y, Wong T J, Wehlin B H, Ma M K, Huynh C and Dynes R C 2015 Nano Josephson superconducting tunnel junctions in $\text{YBa}_2\text{Cu}_3\text{O}_{7-\delta}$ directly patterned with a focused helium ion beam *Nat. Nanotechnol.* **10** 598–602
- [64] Müller B, Karrer M, Limberger F, Becker M, Schröppel B, Burkhardt C J, Kleiner R, Goldobin E and Koelle D 2019 Josephson junctions and SQUIDs created by focused helium-ion-beam irradiation of $\text{YBa}_2\text{Cu}_3\text{O}_7$ *Phys. Rev. Appl.* **11** 044082
- [65] Li H, Cai H, Cho E Y, McCoy S J, Wang Y T, Lefebvre J C, Zhou Y W and Cybart S A 2020 High-transition-temperature nanoscale superconducting quantum interference devices directly written with a focused helium ion beam *Appl. Phys. Lett.* **116** 070601
- [66] Cai H, Li H, Cho E Y, Lefebvre J and Cybart S A 2021 $\text{YBa}_2\text{Cu}_3\text{O}_7$ -single flux quantum flip flop directly written with a focused helium ion beam *IEEE Trans. Appl. Supercond.* **31** 7200205
- [67] Utke I, Hoffmann P and Melngailis J 2008 Gas-assisted focused electron beam and ion beam processing and fabrication *J. Vac. Sci. Technol. B* **26** 1197
- [68] Van Dorp W F and Hagen C W 2008 A critical literature review of focused electron beam induced deposition *J. Appl. Phys.* **104** 081301
- [69] Fernández-Pacheco A, De Teresa J M, Córdoba R and Ibarra M R 2009 Metal-insulator transition in Pt-C nanowires grown by focused-ion-beam-induced deposition *Phys. Rev. B* **79** 174204
- [70] Schwalb C H *et al* 2010 A tunable strain sensor using nanogranular metals *Sensors* **10** 9847–56
- [71] De Teresa J M and Fernández-Pacheco A 2014 Present and future applications of magnetic nanostructures grown by FEBID *Appl. Phys. A* **117** 1645–58
- [72] Fernández-Pacheco A, Skoric L, De Teresa J M, Pablo-Navarro J, Huth M and Dobrovolskiy O V 2020 Writing 3D nanomagnets using focused electron beams *Materials* **13** 3774
- [73] Graells S, Acimović S, Volpe G and Quidant R 2010 Direct growth of optical antennas using e-beam-induced gold deposition *Plasmonics* **5** 135–9
- [74] Haverkamp C, Höflich K, Jäckle S, Manzoni A and Christiansen S 2017 Plasmonic gold helices for the visible range fabricated by oxygen plasma purification of electron beam induced deposits *Nanotechnology* **28** 055303
- [75] Sadki E S, Ooi S and Hirata K 2004 Focused-ion-beam-induced deposition of superconducting nanowires *Appl. Phys. Lett.* **85** 6206–8
- [76] Sengupta S, Li C, Baumier C, Kasumov A, Guéron S, Bouchiat H and Fortuna F 2015 Superconducting nanowires by electron-beam-induced deposition *Appl. Phys. Lett.* **106** 042601
- [77] Utke I, Michler J, Winkler R and Plank H 2020 Mechanical properties of 3D nanostructures obtained by focused electron/ion beam-induced deposition: a review *Micromachines* **11** 397
- [78] Córdoba R, Lorenzoni M, Pablo-Navarro J, Magén C, Pérez-Murano F and De Teresa J M 2017 Suspended tungsten-based nanowires with enhanced mechanical properties grown by focused ion beam induced deposition *Nanotechnology* **28** 445301
- [79] Orús P, Sigloch F, Sangiao S and De Teresa J M 2022 Superconducting materials and devices grown by focused ion and electron beam induced deposition *Nanomaterials* **12** 1367
- [80] Aloysius R P, Husale S, Kumar A, Ahmad F, Gangwar A K, Papanai G S and Gupta A 2019 Superconducting properties of tungsten nanowires fabricated using focussed ion beam technique *Nanotechnology* **30** 405001
- [81] Orús P, Fomin V M, De Teresa J M and Córdoba R 2021 Critical current modulation induced by an electric field in superconducting tungsten-carbon nanowires *Sci. Rep.* **11** 17698
- [82] Guillamón I, Suderow H, Vieira S, Fernández-Pacheco A, Sesé J, Córdoba R, De Teresa J M and Ibarra M R 2008 Nanoscale superconducting properties of amorphous W-based deposits grown with a focused-ion-beam *New J. Phys.* **10** 093005
- [83] Guillamón I, Suderow H, Fernández-Pacheco A, Sesé J, Córdoba R, De Teresa J M, Ibarra M R and Vieira S 2009 Direct observation of melting in a two-dimensional superconducting vortex lattice *Nat. Phys.* **5** 651–5
- [84] Guillamón I, Suderow H, Vieira S, Sesé J, Córdoba R, De Teresa J M and Ibarra M R 2011 Direct observation of stress accumulation and relaxation in small bundles of superconducting vortices in tungsten thin films *Phys. Rev. Lett.* **106** 077001
- [85] Guillamón I, Córdoba R, Sesé J, De Teresa J M, Ibarra M R, Vieira S and Suderow H 2014 Enhancement of long-range correlations in a 2D vortex lattice by an incommensurate 1D disorder potential *Nat. Phys.* **10** 851–6
- [86] Serrano I G, Sesé J, Guillamón I, Suderow H, Vieira S, Ibarra M R and De Teresa J M 2016 Thickness-modulated tungsten-carbon superconducting nanostructures grown by focused ion beam induced deposition for vortex pinning up to high magnetic fields *Beilstein J. Nanotechnol.* **7** 1698–708
- [87] Córdoba R *et al* 2013 Magnetic field-induced dissipation-free state in superconducting nanostructures *Nat. Commun.* **4** 1437
- [88] Córdoba R *et al* 2019 Long-range vortex transfer in superconducting nanowires *Sci. Rep.* **9** 12386
- [89] Orús P, Córdoba R, Hlawacek G and De Teresa J M 2021 Superconducting properties of in-plane W-C nanowires grown by He^+ focused ion beam induced deposition *Nanotechnology* **32** 085301
- [90] Dobrovolskiy O V, Vodolazov D Y, Porrati F, Sachser R, Bevs V M, Mikhailov M Y, Chumak A V and Huth M 2020 Ultra-fast vortex motion in a direct-write Nb-C superconductor *Nat. Commun.* **11** 3291
- [91] Blom T J, Mechielsen T W, Fermin R, Hesselberth M B S, Aarts J and Lahabi K 2021 Direct-write printing of Josephson junctions in a scanning electron microscope *ACS Nano* **15** 322–9
- [92] Porrati F, Jungwirth F, Barth S, Gazzadi G C, Frabboni S, Dobrovolskiy O V and Huth M 2022 Highly-packed proximity-coupled DC-Josephson junction arrays by a direct-write approach *Adv. Funct. Mater.* **32** 2203889

- [93] Sigloch F, Sangiao S, Orús P and de Teresa J M 2022 Direct-write of tungsten-carbide nanoSQUIDs based on focused ion beam induced deposition *Nanoscale Adv.* **4** 4628–34
- [94] Martínez-Pérez M J, Sesé J, Córdoba R, Luis F, Drung D and Schurig T 2009 Circuit edit of superconducting microcircuits *Supercond. Sci. Technol.* **22** 125020
- [95] Shailos A, Nativel W, Kasumov A, Collet C, Ferrier M, Guéron S, Deblock R and Bouchiat H 2007 Proximity effect and multiple Andreev reflections in few-layer graphene *EPL Europhys. Lett.* **79** 57008
- [96] Sangiao S, Casado L, Morellón L, Ibarra M R and De Teresa J M 2017 Proximity-induced superconductivity in bismuth nanostripes *J. Phys. D: Appl. Phys.* **50** 12LT02
- [97] Murani A *et al* 2017 Ballistic edge states in bismuth nanowires revealed by SQUID interferometry *Nat. Commun.* **8** 15941
- [98] Kompaniets M, Dobrovolskiy O V, Neetzel C, Begun E, Porrati F, Ensinger W and Huth M 2014 Proximity-induced superconductivity in crystalline Cu and Co nanowires and nanogranular Co structures *J. Appl. Phys.* **116** 073906
- [99] Wang J, Shi C, Tian M, Zhang Q, Kumar N, Jain J K, Mallouk T E and Chan M H W 2009 Proximity-induced superconductivity in nanowires: minigap state and differential magnetoresistance oscillations *Phys. Rev. Lett.* **102** 247003
- [100] Bhattacharyya B, Awana V P S, Senguttuvan T D, Ojha V N and Husale S 2018 Proximity-induced supercurrent through topological insulator based nanowires for quantum computation studies *Sci. Rep.* **8** 17237
- [101] Li C *et al* 2014 Magnetic field resistant quantum interferences in Josephson junctions based on bismuth nanowires *Phys. Rev. B* **90** 245427
- [102] Matsui S, Kaito T, Fujita J, Komuro M, Kanda K and Haruyama Y 2000 Three-dimensional nanostructure fabrication by focused-ion-beam chemical vapor deposition *J. Vac. Sci. Technol. B* **18** 3181
- [103] Fowlkes J D, Winkler R, Lewis B B, Stanford M G, Plank H and Rack P D 2016 Simulation-guided 3D nanomanufacturing via focused electron beam induced deposition *ACS Nano* **10** 6163–72
- [104] Córdoba R, Ibarra A, Maily D and De Teresa J M 2018 Vertical growth of superconducting crystalline hollow nanowires by He⁺ focused ion beam induced deposition *Nano Lett.* **18** 1379–86
- [105] Córdoba R, Maily D, Rezaev R O, Smirnova E I, Schmidt O G, Fomin V M, Zeitler U, Guillamón I, Suderow H and De Teresa J M 2019 Three-dimensional superconducting nanohelices grown by He⁺-focused-ion-beam direct writing *Nano Lett.* **19** 8597–604
- [106] Fomin V M and Dobrovolskiy O V 2022 A perspective on superconductivity in curved 3D nanoarchitectures *Appl. Phys. Lett.* **120** 090501
- [107] Gierak J, Ben Assayag G, Schneider M, Vieu C and Marzin J Y 1996 *Microelectron. Eng.* **30** 253–6
- [108] Bret T, Hofmann T and Edinger K 2014 Industrial perspective on focused electron beam-induced processes *Appl. Phys. A* **117** 1607–14
- [109] Mohiuddin T 2014 Focused ion beam (FIB) circuit edit *Electron. Device Fail. Anal.* **3** 20–23
- [110] Faley M I, Bikulov T I, Bosboom V, Golubov A A and Dunin-Borkowski R E 2021 Bulk nanomachining of cantilevers with Nb nanoSQUIDs based on nanobridge Josephson junctions *Supercond. Sci. Technol.* **34** 035014
- [111] Forrer L, Kamber A, Knoll A, Poggio M and Braakman F 2022 Electron-beam lithography of nanostructures at the tips of scanning probe cantilevers (arXiv:2209.11503)
- [112] Fazio R and Van der Zant H 2001 Quantum phase transitions and vortex dynamics in superconducting networks *Phys. Rep.* **355** 235–334
- [113] Wallraff A, Lukashenko A, Lisenfeld J, Kemp A, Fistul M V, Koval Y and Ustinov A V 2003 Quantum dynamics of a single vortex *Nature* **425** 155–8
- [114] Valentini M, Borovkov M, Prada E, Marti-Sanchez S, Botifoll M, Hofmann A, Arbiol J, Aguado R, San-Jose P and Katsaros G 2022 Majorana-like coulomb spectroscopy in the absence of zero bias peaks *Nature* **612** 442