



Enhanced light signal for the suppression of pile-up events in Mo-based bolometers for the $0\nu\beta\beta$ decay search.

A. Ahmine¹, A. Armato², I. Bandac³, L. Bergé⁴, J. M. Calvo-Mozota^{3,5}, P. Carniti⁶, M. Chapellier⁴, T. Dixon⁴, L. Dumoulin⁴, A. Giuliani⁴, Ph. Gras², F. Ferri², L. Imbert⁴, H. Khalife², P. Loaiza⁴, P. de Marcillac⁴, S. Marnieros⁴, C. A. Marrache-Kikuchi⁴, C. Nones², E. Olivieri^{4,a}, A. Ortiz de Solórzano⁷, G. Pessina⁶, D. V. Poda⁴, Th. Redon⁴, J. A. Scarpaci^{4,b}, M. Velázquez¹, A. Zolotarova²

¹ Université Grenoble Alpes, CNRS, Grenoble INP, SIMAP, 38402 Saint Martin d'Hères, France

² IRFU, CEA, Université Paris-Saclay, 91191 Gif-sur-Yvette, France

³ Laboratorio Subterráneo de Canfranc, 22880 Canfranc-Estación, Spain

⁴ Université Paris-Saclay, CNRS/IN2P3, IJCLab, 91405 Orsay, France

⁵ Escuela Superior de Ingeniería y Tecnología, Universidad Internacional de La Rioja, 26006 Logroño, Spain

⁶ INFN, Sezione di Milano Bicocca, 20126 Milan, Italy

⁷ Centro de Astropartículas y Física de Altas Energías, Universidad de Zaragoza, 50009 Zaragoza, Spain

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Abstract Random coincidences of events could be one of the main sources of background in the search for neutrino-less double-beta decay of ^{100}Mo with macro-bolometers, due to their modest time resolution. Scintillating bolometers as those based on Li_2MoO_4 crystals and employed in the CROSS and CUPID experiments can eventually exploit the coincident fast signal detected in a light detector to reduce this background. However, the scintillation provides a modest signal-to-noise ratio, making difficult a pile-up pulse-shape recognition and rejection at timescales shorter than a few ms. Neganov–Trofimov–Luke assisted light detectors (NTL-LDs) offer the possibility to effectively increase the signal-to-noise ratio, preserving a fast time-response, and enhance the capability of pile-up rejection via pulse shape analysis. In this article we present: (a) an experimental work performed with a Li_2MoO_4 scintillating bolometer, studied in the framework of the CROSS experiment, and utilizing a NTL-LD; (b) a simulation method to reproduce, synthetically, randomly coincident two-neutrino double-beta decay events; (c) a new analysis method based on a pulse-shape discrimination algorithm capable of providing high pile-up rejection efficiencies. We finally show how the NTL-LDs offer a balanced solution between performance and complexity to reach background index $\sim 10^{-4}$ counts/keV/kg/year with 280 g Li_2MoO_4 (^{100}Mo enriched) bolometers at 3034

keV, the $Q_{\beta\beta}$ of the double-beta decay, and target the goal of a next generation experiment like CUPID.

1 Introduction

The observation of the neutrino-less double-beta ($0\nu 2\beta$) decay would imply the violation of lepton number conservation and establish the Majorana nature of neutrino [1–4]. Cryogenic bolometers are very competitive detectors to search for this extremely rare process ($T_{1/2}^{0\nu 2\beta} > 10^{24} - 10^{26}$ years [5–13]) in a few theoretically and experimentally favorable nuclei. The lithium molybdate compound (Li_2MoO_4) has been experimentally demonstrated as one of the most promising materials to this end [12–17], thanks to the recent progress in the techniques to synthesize large, high-quality ^{100}Mo -enriched radio-pure scintillating single crystals [13, 15, 18–20], and providing excellent bolometric performances overall [16].

Both CROSS [21] and CUPID [22] experiments develop a technology based on Li_2MoO_4 macro-bolometers coupled to bolometric light detectors and use neutron-transmutation-doped Ge thermistors (NTD) [23] as sensors. These sensors can be produced in large numbers and they can be read out via simple, conventional, low-noise JFET-based electronics [24]. Their major drawback is an intrinsic slow (1–10 ms) response time, essentially due to (1) their high impedance at the optimal working point, (2) the gluing interface with

^a e-mail: emiliano.olivieri@ijclab.in2p3.fr (corresponding author)

^b e-mail: jean-antoine.scarpaci@ijclab.in2p3.fr

the crystal, and (3) the internal electron–phonon decoupling. Slow response time can lead to pile-up events mimicking single, normal events at the Q-value of the double-beta decay $Q_{\beta\beta}$ [18, 25]. The identification of these events is extremely important when searching for $0\nu 2\beta$ decay of ^{100}Mo : in fact, having the ^{100}Mo a relatively “short” two-neutrino double-beta ($2\nu 2\beta$) half-life ($T_{1/2}^{2\nu 2\beta} = 7.1 \cdot 10^{18}$ years [26]), this latter can bring a large background of pile-up events in the ROI.

Other experiments as AMoRE [27], also looking for ^{100}Mo neutrinoless double-beta decay, adopted metallic-magnetic-calorimeter (MMC) as temperature sensors [28]. The major advantage of this sensor technology is to provide signals with faster response times than that of the NTDs, reducing the pile-up background in the ROI.

The counting rate of randomly coincident $2\nu 2\beta$ decay events in a 280 g $\text{Li}_2^{100}\text{MoO}_4$ CUPID detector is estimated on the level of $3.3 \cdot 10^{-4}$ counts/keV/kg/year (ckky) at 3034 keV, assuming a time-resolving capability of 1 ms [18]: randomly-coincident $2\nu 2\beta$ decay events represent at the moment the main source of background for the next-generation, large-scale, high-radio-pure experiments based on the CUPID technologies [22, 29].

Pile-up rejections using pulse-shape analysis of the heat channel have been presented [30]: rejection performances of 90% for pile-up times down to 2 ms were reported. However, these values are not sufficient to reach the ultimate CUPID goal.

The approach followed here is the same as that reported in Ref. [18], consisting of exploiting the light signal to improve pile-up rejection through pulse-shape discrimination. In fact, as reminded above, both CROSS and CUPID will be provided with optical bolometers to detect the scintillation light in coincidence with the heat signal measured in the $\text{Li}_2^{100}\text{MoO}_4$ crystal. These light detectors consist of thin Ge wafers equipped with NTD’s as the $\text{Li}_2^{100}\text{MoO}_4$ crystal. The collected light is detected as a temperature pulse in the wafer. The primary function of the double heat-light readout is the rejection of the alpha background by exploiting the lower scintillation yield of alphas with respect to betas/gammas for the same deposited energy. Besides this, the light detector can play a crucial role also to mitigate the pile-up background, since its signal rise-time is about ten time shorter than that of the heat signal. In order for this method to be effective, the signal-to-noise ratio needs to be enhanced, which can be obtained through the so-called Neganov–Trofimov–Luke (NTL) effect [31, 32].

With respect to past work, which was mainly conceptual, our results here are supported by extensive experimental results and more sophisticated simulations, providing a convincing and operational method to reject the background related to $2\nu 2\beta$ decay events down to the desired level.

In this study we report about an experimental and simulation work which provides a technological solution combined with simulations and analysis methods to demonstrate how to reach a background index (BI) lower than $\sim 10^{-4}$ ckky in the region of interest (ROI) of ^{100}Mo $0\nu 2\beta$ decay.

It consists of three main sections:

- an experiment performed with a 245 g Li_2MoO_4 scintillating bolometer equipped with a NTL effect boosted light detector (NTL-LD) as such in [33]. The bolometer was realized in the framework of the CLYMENE project and the experiment run at the C2U (CROSS Cryogenic Underground) facility at Canfranc Underground Laboratory (Spain) as part of the CROSS/CLYMENE joint R&D program (Sect. 2);
- a new analysis method based on an optimal-filtering pulse-shape discrimination algorithm, capable to provide enhanced pile-up rejection efficiencies (Sect. 3);
- a simulation method to reconstruct synthetically produced random coincidences of $2\nu 2\beta$ decays: it is fully based on signals and noise obtained from detector measurements (Sect. 4).

2 The experiment

2.1 Setup description

Figure 1 shows a picture of the scintillating macro-bolometer mounting used in this work. The experiment was performed in a low radioactivity pulse tube dilution refrigerator (Hexadry-400, from Cryoconcept) at around 15 mK. The main bolometer consists of a 245 g Li_2MoO_4 cylindrical single crystal; it is fit in a silver-coated reflective cavity and equipped with two NTD-Ge sensors ($3 \times 3 \times 1 \text{ mm}^3$ and $10 \times 3 \times 1 \text{ mm}^3$) and one 300 k Ω Si:P heater [34]. This detector was developed within the CLYMENE project [35, 36] (ANR funded) and studied in synergy with the CROSS ERC granted project [21].

A Neganov–Trofimov–Luke-effect boosted germanium light detector, identical to the one described in [33], is coupled to the cavity and records the scintillation emitted in coincidence with the particle events occurring in the main bolometer, allowing to reject the α background. This detector is fabricated with a 170 μm thick, $\varnothing = 44 \text{ mm}$ high purity Ge wafer on top of which annular aluminum electrodes of 200 μm width and 3.8 mm pitch are evaporated. The electrodes are interconnected to produce two different electrode sets, and kept at a voltage difference V_e . The NTL-LD was operated with several V_e up to a maximum of 50 V: for this value it returned an enhanced sensitivity about 10 times larger than at $V_e = 0 \text{ V}$ and no additional contribution in the Noise Power Spectrum (NPS).

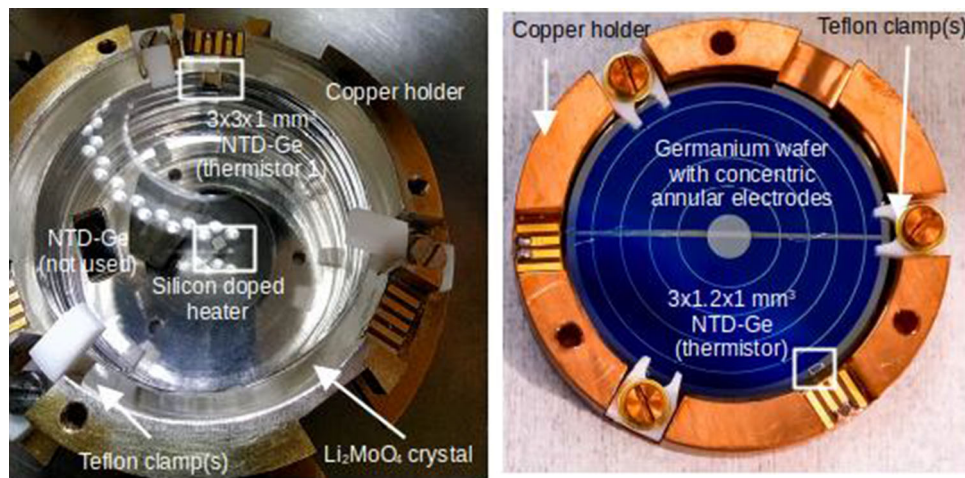


Fig. 1 (LEFT) Main heat bolometer, accommodated in an silver-coated copper case and operated at 15 mK. It is equipped with 2 different NTD-Ge thermistors and a 300 k Ω silicon doped heater; (RIGHT) a NTL-LD germanium detector, equipped with interconnected, concentric electrodes: it faces the heat bolometer and closes the cavity on

top. It has an effective signal-to-noise gain of the order of 10 when the differential of potential of the two set of interconnected electrodes is kept at 50 V. An anti-reflecting SiO coating (bluish) is deposited on the germanium wafer, between the electrodes

An optical fiber is coupled with a room temperatures 880 nm wavelength LED and used to shine the NTL-LD in the cavity. The LED was driven via Keysight 33500B wavefunction generator sending typically square voltage pulses of about 400 ns time-width and a voltage amplitude around 1 V.

2.2 Measurements

We artificially produced pile-up events in the light detector via LED photo-pulses sent through the optical fiber. The voltage amplitudes, A1 and A2, of the wave-function generator were tuned, together with the pulse duration (typically a few μ s, much shorter than the rise-time τ_r of the light detector of the order of 1 ms), to provide single pulses of energy $E = 450$ eV. Hence, a perfect synchronous two LED pulses ($\Delta t = 0$ ms) delivers 900 eV, i.e. the amount of scintillating energy recovered on a single light detector for an event at the ^{100}Mo $Q_{\beta\beta}$ (3 MeV), for a light yield of 0.3 keV/MeV as in CROSS or CUPID setup [19,37]. For simplicity, we worked with A1=A2 as the simulation presented hereafter shows that this pulse amplitude combination gives the main pile-up contributions, and sending two subsequent pulses spaced by given Δt time interval. We adopted the following Δt time pattern: 0.1; 0.3; 0.5; 0.7; 1.0; 3.0; 5.0; 0.05 ms. We delivered 100 (pile-up) signals for each Δt , at a repetition rate of 0.2 Hz. We have performed several set of measurements, by varying the NTL-LD electrode voltage bias V_e (10, 30 and 50 V). As a precaution, between each set of voltage we used the LED to charge-reset the NTL-LD, and clean the residual, spuri-

Table 1 Characterization of different NTL-LD working points with respect to several I_{NTD} thermal sensor bias current, for a mixing chamber temperature regulated at 15 mK. We finally performed all the measurements at 1 nA bias current, which is chosen to obtain a good compromise between fast response and decent signal amplitude

I_{NTD} [nA]	R_{NTD} [M Ω]	Responsivity [A.U.]	τ_r (10–90 %) [ms]
0.28	10	1	2
1	2.3	0.363	1.2
2.9	0.7	0.182	0.8

ous electric field built-up in the semiconductor due to charge trapping as described in [38].¹

We measured an average performance on the light channel of $\sigma \sim 90$ eV (~ 9 eV) baseline noise when operated at $V_e = 0$ V (50 V) and sensitivity of 1 μ V/keV (10 μ V/keV). We explored different NTL-LD detector working points by scanning with respect to different sensor bias currents (Table 1). We finally chose to work at a bias of 1 nA, which provides a signal rise-time of 1.2 ms.

The NTL-LD signals were filtered with an analog low-pass Bessel filter: the cut-off frequency was set at 500 Hz [39–41], above the intrinsic detector cut-off frequency $F_{intr} = 0.35/\tau_r$. All the measurements were 24 bit sampled at a frequency of 5 kHz and continuously recorded (streaming) during the course of the experiment. The streaming files were analyzed offline via an analysis software using Gatti–

¹ However a similar NTL light detector was operated in the same setup during one month for background acquisition without need of any charge-reset procedure.

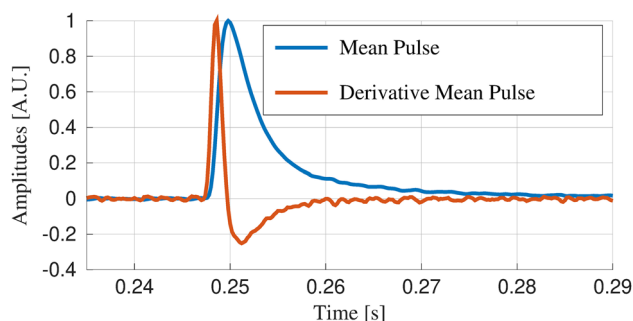


Fig. 2 Mean, normalized LED pulse $m(t)$ and its derivative $\frac{d}{dt}m(t)$. A 500 ms time-window was used for the Gatti–Manfredi optimal filter analysis

Manfredi matched optimum filter [42]: it returns the energy estimate and pile-up rejection parameters, as defined hereafter in Sect. 3.

3 Data analysis: method and results

To optimally reconstruct the energy of an event over the noise by exploiting the maximum of a signal pulse we employed the optimal filtering algorithm reported in [42]. Few elements are required: (1) the typical average baseline power spectrum of the measurements, obtained by using data streams where no pulses are present (more than 200 baseline windows); (2) a mean pulse $m(t)$, obtained by averaging 100 pulses with the lowest used Δt of 50 μs . This value being much shorter than the rise-time we can consider these events as singles (Fig. 2).

We then built a transfer function $H(f)$ accordingly and filtered each pulse in the frequency domain; the maximum A of the filtered pulse $s_f(t)$ in the time domain is then, by construction, the pulse amplitude (energy) estimator which provides the best signal-to-noise ratio (S/N).

In order to evaluate the difference in shape of each pulse (pile-up) with respect to the average pulse (single), every filtered signal is compared in the time-domain with the filtered average pulse $m_f(t)$ by fitting with $s_f(t) = A_{fit} \cdot m_f(t + \delta t)$; the χ^2 is minimized with respect to the A_{fit} and δt . The minimization returns a second pulse amplitude estimator A_{fit} .

For each signal we can determine a pulse shape parameter discriminator as $\text{PSD} = \frac{A}{A_{fit}}$: it will have value of 1 for pulses identical to that of the average pulse, lower if the shape is different as for pile-up events, and measures how much a signal differs from the reference pulse.

Particular attention was devoted to compare the pulse shape of particle-induced scintillation events with LED-generated ones; to this end we analyzed ^{232}Th -source calibration run (48 h) and selected the ^{208}Tl (2615 keV γ s) scintillation events. We observed very minor differences in the

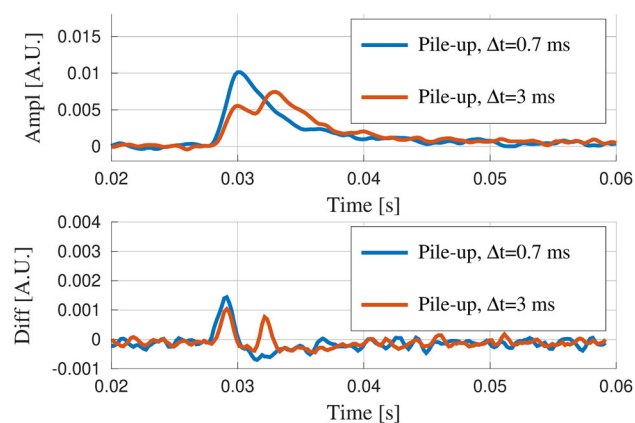


Fig. 3 Example of two 0.45 keV pile-up pulses (top) and derivatives (bottom, time-shifted to have the maximum centered at $t = 0.03$ s) recorded by the NTL-LD at $V_e = 50$ V, for a pile-up time Δt of 3 ms (red) and $\Delta t = 0.7$ ms (blue), respectively. Our pulse shape parameter algorithm utilizes the derivative of the signals and allows to reject 95% of pile-up pulses with $\Delta t = 0.7$ ms

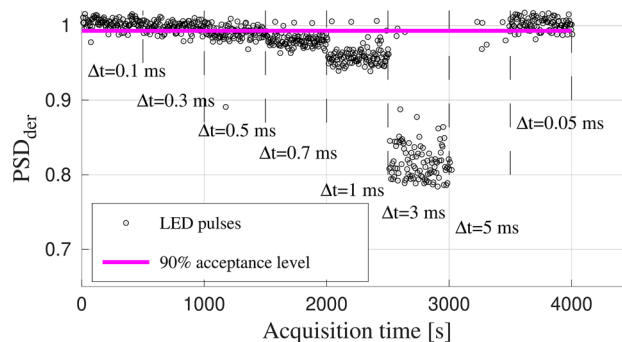


Fig. 4 Scatter-plot of the PSD_{der} as a function of the acquisition time (the detector is biased at $V_e = 50$ V). Every 500 s the Δt between the two pile-up pulses is changed, according to the pattern reported in the text. The distribution allows to trace the pile-up rejection curve with respect to Δt

shape, whose effect is negligible with respect to the scope of this work.

To better distinguish signals differing in the rise-time part it is convenient to consider the derivative of the signal instead of the signal itself. In the following we will define as PSD_{sig} the shape parameter based on the signal itself, and PSD_{der} on the derivative of the signal. Figure 2 shows the average signal and its derivative, whose maximum corresponds to the maximum slope of the signal in its rising part. With simple, geometrical consideration we can determine that a single event has a derivative maximum larger than that of a pile-up event at the same energy. Figure 3 shows an example of two pile-up signals separated by 0.7 ms and 3 ms, together with their derivatives.

From now on we will work exploiting PSD_{der} instead of PSD_{sig} . Figure 4 reports the PSD_{der} as a function of the running time for a full measurement acquired at $V_e = 50$ V

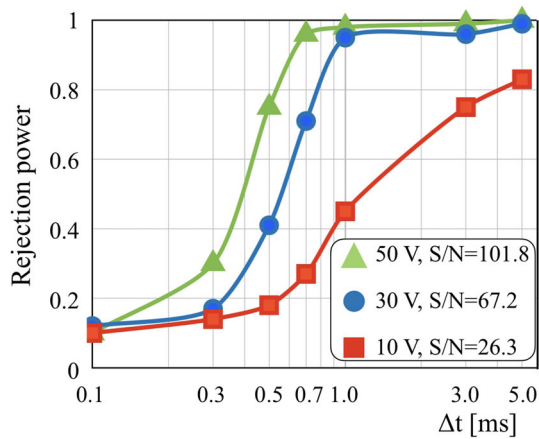


Fig. 5 Experimental rejection curves traced for several V_e (continuous lines are used to guide the eye). The S/N on the filtered signal $s_f(t)$ spans from 9.6 at $V_e = 0$ V to 101.8 at $V_e = 50$ V, corresponding to an effective NTL gain of about 10

and LED pulses injected according to the Δt time pattern as defined in Sect. 2.2. A PSD_{cut} value, shown as a pink horizontal line in Fig. 4, is determined and adjusted such as to keep 90% of single-pulse events ($\Delta t = 0.05$ ms). For each group of pile-up pulses (100 consecutive) the number of events N_{rej} with $PSD_{der} < PSD_{cut}$ is counted and compared to the total number N_{inj} of events injected. The rejection factor is defined as $r_{\Delta t} = N_{rej}/N_{inj}$ and the pile-up rejection power curves are traced for each set of measurements. Figure 5 shows all the experimental results together²; for completeness, for each set the S/N ratio is also given, which shows that the rejection capabilities increases with increasing S/N ratio, as also reported in [18,25], and expected from signal processing in general.

4 Simulations

4.1 Synthetic data generation, analysis and results

In order to reproduce, control and understand our pile-up experimental data, we adopted a method which permits to generate synthetic data, indistinguishable from the real, measured data [43]. The method is hereafter described.

Starting from a record of data (streaming) we proceed by:

- (1) constructing an average signal $m(t)$ in the exact same condition as previously performed using the experimental data (see above);

² For $V_e = 0$ V the pulses are almost buried in the signal noise; the corresponding rejection power being far away from the goal.

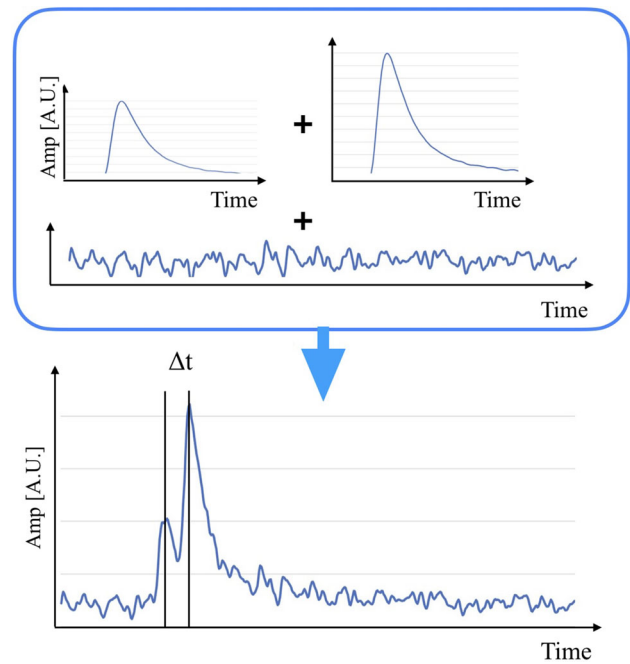


Fig. 6 Two average signals of different amplitudes are summed together with a time difference of Δt and with a noise sample to give the synthetic data shown in the bottom of the figure

- (2) summing the average signal re-scaled to an amplitude A_1 with an another average signal of re-scaled amplitude A_2 , but time-shifted of Δt ;
- (3) inserting the previously constructed pile-up pulses to the experimental data streaming (the full measurement was taken into account and we made sure that in the selected region no pulses were present).

The full procedure is sketched in Fig. 6.

We built the synthetic data streaming conforming with our experimental measurements, namely equal amplitudes of the two signals, identical Δt pattern and the same number of pile-up events and repetition rate. The synthetic data are then elaborated using the same analysis pipeline of the experimental data. The pile-up rejection values $r_{\Delta t}$ are hence extracted as described in the previous section.

To benchmark the quality of the synthetic data we compared in Fig. 7 the synthetic pile-up rejection performances with the experimental one. An excellent agreement is observed in the whole range, within the uncertainties,³ between the measurement and the synthetic data.

³ Bayesian statistics calculation was used to infer the error bars on the experimental data and are within the symbols. The variance for a having k out of n occurrences reads: $V = \frac{(k+1)(k+2)}{(n+2)(n+3)} - \frac{(k+1)^2}{(n+2)^2}$. We finally have 68% within $k \pm \sigma$ where $\sigma = \sqrt{V}$. For a rejection of 0.1 ($\frac{k}{n} = 0.1$) and a number of occurrences of 100, $\sigma=0.03$. They are equal as for the synthetic simulation as the number of occurrences is the same, namely 100 events for each Δt [44].

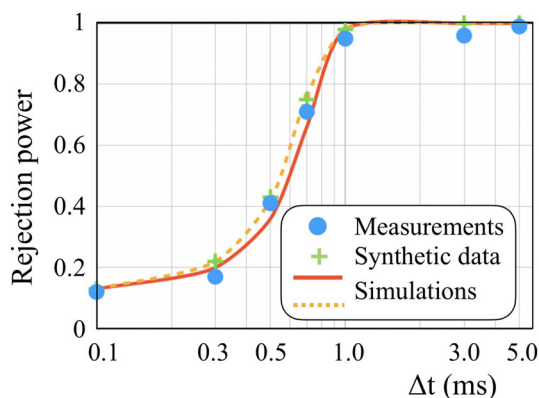


Fig. 7 Rejection power curves versus Δt for an electrode bias $V_e = 30$ V. Blue dots are from the measurements (see Fig. 5), green crosses are from the synthetic data, red plain curve is from the full simulation, i.e. $A1 \& A2 \in 2\nu 2\beta$ -spectrum, and orange dashed curve is from the approximate simulation with $A1 = A2$. Error bars are within the symbols

In the next section we will show how we performed wider synthetic data simulations by modifying the pile-up time step, number of occurrences, and $A1/A2$ ratio to best comply with a real double-beta decay experiment.

4.2 Refined synthetic pile-up simulation

First of all we refined our synthetic data by producing pile-up events with a Δt running from 0 to 3 ms with a time step of 0.1 ms, and injecting 1800 events for each, assuming equal amplitudes for the two signals ($A1 = A2$). This produces the orange curve shown in Fig. 7.

However, a realistic synthetic simulation (called hereafter full simulation) must take into account that the amplitudes of the two signals, $A1$ and $A2$, should comply with the $2\nu 2\beta$ energy distribution [45]. Therefore, pile-up events are constructed by picking up twice randomly inside this energy distribution and summing them up with a Δt ranging from 0 to 3 ms. We finally select those events having an energy in the ROI, i.e. $3034 \text{ keV} \pm 50 \text{ keV}$ (Fig. 8). The full simulation pile-up rejection curve is shown in Fig. 7 as red solid line. It should be noticed that we expect a lower pile-up rejection efficiency than for the case where pulses have identical amplitudes (orange curve). This is due to the fact that for $A1 \ll A2$ ($A1 \gg A2$) pile-up events may be barely distinguishable from single-pulses and may not be rejected. This is precisely what is observed in Fig. 7 as the red plain curve ($A1 \neq A2$) is below the orange dashed one ($A1 = A2$). The full simulation and the approximate simulation returning almost the same rejection power curves motivates the simplified approach employed in the experimental work.

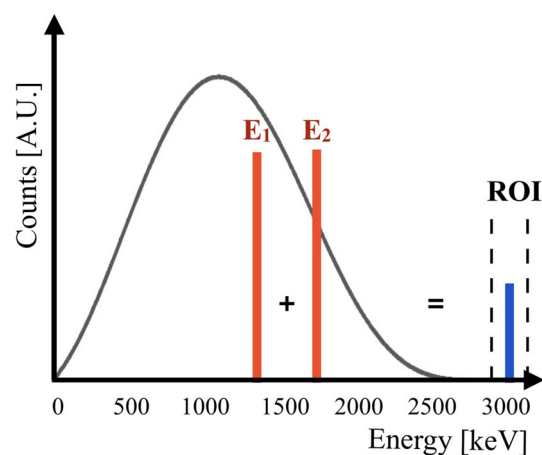


Fig. 8 Energy spectrum of ^{100}Mo $2\nu 2\beta$ decay. The two red bars correspond to the energies of randomly picked up values which sum up to an energy in the ROI of ^{100}Mo $0\nu 2\beta$ decay

4.3 Background index extraction

To extract the background index resulting from pile-up events from these simulations we need to compute the probability, $\epsilon_{Q\beta\beta}(\Delta t)$, to obtain an event at 3034 keV resulting from a pile-up of two events coming from the $2\nu 2\beta$ decay for different values of Δt between the two single events.

These probabilities are shown in Fig. 9 where the distributions of the amplitude of the pile-up events are presented for $\Delta t = 0$ and 1 ms. The rightmost distribution corresponds to $\Delta t = 0$ ms and does not depend on the signal shape since it is identical to the initial average signal. Hence the amplitude of the signal does not vary after the optimal filtering whereas for $\Delta t \neq 0$ it does. The presented distributions were obtained for an analytical signal of 1.2 ms rise-time, the description of which is presented hereafter. The leftmost curve (blue) corresponds to the amplitude of the pile-up events for $\Delta t = 1$ ms and the middle (red) one corresponds to its distribution, slightly distorted by the optimal filtering procedure.

We then calculated the background indexes associated to pile-ups of ^{100}Mo $2\nu 2\beta$ events for every simulated configuration (Table 2) as follows:

$$BI = \epsilon_{Q\beta\beta} \times (1 - r_{\Delta t}) \times \tau \times \left(\frac{\ln 2 \cdot N_{100\text{Mo}}}{T_{1/2}^{2\nu 2\beta}} \right)^2 \quad [\text{ckky}] \quad (1)$$

where τ is the time step (here 0.1 ms as in the simulations), $N_{100\text{Mo}}$ the number of ^{100}Mo nuclei and $T_{1/2}^{2\nu 2\beta}$ is the half-life of the ^{100}Mo $2\nu 2\beta$ decay.

In the next section we study how the signal rise-time changes the pile-up rejection efficiency.

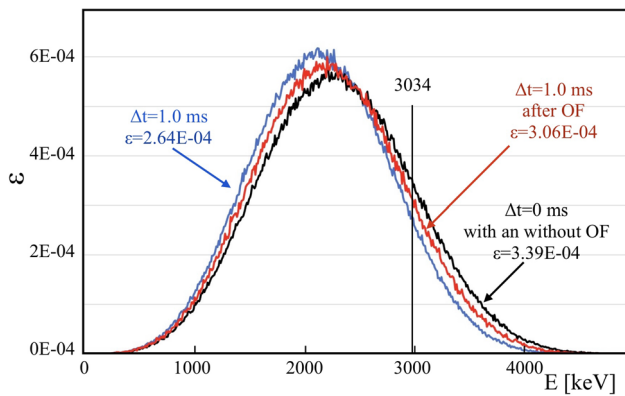


Fig. 9 Distributions of the sum of two $2\nu 2\beta$ decays separated by Δt equal 0 and 1 ms after the optimal filtering procedure. The probability ϵ is given at 3034 keV

4.4 Signal rise-time and pile-up rejection efficiency

It is of major interest to investigate and predict how the light detector rise-time τ_r will affect the pile-up rejection capability, combined with the S/N ratio. To this end, we generated an analytical average pulse, which is profiled by adding a Gaussian function, to account for the rising part of the signal, with a sum of exponential functions, to account for the decay part of the signal.

Figure 10 shows three analytic average pulses with different rise-time values; even though the blue curve ($\tau_r = 1.2$ ms) does reproduce fairly well the experimental average pulse $m(t)$ (dashed gray line) extracted from the measurements, all the simulations with these rise-time were performed with the experimental average pulse.

Analytical pulses enable to make faster/slower average pulses in a simple manner, to produce different synthetic simulation data and extract, accordingly, the power rejection curves $r_{\Delta t} = f(S/N, \tau_r)$. The variation of the pile-up rejection power curves with respect to the pulse decay time is less important and therefore is not taken into account in this study.

We have performed full simulations with the pulses of Fig. 10, varying for each the S/N ratio accordingly; results

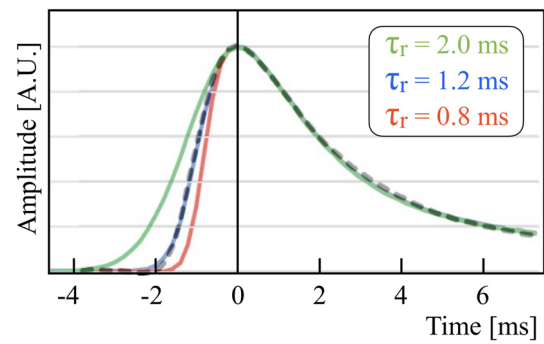


Fig. 10 Average signals coming from the fit as described in the text for rise times equal to 0.8, 1.2 and 2.0 ms. The gray dashed line corresponds to the average signal for 1.2 ms rise time

are displayed in Fig. 11. It should be noticed that the S/N achieved correspond to the 1.2 ms rise-time signal (as in the experiment) and for NTL-LD electrode biases $V_e = 10, 30, 50$ V, the three left round blue dots of Fig. 11. The S/N corresponding to 70 and 90 V were extrapolated.

The method here presented is a powerful tool to predict the pile-up rejection power and hence the pile-up background index achievable in the ROI, by simply combining few, generic detector specification as S/N ratio and rise-time.

4.5 Approximate evaluation of the background index

As we performed the full simulations for every bias, we were able to determine the Δt value corresponding to 50% pile-up rejection ($\Delta t_{50\%}$). This latter was calculated using a linear interpolation between the two consecutive Δt leading to rejection below and above 50%. Corresponding values are reported in Table 2 as well as the background index. The background index associated to pile-ups of ^{100}Mo $2\nu 2\beta$ events in a 280 g bolometer, 95% ^{100}Mo -enriched and using the PSD_{der} parameter can be approximated as:

$$BI \approx \Delta t_{50\%} \times 2.75 \cdot 10^{-4} \text{ [ckky]}, \tag{2}$$

where $\Delta t_{50\%}$ is expressed in ms.

Table 2 Background index values for different S/N ratio values and signal rise-time as shown in Fig. 11. $\Delta t_{50\%}$ are the Δt corresponding to 50% of pile-up rejection for signals of $\tau_r = 1.2$ ms

Bias [V]	S/N	BI [in 10^{-4} ckky]			$\Delta t_{50\%}$ [ms] For $\tau_r = 1.2$ ms
		For $\tau_r = 2$ ms	For $\tau_r = 1.2$ ms	For $\tau_r = 0.8$ ms	
10	26	3.9	2.7	1.9	0.91
30	67	2.5	1.6	0.88	0.58
50	103	1.9	1.3	0.63	0.47
70	141	1.6	1.1	0.48	0.40
90	181	1.5	1.0	0.45	0.37

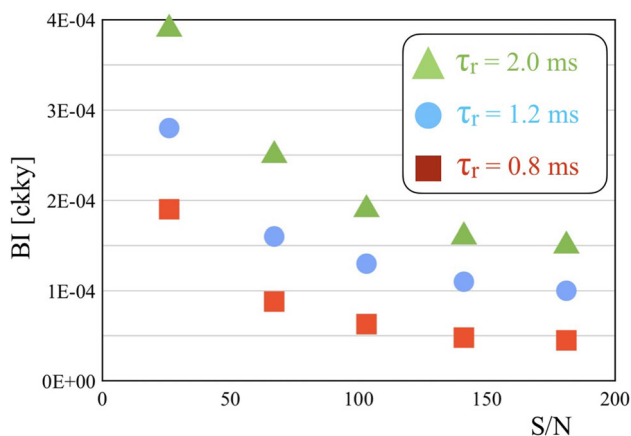


Fig. 11 Background index associated to ^{100}Mo $2\nu 2\beta$ decay events, after a PSD_{der} selection, for three values of the signal rise-time and several S/N ratios (Table 2). The simulations of the blue circles corresponding to $\tau_r = 1.2$ ms were done with the average experimental signal whereas the two others, $\tau_r = 2$ ms and $\tau_r = 0.8$ ms, used the analytical signals described in Fig. 10

Because of the high slope of the rejection power curve around $\Delta t_{50\%}$, the above equation gives a better feeling of the BI that can be achieved than by simply extrapolating from the Δt value where 90% rejection is obtained as often expressed [30]. With this rule of thumb hereby expressed, in order to obtain $5 \cdot 10^{-5}$ ckky [22] we should reach 50% rejection for signal separated by $\Delta t = 0.18$ ms.

5 Conclusions

Some future bolometric experiments, like CROSS and CUPID, rely on a detector technology based on NTD-equipped scintillating bolometers to search for the $0\nu 2\beta$ of ^{100}Mo . Due to the poor time resolution of the main heat bolometer, randomly-coincident (pile-up) ^{100}Mo $2\nu 2\beta$ decay events will eventually represent the main source of background in the next-generation, large-scale, $0\nu 2\beta$ decay searches based on this technology. To circumvent this problem we have operated a Li_2MoO_4 scintillating bolometer in combination with a Neganov–Trofimov–Luke light detector. Thanks to the fast time response and the enhanced S/N ratio performances of this latter, we investigated the rejection of pile-ups from single-pulse events utilizing the mere scintillation signal. We studied the pile-up rejection performance of the setup in a validation run hosted in the CROSS cryogenic underground facility. We demonstrated for first time with an experimental pile-up measurement coupled with a simulation, that it is possible to reject randomly-coincident events in massive $\text{Li}_2^{100}\text{MoO}_4$ cryogenic scintillating bolometers, as those of CROSS and CUPID experiments, down to background indexes of $\sim 10^{-4}$ ckky (at the $Q_{\beta\beta}$ of ^{100}Mo), via the scintillation signal.

Together with the experimental work, we presented (i) an approximate and full simulation method to reconstruct, synthetically, randomly coincident events from the $2\nu 2\beta$ decay mode, (ii) a new pulse-shape discrimination algorithm based on a derivative, optimal-filtering signal processing technique capable to provide superior pile-up rejection efficiencies. The experimental and simulation pile-up rejection results have been compared: we observed an excellent agreement between them. As we have shown that there is a strong dependence with the signal rise-time, it is strongly recommended that we use the real signal such as the one coming from calibrations to extract the average signal to be used in the simulation to predict the achievable background index.

With respect to CUPID, the CROSS detectors foresee to have the additional capability to reject surface events [46]. The reduction of the random-coincidence background enables to fully exploit the CROSS surface sensitive technology. In fact, the background induced by beta particles emitted by the radioactive contamination of the passive materials facing the detectors is a sub-dominant contribution of the background in the ROI that will emerge only after the mitigation of the random-coincidence component.

New investigations are ongoing to further enhance the light detector S/N ratio via higher NTL electrode bias, shorten the light detector rise-time and hopefully reach background indexes in the ROI of $5 \cdot 10^{-5}$ ckky, which would fully comply with the CUPID experiment goal.

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