# Journal Pre-proof

Heat capacity and magnetocaloric effect in the zircon and scheelite phases of  $RCrO_4$ , R = Tb, Er, Ho

E. Palacios, M. Castro, J. Romero de Paz, J.M. Gallardo-Amores, R. Sáez-Puche

PII: S0022-4596(22)00481-9

DOI: https://doi.org/10.1016/j.jssc.2022.123356

Reference: YJSSC 123356

To appear in: Journal of Solid State Chemistry

Received Date: 30 March 2022

Revised Date: 14 June 2022

Accepted Date: 19 June 2022

Please cite this article as: E. Palacios, M. Castro, J. Romero de Paz, J.M. Gallardo-Amores, R. Sáez-Puche, Heat capacity and magnetocaloric effect in the zircon and scheelite phases of *R*CrO<sub>4</sub>, *R* = Tb, Er, Ho, *Journal of Solid State Chemistry* (2022), doi: https://doi.org/10.1016/j.jssc.2022.123356.

This is a PDF file of an article that has undergone enhancements after acceptance, such as the addition of a cover page and metadata, and formatting for readability, but it is not yet the definitive version of record. This version will undergo additional copyediting, typesetting and review before it is published in its final form, but we are providing this version to give early visibility of the article. Please note that, during the production process, errors may be discovered which could affect the content, and all legal disclaimers that apply to the journal pertain.

© 2022 Published by Elsevier Inc.



# **Credit Author Statement**

**Elias Palacios.** Conceptualization. Methodology. Investigation. Magnetocaloric effect. Writing - Original Draft. **Miguel Castro.** Investigation. Heat Capacity. Writing - Review & Editing. **Julio Romero de Paz.** Investigation. Preparation of zircons. Writing - Review & Editing. **José Manuel Gallardo-Amores**. Investigation. High pressure. Preparation of scheelites. Writing - Review & Editing. **Regino Sáez-Puche.** Conceptualization. Methodology. Investigation. Magnetiztion mesurements. Writing - Review & Editing.

Journal Prevention



# Heat capacity and magnetocaloric effect in the zircon and scheelite phases of $RCrO_4$ , R = Tb, Er, Ho

E. Palacios<sup>a,b,</sup>, M. Castro<sup>b,c</sup>, J. Romero de Paz<sup>d</sup>, J. M. Gallardo-Amores<sup>d</sup>, R. Sáez-Puche<sup>d</sup>

<sup>a</sup>Departamento de Física de la Materia Condensada, Universidad de Zaragoza, 50009 Zaragoza, Spain

<sup>b</sup>Instituto de Nanociencia y Materiales de Aragón (INMA), CSIC–Universidad de Zaragoza, 50009 Zaragoza, Spain

<sup>c</sup>Departamento de Ciencia y Tecnología de Materiales y Fluidos, Universidad de Zaragoza, 50018 Zaragoza, Spain

<sup>d</sup>Departamento de Química Inorgánica, Universidad Complutense de Madrid, 28040 Madrid, Spain

### Abstract

We present here new magnetization and heat capacity data under magnetic field and direct measurements of the magnetocaloric effect (MCE) in the zircon and the new scheelite phases of  $R \text{CrO}_4$  (R = Tb, Er, Ho) from 5 K to 100 K, for magnetic fields B from 0 to 9 T. Zircons have a high MCE near their Curie point,  $T_C \simeq 20$  K, reaching maximum isothermal entropy increments,  $|\Delta S_T| = 21$ , 19.4, and 16.2 J kg<sup>-1</sup>K<sup>-1</sup> for HoCrO<sub>4</sub>, ErCrO<sub>4</sub>, and TbCrO<sub>4</sub>, respectively, for an external field of 5 T. TbCrO<sub>4</sub> has another anomaly near  $T_D = 60$  K associated to a Jahn-Teller transition from the tetragonal zircon structure to an orthorhombic phase. Scheelites are antiferromagnetic with  $T_N \simeq 25$  K. In the Tb scheelite the rare earth is strongly coupled to Cr<sup>5+</sup> and the MCE exhibits the typical features of an antiferromagnet, *i.e.* a sort of Curie-Weiss behavior above  $T_N$  and a sudden drop to small or even inverse values below. In the Er and Ho scheelites the  $R^{3+}$ -Cr<sup>5+</sup> exchange coupling is very weak and the  $R^{3+}$  ion behaves independently of the Cr<sup>5+</sup>. As a striking consequence the MCE is quite stronger well below  $T_N$ .

*Keywords:* Polymorphism of  $RCrO_4$  oxides, Magnetic meaurements, Heat capacity and entropy, Magnetocaloric effect

Email address: elias@unizar.es (E. Palacios)

### 1. Introduction

Refrigeration by demagnetization of a material with strong magnetocaloric effect (MCE) is a procedure used since the 1930's to reach temperatures below 1 K [1]. The method was intended for reaching the lowest possible temperatures, with scientific purposes. Therefore, in that time paramagnetic salts were used. These are composed by ions of high magnetic moment separated by many non magnetic ones preventing ordering by magnetic dipolar interaction, which allowed to cool down to 40 mK by routine, in a single shot. Today there are other procedures of refrigeration, but it turns out that the old demagnetization method is thermodynamically very efficient. Moreover, 10 refrigeration at temperatures of the boiling points of helium, hydrogen or natural gas overtakes the pure scientific research by a large amount, when liquid helium is currently used in many scenarios, hydrogen is proposed as a clean energy vector, and natural gas is a fuel reducing considerably the emission of  $CO_2$  to the atmosphere, with respect to other usual hydrocarbons. 15 A review of materials and systems for magnetic refrigeration at cryogenic temperatures is [2], where the full section of the volume is devoted to the subject. A more recent review is [3].

- The ideal material to use the MCE for refrigeration above 1 K would be composed of atoms with high spin, high density of magnetic moments, low anisotropy, and weak exchange interactions. This is the case of the previously studied zircon phase of GdCrO<sub>4</sub> [4, 5, 6] where the partial polarization of the Gd<sup>3+</sup> ions confers to this compound a high MCE over a wide temperature range, with  $|\Delta S_T| > 20$  J kg<sup>-1</sup>K<sup>-1</sup> between 5 K and 35 K and a maximum of 29 J kg<sup>-1</sup>K<sup>-1</sup> at 22 K, in both cases for a field increment from zero to
- 9 T. The gadolinium compound is the most evident case among the zircons  $R \text{CrO}_4$  (R = rare-earth atom) because of the virtually isotropic behavior of  $\mathrm{Gd}^{3+}$ , in the temperature range of this work, but other rare earths can be explored. In this sense, it has been reported that other zircons  $R \text{CrO}_4$  (R
- <sup>30</sup> = Ho and Dy) show also large values of the magnetocaloric parameters that make of these oxides potential refrigerant materials [7]. Moreover, recently the scheelite polymorphs (space group, s. g. I4<sub>1</sub>/a) have been synthesized at high pressure from the zircon phases for most R elements. These scheelite forms are quenchable after releasing the pressure [6, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17].



Figure 1: Left side: Perspective view of the zircon and scheelite-type structures showing the edge sharing chains of  $RO_8$  bisdisphenoids. Blue:  $Cr^{5+}$ , red:  $O^{2-}$ , orange:  $R^{3+}$ . Right side: Two possible *R*-Cr exchange pathways 1 and 2 in both structures, showing the very different *R*-O-Cr angles that determine the sign of the interaction.

Most of the zircon-type  $RCrO_4$  oxides behave as ferromagnetic (FM), while the scheelite polymorphs are made of ferromagnetic layers, perpendicular to the c-axis, coupled antiferromagnetically (AFM). The change in the sign of the magnetic interaction can be explained by considering the changes in the bond angles of Cr-O-R pathways through which the superexchange interactions take place in these two structural types, see Fig. 1. In the case of the zircon polymorphs the pathway 1 (Fig. 1) with a bond angle near of  $90^{\circ}$  (94.8(2)° for TbCrO<sub>4</sub> is a typical example) accounts for the observed FM interaction, while for the scheelite polymorphs the corner sharing between the  $[RO_8]$  and  $[CrO_4]$  polyhedra significantly increases that Cr-O-R angle 45 (to  $132.3(3)^{\circ}$  for TbCrO<sub>4</sub>) and with it the type of interaction changes from FM to AFM. In addition to the fundamental physical and chemical properties, the following features make these  $RCrO_4$  oxides suitable for potential refrigerant in comparison with other rare earth transition metal oxides. First, a large magnetic moment, typical of many rare earth ions, makes easier the polarization by a moderate external magnetic field. Second, for some rare earths the crystal field (CF) favor the thermal population of many magnetic states (*i.e.* random distribution of the magnetic moment directions above  $T_N$  or  $T_C$  but still at low temperatures) at zero field. Third, the exchange interaction with the 3*d*-ion, usually much higher than R-R exchange interac-55 tion, provides an internal field increasing the polarization below the ordering temperature.

The Cr<sup>5+</sup> ion plays an important role as promoter of the interactions in the rare earth sublattice increasing the ordering temperatures by one order of magnitude in comparison with the analogous  $RXO_4$  (X = P, As, V) where X is a diamagnetic element [18, 19]. The order temperatures in these compounds are well below 5 K, indicating that the direct R - R interaction is much weaker than R-Cr or Cr-Cr. On the other hand, the lower  $T_C$  in the Crzircons where R is not magnetic (e.g. YCrO<sub>4</sub> [9] or LuCrO<sub>4</sub> [8]) indicates that

- the *R*-Cr interaction is relevant and enhances the FM coupling. Additionally, a ferroelectric transition near 100 K has been reported in  $R \text{CrO}_4$  (R = Y, Gd, Ho, Sm), related to a distortion of the  $\text{CrO}_4^{3-}$  tetrahedra [20]. This fact opens the possibility of changing the exchange interactions, thus a magnetoelectric effect.
- The structural and magnetic properties of the zircon and scheelite polymorphs of  $RCrO_4$  (R = Tb, Er, Ho) have been discussed in a previous series of papers [8, 9, 11, 12, 13, 14, 15, 16, 21, 22]. The heat capacity was studied at zero magnetic field and for the scheelite TbCrO<sub>4</sub> also at 3 T and 8 T [14].

This work is essentially focused on the MCE of both polymorphs of  $R \text{CrO}_4$ (R = Er, Ho, Tb) oxides, by studying the isothermal entropy change,  $\Delta S_T$ , associated to the applied magnetic field change  $\Delta B = B - 0$  (see section 2.3.1). Thus,  $\Delta S_T$  is obtained from isothermal magnetization, from heat capacity data at several magnetic fields and by direct measurements of the heat released/absorbed on isothermal magnetization/demagnetization. The heat capacity data are analysed in relation with the CF splitting of the ground level of each rare earth ion. A possible Dzialozhinsky-Moriya interaction in scheelites has a too small influence in the MCE. Although it is never explicitly stated we will assume a simple Heisenberg interaction hamiltonian, as the ansisotropy comes mainly from the CF at the rare earth ion site.

### **2.** Experimental details

### 2.1. Sample preparation

Zircon-type RCrO<sub>4</sub> powder samples were prepared by heating the stoichiometric amounts of Cr(NO<sub>3</sub>)<sub>3</sub> · 9 H<sub>2</sub>O and R(NO<sub>3</sub>)<sub>3</sub> · 6 H<sub>2</sub>O in an oxygen flow according to the following thermal process: 30 min at 433 K, 30 min at 473 K and 10-12 h at 853 K. Scheelite-type RCrO<sub>4</sub> powder samples were obtained in a belt type press from the corresponding zircon-type RCrO<sub>4</sub> under a high pressure of 40 kbar and 833 K for 30-40 min [12, 14, 23]. For both polymorphs, the X-ray powder diffraction patterns obtained confirmed the respective structures and purity.

### 95 2.2. Magnetization measurements

New isothermal DC magnetization M data were collected using a Quantum Design Physical Property Measurement System (PPMS), from 2 K to 60 K and for applied magnetic fields B up to 9 T. These measurements were used to deduce the MCE. Only the M-data for the scheelite TbCrO<sub>4</sub> are shown (Fig. 7), since most of results have been discussed in previous works. We give

the *M*-data in a double scale, since in  $\mu_B/fu$  they are more directly related to the atomic properties than in emu/g. The DC magnetic susceptibility,  $\chi$ , has been deduced as  $\chi = M/B$  for low field data. The AC susceptibility has been taken from previous works.

### 105 2.3. Heat capacity and entropy

For the determination of the heat capacity,  $C_{p,B}$ , the usual relaxation procedure is used in a PPMS at constant magnetic fields from 0 to 9 T and

very low pressure, using a pellet of pressed powder. The accuracy is better than 5% between 2 K and 50 K. To determine the phonon contribution of the zircon phases the heat capacity of  $LuCrO_4$  [10] has been used, where  $Lu^{3+}$  is not magnetic and  $Cr^{5+}$  orders at the low  $T_N = 9.2$  K, allowing to extrapolate the experimental higher temperature data to  $T \rightarrow 0$  by a Debye function. For other zircons an empirical corresponding states law was used as an estimation of the phonon contribution, *i.e.*  $C_{ph} \simeq C_{ph} (\text{LuCrO}_4, T/fs)$ using a proper scale factor  $fs \simeq 1$ . This estimation reproduces well the heat 115 capacity of other zircons like  $YCrO_4$  [10] and  $GdVO_4$  [24] at temperatures where the magnetic contribution is negligible. These compounds have no contribution of the crystal- field either. For scheelites a corresponding states law has been applied to the very precise, reliable and recent experimental data of  $LaNbO_4$ , by adiabatic calorimetry [25]. This law reproduces acceptably 120 the experimental heat capacity of  $YVO_4$ , despite of the very different atomic

masses in both compounds.

To estimate the contribution of the thermal population of the CF levels in zircons, the isostructural  $RVO_4$  compounds [18] have been used, when the CF is essentially produced by the charge of  $O^{2-}$  in all cases. For the ErCrO<sub>4</sub> sheelite, the levels of Er-doped scheelites  $AMoO_4$  (A = Ca, Sr, Pb) [26] have been assumed. Lacking any direct determination of the CF splitting in other scheelite-oxides, the data of the  $RLiF_4$  [27, 28, 29, 30, 31, 32] have been taken. Because of the higher  $O^{2-}$  charge vs.  $F^-$ , the CF splitting of the ground free ion manifold in the fluorides must be quite smaller than in the orthochromates, but we assume that at least the splitting scheme is the same in both compounds for every R.

The entropies have been determined by the thermodynamic relation

$$S(T,B) = S(T_0,B) + \int_{T_0}^T \frac{C_{p,B}dT}{T}$$
(1)

Here  $T_0 = 0$  is taken when a clear extrapolation of the experimental data to  $T \to 0$  is possible (e.g. for a high applied field), assuming S(0, B) = 0. Otherwise another different temperature  $T_0 \gg 0$  is taken using the experimental difference  $S(T_0, B_2) - S(T_0, B_1)$ , obtained from magnetocaloric measurements, for setting  $S(T_0, B_2)$ , knowing  $S(T_0, B_1)$ . The molar heat capacity and entropy are given always in units of the gas constant R, that should be not confused with the symbol for a rare earth. In these units they are directly related to atomic properties (e. g. the entropy is an experimental measurement of the logaritm of the number of thermally accessible states, per chemical unit).  $\Delta S_T$  (MCE) is given in double scale, per unit of mass, and molar.

#### 2.3.1. Magnetocaloric effect

- The magnetocaloric effect is characterized by the isothermal entropy change,  $\Delta S_T$ , or the adiabatic temperature change,  $\Delta T_{ad}$ , for a magnetic field variation  $\Delta B = B - 0$ .  $\Delta S_T$  has been obtained at least in two of the three following ways:
  - 1) Directly, by the procedure described in [33].
- <sup>150</sup> 2) From isothermal magnetization data, M, via the well-known Maxwell relation

$$\left(\frac{\partial S}{\partial B}\right)_T = \left(\frac{\partial M}{\partial T}\right)_B \Rightarrow$$
$$\Delta S_T \equiv S(T, B) - S(T, 0) = \int_0^B \left(\frac{\partial M}{\partial T}\right)_B dB \tag{2}$$

3) From heat capacity data at several constant fields, via the deduced entropies,  $\Delta S_T = S(T, B) - S(T, 0)$ .

Usually these three methods are complementary. The values deduced from M are not always precise or even correct. The entropies deduced from  $C_{p,B}$  frequently involve a not well determined constant and the direct determinations are only possible in a narrower temperature range. The initial field is always assumed zero throughout this work, and we write always Bfor  $\Delta B$  to simplify the notation. It should be noted that the results form M should be slightly higher than form  $C_{p,B}$  or directly measured, due to the different demagnetization factor of the samples used for each experiment, when  $B = \mu_0 H$  is always the external field.

### 3. Results and discussion

### 3.1. Heat capacity of zircons

<sup>165</sup> 3.1.1. TbCrO<sub>4</sub>

The heat capacity of the zircon TbCrO<sub>4</sub> (Fig. 2) at zero field shows a  $\lambda$ -peak at  $T_C = 22.2(1)$  K in agreement with other determinations [34, 9]. This anomaly rounds off and its maximum moves to higher temperature on application of a weak external magnetic field indicating a FM ordering, like



Figure 2: Heat capacity of the zircon phase of  $\text{TbCrO}_4$ . Continuous line: Estimation of the phonon contribution as explained in the experimental section. Vertical lines indicate the temperatures at which the entropy is given.

- <sup>170</sup> most of zircons. There is another round anomaly starting near  $T_D = 60$  K and downwards. We ascribe this anomaly to a co-operative Jahn-Teller (JT) distortion (very usual also in other rare earth zircons like  $RXO_4$  with R =Tb, Dy, Tm and X =V, As or P) from the room temperature (RT) tetragonal zircon structure to an orthorhombic phase which has been described with
- the s. g. F222 [34] and more recently with Fddd [8]. Differently of other Tb zircons (e.g. TbVO<sub>4</sub> [35]) this transition does not have the typical  $\lambda$ shape of the second-order transitions. In our opinion that is due to the stress distribution in the pellet used for  $C_{p,B}$  measurements, since the JT transition is very sensitive to stress [36]. In contrast, the anomaly is insensitive to a measurement field larger than 5. To At zero field, the measurements
- <sup>180</sup> magnetic field lower than 5 T. At zero field, the magnetic anomaly in  $C_p$ occurs well below  $T_D$ . The much higher  $T_D$  with respect to that for TbVO<sub>4</sub> would be related to a stronger electron-phonon coupling in the Cr compound producing a wider splitting of the ground quasi-quartet of Tb<sup>3+</sup> as explained in [36].
- The entropy of both anomalies together (*i.e.* the experimental entropy at zero field minus the estimated normal phonon contribution), at 65 K is  $S_{anom}/R = 2.13$ . To understand this value, let us consider the well known isostructural TbVO<sub>4</sub>. It has a JT distortion at  $T_D = 33.1$  K [35, 18]. In the tetragonal phase of TbVO<sub>4</sub> the lowest crystal-field levels of Tb<sup>3+</sup> are one singlet (ground state), one doublet at 8.6 cm<sup>-1</sup> = 12.4 K (the factor
- one singlet (ground state), one doublet at 8.6 cm<sup>-1</sup> = 12.4 K (the factor  $E(K)/E(cm^{-1}) = 1.439 \text{ K/cm}^{-1}$  will be implicitly invoked throughout this

paper), and one singlet at 22.9 cm<sup>-1</sup>. Next level is at 91.5 cm<sup>-1</sup>, clearly too high in energy to be thermally populated at  $T_D$ . The total theoretical anomalous entropy, considering a contribution of  $Cr^{5+}$  as  $\ln(2)$ , would be  $S_{anom}/R = \ln(2) + \ln(4) = \ln(8) = 2.08$ , very close to the observed value. However in TbCrO<sub>4</sub> the anomaly in  $C_p$  at zero field occurs below 60 K. Therefore the thermal occupation of the next excited levels at 60 K would explain the observed excess of anomalous entropy above  $\ln(8)$ . Now let us consider the entropy at 25.5 K, just above the  $\lambda$ -peak. Subtracting the phonon contribution it gives  $S_{anom}/R = 1.28$ , slightly below  $2\ln(2) = 1.39$ , which can be interpreted as the magnetic contribution of  $Cr^{5+}$  plus a full thermal population of the ground CF doublet of Tb<sup>3+</sup> in the orthorhombic phase.

Within this interpretation, it is to be remarked that M does not reach saturation even at 2 K for 9 T, when  $M = 135 \text{ emu/g} = 6.64 \ \mu_B/fu$ , while the moments determined by neutron diffraction [9] are  $\mu(\text{Tb}^{3+}) = 7.62(8) \ \mu_B$ ,  $\mu(\text{Cr}^{5+}) = 0.96(3) \ \mu_B$ , giving a saturation magnetization  $M_s = 8.6(1) \ \mu_B/fu$ , much higher than observed. The explanation is the strong anisotropy of Tb and the random orientation of the crystallites in a powder sample, when only the parallel component of the field to the easy direction produces a relevant polarization effect.

3.1.2. HoCrO<sub>4</sub>

The lowest lying CF levels of Ho<sup>3+</sup> in HoVO<sub>4</sub> are a non magnetic singlet  $(E_0 \equiv 0)$ , with  $\langle J_z \rangle = 0$ , a doublet at  $E_1 = 19.5 \text{ cm}^{-1}$ , with  $J_z \simeq \pm 1$ , a <sup>215</sup> singlet at  $E_2 = 43.2 \text{ cm}^{-1}$ , with  $\langle J_z \rangle = 0$  and a doublet at  $E_3 = 44.4 \text{ cm}^{-1}$ with predominance of the states with  $J_z = \pm 1$  [37]. Next level is more than 100 cm<sup>-1</sup> above the ground level but the high  $J_z = \pm 7$  make it reachable on application of a strong external magnetic field. Ho<sup>3+</sup> has no moment for zero field but the relatively near excited doublet produces magnetic polarization by moderate magnetic fields. For a magnetic field in the *ab*-plane, the behavior is as van Vleck paramagnet with a large susceptibility. We can assume small changes of the crystal-field levels on going to HoCrO<sub>4</sub>. Therefore, at first, a Schottky anomaly in the zero-field heat capacity (Fig. 3) with maximum near 13 K is expected, due to the thermal occupation of the CF levels,

in addition to the magnetic contribution of  $Cr^{5+}$ . This latter contribution is related to a peak at  $T_C = 17.4(2)$  K which hide somewhat the Schottky anomaly.

The peak becomes a round anomaly under a small field of 1 T, therefore



Figure 3: Heat capacity of the zircon phase of  $\text{HoCrO}_4$  under several applied magnetic fields. Dashed green line: Estimation of the phonon contribution. Dotted red line: Contribution of the first two crystal-field levels of  $\text{Ho}^{3+}$ . Solid blue line: sum of phonon and crystal-field contributions.

it is due to the FM ordering of the  $Cr^{5+}$  ions, as also deduced from magnetic susceptibility [12]. The magnetic entropy just above the peak (e. g. at 26.3 K), where the magnetic contribution of the  $Cr^{5+}$  ions should be  $S_m/R =$ ln(2), is actually S(26.3 K)/R = 2.31. It turns out that the sum of the magnetic part, plus the phonon contribution,  $S_{ph}/R = 0.28$ , plus that of the CF levels,  $S_{CF}/R = 1.55$ , make a total of S/R = 2.52. The value is near that calculated, and most probably the difference is due to a an imprecise estimation of the CF levels in HoCrO<sub>4</sub>, taken from HoVO<sub>4</sub>. In any case the heat capacity at zero field can be semiquantitatively explained by the sum

# of the phonon plus magnetic plus CF contributions at low temperature.

### 3.2. Heat capacity of scheelites

240 3.2.1. HoCrO<sub>4</sub>

245

This compound orders antiferromagnetically as reported from  $\chi$ -data [12]. However this reference gives 7.6 K as Néel temperature, although the present heat capacity data shows a very clear  $\lambda$ -anomaly with the sharp maximum at  $T_N = 24.8(2)$  K (Fig. 4). If the maximum in  $\chi$  is associated to weakferromagnetism is to study.

The CF of Ho<sup>3+</sup> in LiF-scheelites has been studied by several techniques. A recent direct determination of the CF levels by inelastic neutron scattering in HoLiF<sub>4</sub> is given in [32]. The ground manifold of the free ion Ho<sup>3+</sup>,  ${}^{5}I_{8}$ , splits into four doublets and nine singlets.



Figure 4: Black symbols: Heat capacity of  $HoCrO_4$  (scheelite) at zero field. Blue line: heat capacity of LaNbO<sub>4</sub>, taken as phonon contribution. Green symbols: Magnetic heat capacity at zero field,  $C_m$ , deduced as the experimental data minus the phonon contribution. Red line: Contribution of the crystal-field levels of Ho in HoLiF<sub>4</sub>, after [28], for comparison. Green line: Magnetic entropy.



Figure 5: Heat capacity under applied magnetic field (left side scale) and entropy (right side scale) of the scheelite phase of  $HoCrO_4$ .

In the scheelite  $HoCrO_4$ ,  $Ho^{3+}$  is expected to be under a more intense CF 250 than in HoLiF<sub>4</sub>. Moreover in the Cr-scheelite the Cr-Ho exchange, similarly to a staggered magnetic field, polarizes the  $Ho^{3+}$  ions, especially the ground doublet, mainly made of  $|J_z\rangle = |\pm 7\rangle$  states, below  $T_N$ , when the Cr<sup>5+</sup> orders. The heat capacity has a bump with maximum at 8 K that can be assigned to the thermal occupation of the lowest three CF levels. The phonon 255 contribution is estimated as the heat capacity of LaNbO<sub>4</sub> (*i.e.* fs = 1). The magnetic contribution is deduced by subtraction of last two data sets. For comparison, the calculated contribution for the CF levels of  $Ho^{3+}$  in  $HoLiF_4$ is included. The CF levels cannot be deduced from heat capacity, since a fitting would be ill conditioned, but it is clear than the excess with respect to  $LaNbO_4$  is due to the thermal population of the CF levels well above  $T_N$  (*i.e.* say above 40 K), and to a combination of that and the magnetic contribution of  $Cr^{5+}$  below this temperature. In this range only the first three CF levels (one doublet and one singlet) are significantly populated and the entropy clearly tends to the theoretical upper limit  $S_m(T \to \infty)/R =$ 265  $\ln(2) + \ln(3) = 1.79$ , before the thermal occupation of higher CF levels will become relevant. The bump near 8 K can be related to the observed increase in susceptibility [12]. It would be due to two combined effects. First, a larger energy difference between the ground doublet and the first excited CF level in  $HoCrO_4$ . Second, the splitting of the ground doublet by the exchange with 270  $Cr^{5+}$ , which apparently is not intense enough to do it at  $T_N$ .

Under a weak or moderate external magnetic field of 1 T, the heat capacity does not change substantially (Fig. 5), as correspond to an antiferromagnet. For a field of 5 T or stronger the  $\lambda$ -anomaly change slightly, the maximum becoming more round and shifting to lower temperatures. Apparently, the spin-flop field of  $Cr^{5+}$  would above 9 T. Contrarily the bump near 8 K shifts to higher temperatures for a field of 5 T or stronger. This fact can be understood if such external field is higher than the spin-flip value for the staggered polarizing field produced by  $Cr^{5+}$ .

280 3.2.2. ErCrO<sub>4</sub>

This phase shows similar features to the Ho scheelite , although the CF splitting scheme of  $\text{Er}^{3+}$  is quite different. A peak in the heat capacity at  $T_N = 24.2$  K (Fig. 6) indicates an AF ordering below this temperature, which we assign to the  $\text{Cr}^{5+}$  atoms, with a small contribution of the  $\text{Er}^{3+}$  as discussed in section 3.4. The crystal-field levels of  $\text{Er}^{3+}$ -doped  $A\text{MoO}_4$  (A = Ca, Sr, Pb) scheelites have been deduced from the EPR data [26].



Figure 6: Heat capacity (open symbols, left side scale) and entropy (solid symbols, right side scale) of the scheelite phase of  $\text{ErCrO}_4$ . Lines: solid,  $C_p/R$  dashed, S/R. Blue line: phonon contribution estimated by corresponding states from LaNbO<sub>4</sub> with fs = 1.00. Black line: Contribution of  $\text{Er}^{3+}$  as deduced from the crystal-field levels given in the text. Red line: sum of phonon and  $\text{Er}^{3+}$  contributions.

The ground free-ion manifold  ${}^{4}I_{15/2}$  splits into 8 Kramers doublets under the local  $D_{2d}$  symmetry. In these compounds the spectrum consist of a ground doublet, two doublets at almost the same energy between 23 and 45 cm<sup>-1</sup>, depending on the compound, a fourth doublet near 50-65 cm<sup>-1</sup> and the last four doublets above 245 cm<sup>-1</sup>. In ErLiF<sub>4</sub> the splittings are similar but the second pair of doublets lies at 18 and 20 cm<sup>-1</sup> [29]. Therefore only the position of the second and the third doublet change substantially from one compound to another. In addition to this, in ErCrO<sub>4</sub>, the effective

- field produced by the ordered  $Cr^{5+}$  ions splits each doublet. For  $ErCrO_4$ , a simplified choice from the data for  $ErLiF_4$  is considered based on: 1) In the range 0-50 K practically only the first four doublets contribute. 2) The exchange with the  $Cr^{5+}$  ion would split each doublet. We adjust only the splitting of the ground doublet and keep approximately the same values for the next two doublets. 3) Upper levels practically do not contribute and we
- take the same values as for  $\text{ErLiO}_4$ . That is, we take the energy levels, in kelvin, as -7, 7, 20, 35, 50, 70, 89, 343, 404, 445, 494. The first 6 levels are singlets (split by the exchange with  $\text{Cr}^{5+}$ ) and the last 5 levels are double degenerate (the exchange splitting is neglected).
- This estimation is somewhat arbitrary, but there are some unambiguous effects. First, at zero external field, the Schottky-like anomaly with maximum near 10 K is essentially due to the thermal occupation of the first excited

states of  $\text{Er}^{3+}$ . Second, the low temperature tail of the anomaly cannot be explained without considering the splitting of the ground doublet by the effective exchange field produced by  $\text{Cr}^{5+}$ . Third, this exchange field is much weaker than in zircons and the polarization of the ground doublet (most probably all doublets) is negligible at  $T_N$  or above. Fourth, an external field up to 9 T does not changes the peak at  $T_N = 24.1(2)$  K, due entirely to the  $\text{Cr}^{5+}$  ions. That means that the spin-flop field for the  $\text{Cr}^{5+}$  ions is quite higher than this value, as usual dealing with 3*d*transition metals.

Considering the splitting of the ground doublet,  $\Delta E_0 = 14$  K, and the experimental magnetic moment of  $\mathrm{Er}^{3+}$  at very low temperature [23],  $\mu$  (Er) = 5.1  $\mu_B$ , an effective staggered exchange field,  $B_{ex} \simeq \Delta E_0/(2\mu(\mathrm{Er})) = 2$  T, is estimated. At very low temperature (e. g. at 2 K) an external field above this value, applied along the easy direction would flip the  $\mathrm{Er}^{3+}$  moments aligning along the external field. The shoulder in  $C_{p,B}$  with maximum near 10 K does not change with applied magnetic fields of 1 T or less (Fig. 6). For high fields the maximum moves to higher temperatures. This change of behavior seems due to a spin-flip transition occurring in the Er sublattice for a field near 1.2 T, as evidenced by a sudden slope change in the magnetization data against field at 2 K [23]. It should be considered that in a powder sample the change is gradual. Therefore the maximum magnetization, measured only up to 5 T, seems compatible with a moment of 5.1  $\mu_B$ .

After subtraction of the phonon contribution the entropy at zero field and  $T \simeq 60$  K is  $(S - S_{ph})/R = 2.25$ . The entropy of Cr<sup>5+</sup> is surely very close to  $\ln(2) = 0.693$ , which leaves  $1.55 = \ln(4.7)$  for Er<sup>3+</sup>, which compares with the theoretical estimation  $1.38 = \ln(4)$ . Assuming a minor contribution of the upper doublets, it is clearly the contribution of the first two doublets, taken at 0 and 27.5 K, since well above  $T_N$  no splitting of the doublets is expected.

 $_{335}$  3.2.3.  $TbCrO_4$ 

As explained below, Tb scheelite is also AFM but behaves quite differently to Er and Ho ones. In the isostructural TbLiF<sub>4</sub> the lowest free ion term, <sup>7</sup>F<sub>6</sub> splits into 3 doublets and 7 singlets, but the two lowest lying ones form a quasi doublet, of two levels just separated by 1.4 K [30], while the next level is about 100 K above. The wavefunctions corresponding to the two lowest levels are combinations of  $|\pm 6\rangle$  and  $|\pm 2\rangle$  but with the major contribution coming from the  $J_z = \pm 6$  states. Tb<sup>3+</sup> behaves as a quasi perfect Ising ion, with FM dipolar interaction. The magnetic moment at low temperature is  $\mu = 8.93 \ \mu_B$ , slightly lower than for the free ion,  $\mu = 9 \ \mu_B$ . Tb<sup>3+</sup> orders



Figure 7: Isothermal magnetization of the scheelite TbCrO<sub>4</sub> in emu/g (left side scale) and in  $\mu_B/fu$  (right side scale).



Figure 8: Heat capacity (left side scale) and entropy (right side scale) of the scheelite phase of  ${\rm TbCrO_4}$ .

ferromagnetically at  $T_C = 2.86$  K via dipolar interaction [30].

These features can be transferred to some extent to the scheelite TbCrO<sub>4</sub>, where the crystal field splitting is higher. Additionally, the main exchange interaction is Cr<sup>5+</sup>-Cr<sup>5+</sup>. This compound has been described as AFM with  $T_N = 29$  K and the moments along the *c*-axis at 2 K [14]. However, below  $T_N$  and similarly to the scheelite DyCrO<sub>4</sub> [38], TbCrO<sub>4</sub> undergoes a metamagnetic transition. New magnetization measurements have been done with narrower temperature step (Fig. 7), in order to deduce the MCE via the Maxwell relation. The *M*-data show a sudden increase at  $B_{sf} = 2.6$  T below  $T_N$  that can be associated to the spin-flip transition in an Ising system. In a powder sample the jump in *M* is not discontinuous due to the random orientation of the grains. Consequently, in spite of the metamagnetic transition *M* does not reach the theoretical saturation value,  $M_s \simeq 10\mu_B/fu$ , for a high

field as 9 T.

380

The DC molar susceptibility,  $\chi$ , between  $T_N$  and 50 K, follows the Curie-Weiss law,  $\chi = C/(T+\theta)$  with  $C = 21.60 \ \mu_B K f u^{-1} T^{-1}$  and  $\theta = -3.6$ 360 K. For two different atoms in the formula unit (*i.e.*  $Cr^{5+}$  and  $Tb^{3+}$ ) the Curie constant results  $C = N_A \mu_B^2 / (3k_B) \times [g_1^2(s_1(s_1+1) + g_2^2 s_2(s_2+1)/3],$ where the divisor 3 for the contribution of  $Tb^{3+}$  comes from the random grain orientation in a powder sample containing a strongly uniaxial anisotropic ion, and assuming negligible its perpendicular susceptibility. Because for  $Cr^{5+}$ . 365  $g_1 = 2, s_1 = 1/2$ , the contribution of Cr is 0.672  $\mu_B K f u^{-1} T^{-1}$ . For  $Tb^{3+}$ , considering an Ising pseudo-spin 1/2,  $g_2 = 18$ ,  $s_2 = 1/2$  accounts 18.1  $\mu_B$ K  $fu^{-1}T^{-1}$ , the Curie constant is  $C = 18.8 \ \mu_B K fu^{-1}T^{-1}$ . This value is similar to the experimental one, but slightly lower since most probably the perpendicular susceptibility is not exactly zero. In any case, the experimental 370 value is far from that for free ions, obtained taking  $g_2 = 1.5$  (the Landé factor for the term  ${}^{7}F_{6}$ ) and  $s_{2} = J = 6$ . Only at temperatures much higher than the crystal-field splitting (i. e. at RT or higher) the free ion C values are expected. This departure from the free-ion behavior occurs also in the zircon phase and has important consequences on the MCE (see below). 375

The heat capacity (Fig. 8) at zero field has a  $\lambda$ -type anomaly at  $T_N = 28.2 \pm 0.2$  K, corresponding to an AFM ordering of both magnetic ions, as previously reported from AC susceptibility, heat capacity, and neutron diffraction [13, 14]. At that time there were not reliable data to estimate the phonon contribution and no many conclusions could be extracted from heat capacity. Using precise measurements of  $C_p$  in the non-magnetic isostructural

 $LaNbO_4$  [25], the magnetic contribution could be deduced. If the CF levels of



Figure 9:  $\Delta S_T$  of TbCrO<sub>4</sub>, zircon. Data from heat capacity, from isothermal magnetization and directly measured.

Tb<sup>3+</sup> in TbLiF<sub>4</sub> would be also considered valid for TbCrO<sub>4</sub> the total magnetic entropy should be  $S_m(T >> T_N)/R = \ln(2) + \ln(2)$ , as the sum of the Cr<sup>5+</sup> and the Tb<sup>3+</sup> contributions. Actually the experimental entropy (up to 85 K) is  $S_m(T >> T_N)/R = 1.81 \simeq \ln(2) + \ln(3)$ . This entropy content indicates that well above  $T_N$  there are three populated levels of Tb<sup>3+</sup>, meaning that a singlet has much lower energy than in TbLiF<sub>4</sub>. Under an applied field of 1 T the peak does not change, as corresponds to an AFM configuration, but under 3 T (Fig. 3 in [14]) or higher it becomes a round anomaly according to the *M* data, showing a spin-flip transition for 2.6 T.

### 3.3. Magnetocaloric effect of zircons

The MCE of GdCrO<sub>4</sub> was previously reported [4]. The anisotropy energy of Gd<sup>3+</sup> is about 1 K, then negligible in the temperature range considered in this work. The exchange interaction Gd<sup>3+</sup>-Cr<sup>5+</sup> is significantly weaker than the Cr<sup>5+</sup>-Cr<sup>5+</sup> one, but much stronger than the Gd<sup>3+</sup>-Gd<sup>3+</sup> one. In such circumstance Gd<sup>3+</sup> is only weakly polarized by Cr<sup>5+</sup> at  $T_C = 21.3$  K, which leaves room to polarize it by an external field well below  $T_C$ , differently of most ferromagnets. As a consequence, GdCrO<sub>4</sub> has strong MCE in a wide temperature range, overcoming 20 J/kg.K between 5 K and 35 K for B = 9T. Taking the data for B = 5 T as most frequently reported, the maximum entropy change is  $|\Delta S_{T,max}| = 19.0$  J/kg<sup>-1</sup>K<sup>-1</sup> at 22 K.

 $\Delta S_T$  of TbCrO<sub>4</sub> (Fig. 9) has been deduced in the three ways indicated in section 2.3.1. The results indicate graphically the limitations of each method, although all of them agree near the maximum. In this case the heat capacity

can be extrapolated to  $T \rightarrow 0$ . Therefore  $T_0 = 0$  was taken in eq. (1) and each determination is independent. For B = 5 T a moderate maximum value  $\Delta S_{T,max} = 16.4 \text{ J kg}^{-1} \text{ K}^{-1}$  is obtained at 23 K. As mentioned above, in the paramagnetic state of  $TbCrO_4$  the JT distortion near 60 K splits the CF quasi-quartet into two quasi-doublets, the higher one being thermally 410 depopulated near  $T_C$ . Adding the contribution of  $Cr^{5+}$  that gives an initial total magnetic entropy  $\Delta S_{ini,m}/R \simeq 2 \ln(2) = 1.39$ . Correspondingly, this value is an upper bound for the entropy reduction by magnetic field well below 60 K, despite the high magnetic moment of  $Tb^{3+}$  ( $\mu = 7.6 \ \mu_B \ [9]$ , higher than the  $Gd^{3+}$  moment, but in any case quite lower than that value 415 for free Tb<sup>3+</sup>,  $\mu$ (free) = 9  $\mu_B$ ) and the large angular moment, J = 6. If the ideal zircon structure would remain down to very low temperatures the initial entropy of  $Tb^{3+}$  would be near  $\ln(4)$ . Therefore the JT distortion makes the entropy change quite lower than for other  $RCrO_4$  in the zircon phase.

<sup>420</sup> As mentioned before, in HoVO<sub>4</sub>, Ho<sup>3+</sup> behaves as a van Vleck paramagnet [18]. The ground state is not magnetic but the first excited one is a doublet lying only 19.5 cm<sup>-1</sup> above. It consist of two states with opposite high magnetic moments and thermally populated near 20 K or above. The magnetic entropy can be deduced from heat capacity data. In the case of HoCrO<sub>4</sub>, just <sup>425</sup> above  $T_C$  (e.g. T = 30 K) the initial magnetic entropy S(30 K, B = 0)/R =1.74 and can be understood as a contribution from  $\text{Cr}^{5+}$ , close to  $\ln(2)$ , and another one from Ho<sup>3+</sup>, estimated from experiment as  $1.74 - \ln(2) = 1.05$ . This value is lower than in HoVO<sub>4</sub> which indicates a higher crystal-field splitting in the Cr compound. For the two-level approximation (neglecting the thermal occupation of higher levels) this entropy corresponds to a splitting around 45 K (31 cm<sup>-1</sup>), or lower if  $S_m(\text{Cr}^{5+})/R < \ln(2)$ .

Due to the high moment of the system this relatively high initial entropy can be easily reduced by an external field. Consequently, the MCE (Fig. 10) is stronger than for TbCrO<sub>4</sub>, with  $|\Delta S_T|$  reaching 30.7 J kg<sup>-1</sup> K<sup>-1</sup> for B = 9 T (or 21.2 J kg<sup>-1</sup> K<sup>-1</sup> for 5 T), near  $T_C$ . The data from heat capacity agree with those deduced from isothermal magnetization [7], especially when the demagnetization factor (lower for the magnetization experiment) is considered. The maximum  $|\Delta S_{T,max}|$  overcomes that of GdCrO<sub>4</sub> at the same temperature, but decays much faster below  $T_C$ .

440

Due to the high anisotropy of  $\text{Ho}^{3+}$ , there is another possible and interesting property of HoCrO<sub>4</sub>. This compound orders ferromagnetically in the *ab*-plane [9] of the tetragonal zircon structure. The entropy reduction would be strong when the field is applied in that plane, but much smaller when



Figure 10:  $\Delta S_T$  of HoCrO<sub>4</sub>, zircon. Solid symbols: Data from heat capacity. Open symbols: Data from isothermal magnetization. At  $T_0 = 40$  K,  $\Delta S_T$  has been taken from the magnetization data in order to determine the absolute entropy for lower fields.

applied in the *c*-direction. Therefore a highly anisotropic MCE can be ex-<sup>445</sup> pected in a single crystal. The present results have been obtained in powder, when the random orientation of grains inhibits a complete orientation of the moments along the field. Actually even at 5 K ( $T \simeq T_c/4$ ), in the FM state the saturation is not reached for a so strong field as 8 T. In a single crystal, or in a previously oriented sample by an external field, there would be a <sup>450</sup> strong MCE by a 90° rotation in a constant field. This anisotropy has been invoked as an interesting MCE effect by rotation in a constant field (e. g. in Dy(HCOO)<sub>3</sub> [39]), but usually such systems are pseudo-Ising, with a modest maximum molar entropy change of  $R \ln(2)$ . In HoCrO<sub>4</sub> the presence of two magnetic atoms and the higher initial entropy of Ho<sup>3+</sup> would enhance this effect.

 $\Delta S_T$  of the ErCrO<sub>4</sub> zircon has been deduced from magnetization (Fig. 11). It is similar to that of HoCrO<sub>4</sub> in spite of a quite different CF levels scheme. In ErVO<sub>4</sub> the free-ion manifold of Er<sup>3+</sup>, <sup>4</sup>I<sub>15/2</sub>, splits into 8 Kramers doublets. The first excited doublet is at 43 cm<sup>-1</sup> [18] and is not thermally populated. It orders AFM at 0.4 K. The close related zircon ErCrO<sub>4</sub> is AFM below  $T_N = 15$  K, but the very weak spin-flip field near 0.04 T provokes a parallel alignment of the moments with a stronger field [21].  $|\Delta S_T|$ , obtained from isothermal magnetization data, shows a maximum of about 20 J/kg.K at 15 K for a field of 5 T. Dong *et al.* [17] do not report any spin-flip at low temperature and describe the transition at 15 K as FM, although the neutron diffraction experiment [21] shows an AFM spin configuration at 2 K



Figure 11:  $\Delta S_T$  of ErCrO<sub>4</sub>, zircon from magnetization data.

and zero field. Probably the existence of a small spin-flip field or not could be due to the external shape of the sample, via the demagnetizing field. The moment at 5 K, for B = 5 T,  $\mu = 7 \mu_B/fu$  is largely below the maximum for the free atom (9  $\mu_B$ ) plus that of Cr<sup>5+</sup> (1  $\mu_B$ ), which makes 10  $\mu_B$ . This 470 behavior in a powder sample seems due to the random orientation of the grains with respect to the external field, along with a strong anisotropy as revealed by the crystal-field splitting of the  $Er^{3+}$  ion. In powder,  $ErCrO_4$ has lower MCE than  $HoCrO_4$ , since the ground state is a Kramers doublet (*i. e.* the molar initial entropy of  $Er^{3+}$  is only  $R\ln(2)$ ) but it could be more 475 anisotropic and interesting in single crystal due to a strong MCE by rotation

in a constant field.

The mean-field calculation given in [17] is made under the assumption that  $Cr^{5+}$  and  $Er^{3+}$  behave together as an average free ion, with J = 6 and g = 15/14, which is not physically justified. Actually for a free ion is L = 6, 480 S = 3/2, J = 15/2, g = 102/85, which gives the maximum moment of 9  $\mu_B$ . The fair agreement of the calculated  $\Delta S_T$  at high temperatures with the experimental data is due to the average over the directions in a powder sample. But the saturation moment in the model is  $6 \mu_B/fu$  that is already surpassed by the experimental magnetization data at 2 K with a field of only 3 T, when M is far from saturation.

#### 485

# 3.4. Magnetocaloric effect of scheelites.

The scheelites are AFM, which reduces the MCE with respect to zircons. This fact overrides the use as practical refrigerators, but the study of their MCE reveals interesting chemical and physical features. The most intense in-



Figure 12:  $\Delta S_T$  of TbCrO<sub>4</sub>, scheelite. Only three curves are depicted for clarity. Vertical line: Temperature taken to set the entropies with respect to that of 9 T. Dashed lines: Curie-Weiss-like (Eq. 3) curves.

teraction is the AFM  $Cr^{5+}-Cr^{5+}$  exchange, as revealed by compounds where the rare earth site is occupied by a non magnetic ion. The MCE depends on the exchange between the  $R^{3+}$  and  $Cr^{5+}$ . In TbCrO<sub>4</sub>, Tb<sup>3+</sup> orders simultaneously with  $Cr^{5+}$ , as deduced by the heat capacity and isothermal magnetization. Consequently the MCE is conventional for an antiferromagnet. That is, for  $T > T_N$  and moderate fields  $\Delta S_T$  follows a sort of Curie-Weiss law for the entropy [24]

$$\frac{\Delta S_T}{R} \simeq -\frac{[C(\text{Tb})/3 + C(\text{Cr})]B^2}{2R(T+\theta)^2}$$
(3)

the Curie constants being  $C = N_A \mu_B^2 g^2 s(s+1)/3k_B$ , as for susceptibility (section 3.2.3), Tb<sup>3+</sup> considered as an Ising pseudo-spin, g = 18, s = 1/2. The quasi-Ising behavior of the Tb<sup>3+</sup> ion and the positive value of  $\theta \simeq T_N =$ 490 25 K reduces the entropy change in a powder sample with respect to other compounds with lower atomic magnetic moment (Fig. 12). In this sense, even for a single crystal if the field was applied in the easy direction, for high B values  $\Delta S_T$  is smaller than expected for a free ion Tb<sup>3+</sup>, although the magnetic moment is approximately the same. It is so because the lowest 495 manifold term of the free  $Tb^{3+}$  is  ${}^{7}F_{6}$  with an initial entropy at zero field  $S_m(\text{Tb})/R = \ln J(J+1) = \ln(42) = 3.74$ , instead of  $\ln(2) = 0.69$ . When the field is applied along the easy direction, the magnetization saturates easily above the spin-flip field, that in the case of  $TbCrO_4$  is estimated in 2.6 T (Fig. 7). 500



Figure 13:  $\Delta S_T$  of HoCrO<sub>4</sub>, scheelite phase.



Figure 14:  $\Delta S_T$  of ErCrO<sub>4</sub>, scheelite phase.

Quite differently, in  $HoCrO_4$  (Fig. 13) and  $ErCrO_4$  (Fig. 14) the maximum entropy change for a given field variation occurs well below  $T_N$ , which cannot be distinguished in the  $\Delta S_T$  data for the Er compound and with only as a small kink in the Ho one. This behavior is very unusual in an antifer-505 romagnet and can be explained if the rare earth is very weakly polarized by the effective exchange field of  $Cr^{5+}$  and the contribution of the rare earth to the entropy is not significantly reduced by the AFM ordered  $Cr^{5+}$  ions. Consequently, the rare earth behaves in a similar way to a paramagnet. Nevertheless, between 5 K and 50 K, neither  $Ho^{3+}$  nor  $Er^{3+}$  do not behave as 510 simple Ising systems (the ground doublet in each case). The bump in  $C_{n,B}$ near 8 K in both cases indicates that upper levels, mainly the first excited singlet, are thermally populated. Therefore the effect of an external magnetic field on the excited levels, especially the first excited one, cannot be neglected. In these conditions the contribution of the rare earth to the MCE is much stronger than expected for an antiferromagnet below  $T_N$ . Oppositely the unchanged peak in  $C_{p,B}$  at  $T_N$  indicates that the magnetic field affects weakly to  $Cr^{5+}$  below  $T_N$ .

### 4. Conclusions

The MCE of the zircon and scheelite phases of  $R \text{CrO}_4$  (R = Tb, Ho, Er) have been studied in the range 5 K - 100 K. According to the reported data the zircons are ferromagnetic (ErCrO<sub>4</sub> is AF with a very weak spin-flip field) and the scheelites are antiferromagnetic. New data of magnetization and heat capacity have been used to obtain the isothermal entropy increment,  $\Delta S_T$ , on application of an external magnetic field up to 9 T.

The results can be compared with the previous ones for the zircon GdCrO<sub>4</sub>. In this compound, where Gd<sup>3+</sup> has no relevant anisotropy in the temperature range of this study, the exchange with  $Cr^{5+}$  is moderately weak in such a way that it is not strong enough to polarize Gd<sup>3+</sup> but helps to an external field to produce below  $T_C$  a much stronger MCE than a paramagnet and a ferromagnet below  $T_C$ .

The compounds presented here are in the other extreme of high anisotropy. Speaking about zircon, the Tb compound undergoes a co-operative JT transition near 60 K. The JT transition is reflected by a jump in heat capacity <sup>535</sup> due to the change of the low lying crystal-field levels of Tb<sup>3+</sup> from a quasiquartet to two highly spaced quasi-doublets. This fact (*i. e.* the low initial entropy of a system for only two levels) is the reason for the relatively low MCE near  $T_C = 22$  K, when  $|\Delta S_T| = 16.3$  J kg<sup>-1</sup> K<sup>-1</sup> for B = 5 T, despite the high magnetic moment.

540

545

The scheelite phase of TbCrO<sub>4</sub> does not undergo a JT transition. Since the electrostatic interaction Tb<sup>3+</sup>-O<sup>2-</sup> is stronger than Tb<sup>3+</sup>-F<sup>-</sup>, in the scheelite TbLiF<sub>4</sub> most probably there are several CF levels thermally populated near  $T_N = 29$  K. Due to the relatively strong exchange coupling between Cr<sup>5+</sup> and Tb<sup>3+</sup> and the high moment of Tb<sup>3+</sup> the spin-flip field is relatively low and the MCE has the typical features of an antiferromagnet.

In the zircon phase the MCE of HoCrO<sub>4</sub> looks like in a conventional ferromagnet, with a high maximum just above  $T_C = 17$  K. The lowest crystal field levels are a non-magnetic singlet and one doublet nearly above. That allows a relatively high initial entropy at  $T_C$ . Consequently the MCE is strong near  $T_C$  with  $|\Delta S_T| = 30.7$  J/kg.K, but decays quickly below, when the only populated state at zero field is the singlet. The MCE of the zircon ErCrO<sub>4</sub> shows similar features to ErCrO<sub>4</sub>, although the CF splitting scheme is different.

In the scheelite phase Ho and Er compounds behave also similarly. The  $R^{3+}$ -Cr<sup>5+</sup> exchange coupling seems much weaker than in the Gd compound. Extrapolating from  $R\text{LiF}_4$  scheelites, the lowest CF states are two Kramers doublets for Er<sup>3+</sup> and a non-Kramers doublet and a singlet for Ho<sup>3+</sup>. In both cases the heat capacity has a Schottky-like anomaly due to the thermal population of these levels. Due to the weak  $R^{3+}$ -Cr<sup>5+</sup> coupling the MCE seems to that a paramagnet. Strikingly,  $|\Delta S_T|$  is much higher below  $T_N$ , where probably only Cr<sup>5+</sup> is substantially ordered.

### Acknowledgments

This work has been funded by Spanish MINECO and FEDER (Projects MAT2017-86019-R and MAT2017-84385-R), Gobierno de Aragón (Consolidated Group E100). Authors would like to acknowledge the use of the Servicio General de Apoyo a la Investigación-SAI, Universidad de Zaragoza.

 W. F. Giauque, D. P. MacDougall, Attainment of temperatures below 1° absolute by demagnetization of Gd<sub>2</sub>(SO<sub>4</sub>)<sub>3</sub>·8H<sub>2</sub>O, Phys. Rev. 43 (1933) 768–768. doi:10.1103/PhysRev.43.768.

570

URL https://link.aps.org/doi/10.1103/PhysRev.43.768

[2] P. J. Shirron, Applications of the magnetocaloric effect in single-stage, multi-stage and continuous adiabatic demagnetization refrigerators, Cryogenics 62 (2014) 130-139. doi:https://doi.org/10.1016/j.cryogenics.2014.03.014. URL https://www.sciencedirect.com/science/article/pii/S0011227514000654

575

580

[3] H. Zhang, R. Gimaev, B. Kovalev, K. Kamilov, V. Zverev, A. Tishin, Review on the materials and devices for magnetic refrigeration in the temperature range of nitrogen and hydrogen liquefaction, Physica B: Condensed Matter 558 (2019) 65–73. doi:https://doi.org/10.1016/j.physb.2019.01.035.

URL https://www.sciencedirect.com/science/article/pii/S0921452619300316

[4] E. Palacios, C. Tomasi, R. Sáez-Puche, A. J. Dos santos García, F. Fernández-Martínez, R. Burriel, Effect of Gd polarization on the large magnetocaloric effect of GdCrO<sub>4</sub> in a broad temperature range, Phys. Rev. B 93 (2016) 064420. doi:10.1103/PhysRevB.93.064420.

URL https://link.aps.org/doi/10.1103/PhysRevB.93.064420

- [5] E. Palacios, C. Tomasi, R. Saez-Puche, A. J. dos Santos-Garcia, F. Fernandez-Martinez, R. Burriel, Enhanced magnetocaloric effect by the rare earth polarization due to the exchange with a transition metal - study of GdCrO<sub>4</sub>, in: Solid Compounds of Transition Elements, Vol. 257 of Solid State Phenomena, Trans Tech Publications Ltd, 2017, pp. 139–142. doi:10.4028/www.scientific.net/SSP.257.139.
- [6] E. Jimenez-Melero, P. Gubbens, M. Steenvoorden, S. Sakarya, A. Goosens, P. D. De Réotier, A. Yaouanc, J. Rodríguez-Carvajal, B. Beuneu, J. Isasi, et al., A combined study of the magnetic properties of GdCrO<sub>4</sub>, Journal of Physics: Condensed Matter 18 (34) (2006) 7893. doi:https://doi.org/10.1088/0953-8984/18/34/004.
- [7] A. Midya, N. Khan, D. Bhoi, P. Mandal, 3d-4f spin interaction induced giant magnetocaloric effect in zircon-type DyCro<sub>4</sub> and HoCrO<sub>4</sub> compounds, Applied Physics Letters 103 (9) (2013) 092402. doi:10.1063/1.4819768.
- [8] E. Jiménez, J. Isasi, R. Sáez-Puche, Synthesis, structural characterization and magnetic properties of  $R \text{CrO}_4$  oxides, R = Nd, Sm, Eu and Lu, Journal of Alloys and Compounds 312 (1) (2000) 53–59. doi:https://doi.org/10.1016/S0925-8388(00)01079-3.
- URL https://www.sciencedirect.com/science/article/pii/S0925838800010793

585

595

590

605

600

- [9] E. Jiménez-Melero, Estudio cristalográfico y magnético de óxidos RCrO<sub>4</sub> (R =tierra rara), Ph.D. thesis, Facultad de Ciencias Químicas (2005). URL https://eprints.ucm.es/id/eprint/7130/
- <sup>610</sup> [10] K. Tezuka, Y. Doi, Y. Hinatsu, Crystal structures and magnetic properties of zircon-type compounds lu 1- x y x cro 4, Journal of Materials Chemistry 12 (4) (2002) 1189–1193. doi:10.1039/B108483F.
  - [11] R. Sáez-Puche, E. Jiménez, J. Isasi, M. T. Fernídez-Dáz, J. L. García-Muoz, Structural and magnetic characterization of RCrO<sub>4</sub> oxides (R =
- Nd, Er and Tm), Journal of Solid State Chemistry 171 (1) (2003) 161–
  169, proceedings from the 23rd Rare Earth Research Conference UC
  Davis Campus, July 13-16, 2002. doi:https://doi.org/10.1016/S00224596(02)00203-7.
  URL https://www.sciencedirect.com/science/article/pii/S0022459602002037
- [12] E. Climent-Pascual, J. Romero de Paz, J. M. Gallardo-Amores, R. Sez-Puche, Ferromagnetism vs. antiferromagnetism of the dimorphic HoCrO<sub>4</sub> oxide, Solid State Sciences 9 (7) (2007) 574–579, bordeaux June 2006. doi:https://doi.org/10.1016/j.solidstatesciences.2007.03.003. URL https://www.sciencedirect.com/science/article/pii/S1293255807000441
- E. Climent, J. Gallardo, J. R. de Paz, N. Taira, R. S. Puche, Phase transition induced by pressure in TbCrO<sub>4</sub> oxide: Relationship structureproperties, Journal of Alloys and Compounds 488 (2) (2009) 524–527, proceedings of the 25th Rare Earth Research Conference, June 22-26, Tuscaloosa, Alabama, USA. doi:https://doi.org/10.1016/j.jallcom.2008.10.060.

URL https://www.sciencedirect.com/science/article/pii/S0925838808017155

- [14] E. Climent Pascual, J. M. Gallardo Amores, R. Sáez Puche, M. Castro, N. Taira, J. Romero de Paz, L. C. Chapon, Zircon to scheelite phase transition induced by pressure and magnetism in TbCrO<sub>4</sub>, Phys. Rev. B 81 (2010) 174419. doi:10.1103/PhysRevB.81.174419. URL https://link.aps.org/doi/10.1103/PhysRevB.81.174419
- [15] A. Dos santos-García, E. Climent-Pascual, J. Gallardo-Amores, M. G. Rabie, Y. Doi, J. Romero de Paz, B. Beuneu, R. Sáaez-Puche, Synthesis and magnetic properties of the high-pressure scheelite-type GdCrO<sub>4</sub> polymorph, Journal of Solid State Chemistry 194 (2012) 119–126.

635

640

doi:https://doi.org/10.1016/j.jssc.2012.04.044. URL https://www.sciencedirect.com/science/article/pii/S0022459612003052

[16] M. S. Rabie, Pressure-induced phase transitions in  $RCrO_4$  oxides: preparation, magnetic and electronic properties (R= rare earth, Ph.D. thesis, Facultad de Ciencias Químicas (2013).

URL https://eprints.ucm.es/id/eprint/21669/

- [17] Q. Dong, Y. Ma, Y. Ke, X. Zhang, L. Wang, B. Shen, J. Sun, Z. Cheng, Ericsson-like giant magnetocaloric effect in GdCrO<sub>4</sub>ErCrO<sub>4</sub> composite oxides near liquid hydrogen temperature, Materials Letters 161 (2015) 669-673. doi:https://doi.org/10.1016/j.matlet.2015.09.070.
  - URL https://www.sciencedirect.com/science/article/pii/S0167577X15305784
- [18] G. J. Bowden, A review of the low temperature properties of the rare earth vanadates, Australian Journal of Physics 51 (1998) 201–236. URL https://www.publish.csiro.au/PH/pdf/P97066
- [19] E. Palacios, J. A. Rodríguez-Velamazán, M. Evangelisti, G. J. McIntyre, 655 G. Lorusso, D. Visser, L. J. de Jongh, L. A. Boatner, Magnetic structure and magnetocalorics of GdPO<sub>4</sub>, Phys. Rev. B 90 (2014) 214423. doi:10.1103/PhysRevB.90.214423. URL https://link.aps.org/doi/10.1103/PhysRevB.90.214423
- [20] A. Indra, K. Dev, J. K. Dev, S. Majumdar, U. Rütt, O. Gutowski, 660 M. v. Zimmermann, S. Giri, cro<sub>4</sub> distortion-driven ferroelectric order in (r, Y)cro<sub>4</sub>(r = Sm, Gd, and Ho): A new family of multiferroics, Phys. Rev. B 98 (2018) 014408. doi:10.1103/PhysRevB.98.014408. URL https://link.aps.org/doi/10.1103/PhysRevB.98.014408
- [21] E. Jiménez, J. Isasi, M. T. Fernández, R. Sáez-Puche, Magnetic 665 behavior of  $ercro_4$  oxide, Journal of Alloys and Compounds 344 (1) (2002) 369–374, proceedings of the Rare Earths' 2001 Conference. doi:https://doi.org/10.1016/S0925-8388(02)00387-0. URL https://www.sciencedirect.com/science/article/pii/S0925838802003870
- [22] E. Jiménez, W. Kraan, N. van Dijk, P. Gubbens, J. Isasi, R. Sáez-Puche, 670 Magnetic domains in  $ercro_4$  studied by 3d neutron depolarization, Physica B: Condensed Matter 350 (1, Supplement) (2004) E293–E296, proceedings of the Third European Conference on Neutron Scattering.

650

645

doi:https://doi.org/10.1016/j.physb.2004.03.073. URL https://www.sciencedirect.com/science/article/pii/S0921452604002509

[23] R. Sáez-Puche, E. Climent, M. G. Rabie, J. Romero, J. M. Gallardo, Neutron diffraction characterization and magnetic properties of the scheelite-type ErCrO<sub>4</sub> polymorph, Journal of Physics: Conference Series 325 (2011) 012012. doi:10.1088/1742-6596/325/1/012012. URL https://doi.org/10.1088/1742-6596/325/1/012012

680

685

695

675

[24] E. Palacios, M. Evangelisti, R. Sáez-Puche, A. J. Dos Santos-García, F. Fernández-Martínez, C. Cascales, M. Castro, R. Burriel, O. Fabelo, J. A. Rodríguez-Velamazán, Magnetic structures and magnetocaloric effect in RVO<sub>4</sub> (R = Gd, Nd, Phys. Rev. B 97 (2018) 214401. doi:10.1103/PhysRevB.97.214401.

URL https://link.aps.org/doi/10.1103/PhysRevB.97.214401

- [25] G. Nikiforova, A. Khoroshilov, A. Tyurin, V. Gurevich, K. Gavrichev, Heat capacity and thermodynamic properties of lanthanum orthoniobate, The Journal of Chemical Thermodynamics 132 (2019) 44–53. doi:https://doi.org/10.1016/j.jct.2018.12.041.
- doi:https://doi.org/10.1016/j.jct.2018.12.041. URL https://www.sciencedirect.com/science/article/pii/S0021961418308875
  - [26] C.-G. Li, X.-Y. Kuang, R.-P. Chai, Y.-R. Zhao, The defect structure and EPR parameters for Er<sup>3+</sup> in molybdates: a complete energy matrices study, Molecular Physics 110 (24) (2012) 3023-3029. arXiv:https://doi.org/10.1080/00268976.2012.695026, doi:10.1080/00268976.2012.695026. URL https://doi.org/10.1080/00268976.2012.695026
    - [27] Vishwamittar, S. Taneja, S. Puri, On the behaviour of  $Er^{3+}$  ion in tetragonal crystalline fields, Journal of Physics and Chemistry of
- Solids 33 (5) (1972) 965-971. doi:https://doi.org/10.1016/S0022-3697(72)80256-7. URL https://www.sciencedirect.com/science/article/pii/S0022369772802567
  - [28] P. E. Hansen, T. Johansson, R. Nevald, Magnetic properties of lithium rare-earth fluorides: Ferromagnetism in  $LiErF_4$  and  $LiHoF_4$  and crystal-
- field parameters at the rare-earth and Li sites, Phys. Rev. B 12 (1975)
   5315-5324. doi:10.1103/PhysRevB.12.5315.
   URL https://link.aps.org/doi/10.1103/PhysRevB.12.5315

 [29] H. P. Christensen, Spectroscopic analysis of LiHoF<sub>4</sub> and LiHoF<sub>4</sub>, Phys. Rev. B 19 (1979) 6564-6572. doi:10.1103/PhysRevB.19.6564.
 URL https://link.aps.org/doi/10.1103/PhysRevB.19.6564

710

730

735

- [30] J. Magariño, J. Tuchendler, P. Beauvillain, I. Laursen, EPR experiments in LiTbF<sub>4</sub>, LiHoF<sub>4</sub>, and LiErF<sub>4</sub> at submillimeter frequencies, Phys. Rev. B 21 (1980) 18-28. doi:10.1103/PhysRevB.21.18. URL https://link.aps.org/doi/10.1103/PhysRevB.21.18
- [31] I. V. Romanova, A. V. Egorov, S. L. Korableva, B. Z. Malkin, M. S. Tagirov, 19f NMR study of LiTbF<sub>4</sub> single crystals, Journal of Physics: Conference Series 324 (2011) 012034. doi:10.1088/1742-6596/324/1/012034. URL https://doi.org/10.1088/1742-6596/324/1/012034
- P. Babkevich, A. Finco, M. Jeong, B. D. Piazza, I. Kovacevic, G. Klughertz, K. W. Kramer, C. Kraemer, D. T. Adroja, E. Goremychkin, T. Unruh, T. Strässle, A. D. Lieto, J. Jensena, H. M. Rnnow, Neutron spectroscopic study of crystal-field excitations and the effect of the crystal field on dipolar magnetism in LiRF<sub>4</sub> (R = Gd, Ho, Er, Tm, and Yb), Physical Review B 92 (2015) 144422. doi:10.1103/PhysRevB.92.144422.
  - [33] E. Palacios, R. Sez-Puche, J. Romero, Y. Doi, Y. Hinatsu, M. Evangelisti, Large magnetocaloric effect in EuGd<sub>2</sub>O<sub>4</sub> and EuDy<sub>2</sub>O<sub>4</sub>, Journal of Alloys and Compounds 890 (2022) 161847. doi:https://doi.org/10.1016/j.jallcom.2021.161847.
  - URL https://www.sciencedirect.com/science/article/pii/S0925838821032564
  - [34] G. Buisson, F. Tchéou, F. Sayetat, K. Scheunemann, Crystallographic and magnetic properties of TbCrO<sub>4</sub> at low temperature (x-ray and neutron experiments), Solid State Communications 18 (7) (1976) 871–875. doi:https://doi.org/10.1016/0038-1098(76)90226-X.

URL https://www.sciencedirect.com/science/article/pii/003810987690226X

- [35] M. Wells, R. Worswick, The specific heat of terbium vanadate TbVO<sub>4</sub>, Physics Letters A 42 (4) (1972) 269–270. doi:https://doi.org/10.1016/0375-9601(72)90416-1.
- URL https://www.sciencedirect.com/science/article/pii/0375960172904161

- [36] G. A. Gehring, K. A. Gehring, Co-operative jahn-teller effects, Reports on Progress in Physics 38 (1) (1975) 1-89. doi:10.1088/0034-4885/38/1/001.
   URL https://doi.org/10.1088/0034-4885/38/1/001
- <sup>745</sup> [37] S. Skanthakumar, C.-K. Loong, L. Soderholm, M. M. Abraham, L. A. Boatner, Crystal-field excitations and magnetic properties of Ho<sup>3+</sup> in HoVO<sub>4</sub>, Phys. Rev. B 51 (1995) 12451–12457. doi:10.1103/PhysRevB.51.12451. URL https://link.aps.org/doi/10.1103/PhysRevB.51.12451
- [38] Y. Long, Q. Liu, Y. Lv, R. Yu, C. Jin, Various 3d-4f spin interactions and field-induced metamagnetism in the Cr<sup>5+</sup> system DyCrO<sub>4</sub>, Phys. Rev. B 83 (2011) 024416. doi:10.1103/PhysRevB.83.024416. URL https://link.aps.org/doi/10.1103/PhysRevB.83.024416
  - [39] G. Lorusso, O. Roubeau, M. Evangelisti, Rotating magnetocaloric effect in an anisotropic molecular dimer, Angewandte Chemie International Edition 55 (2016) n/a-n/a. doi:10.1002/anie.201510468.

## Highlights

Zircon to scheelite  $RCrO_4$  (R = Tb, Ho, Er) phase transition induced at high pressure and high temperature.

Magnetic measurements reveal that *R*CrO<sub>4</sub> Zircons behave as ferromagnetic while the *R*CrO<sub>4</sub> Scheelites are antiferromagnetic.

Heat capacity, magnetization and direct calorimetric measurements had been done in order to determine the magnetic entropy variation for both zircon and scheelite *R*CrO<sub>4</sub> oxides.

Zircon RCrO<sub>4</sub> phases show large magnetocaloric effect according to their ferromagnetic behavior. This effect appear to be lower than in the case of scheelite polymorphs.

Journal Prort

Zircon RCrO<sub>4</sub> phases show large magnetocaloric effect according to their ferromagnetic behavior. This effect as it is expected is lower in the case of antiferromagnetic scheelite polymorphs.

outral Prevence

## Highlihgts

Zircon to scheelite  $RCrO_4$  (R= Tb, Ho, Er) phase transition induced at high pressure and high temperature.

Magnetic measurements reveal that RCrO<sub>4</sub> Zircons behave as ferromagnetic while the RCrO<sub>4</sub> Scheelites are antiferromagnetic.

Heat capacity, magnetization and direct calorimetric measurements had been done in order to determine the magnetic entropy variation for both zircon and scheelite RCrO<sub>4</sub> oxides.

Zircon RCrO<sub>4</sub> phases show large magnetocaloric effect according to their ferromagnetic behavior. This effect appear to be lower than in the case of scheelite polymorphs.

ournal Prort

## **Declaration of interests**

☑ The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

□ The authors declare the following financial interests/personal relationships which may be considered as potential competing interests:

Journal Presson