

# Biomechanical characterization and constitutive modeling of the layer-dissected residual strains and mechanical properties of abdominal porcine aorta

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## Abstract

We analyze the residual stresses and mechanical properties of layer-dissected infrarenal abdominal aorta (IAA). We measured the axial pre-stretch and opening angle and performed uniaxial tests to study and compare the mechanical behavior of both intact and layer-dissected porcine IAA samples under physiological loads. Finally, some of the most popular anisotropic hyperelastic constitutive models (GOH, microfiber and four fiber models) were proposed to estimate the mechanical properties of the abdominal aorta by least-square fitting of the recorded in-vitro uniaxial test results.

The results show that the residual stresses are layer dependent. In all cases, we found that the OA in the media layer is lower than in the whole artery, the intima and the adventitia. For the axial pre-stretch, we found that the adventitia and the media were slightly stretched in the environment of the intact arterial strip, whereas the intima appears to be compressed. Regarding the mechanical properties, the media seems to be the softest layer over the whole deformation domain showing high anisotropy, while the intima and adventitia exhibit considerable stiffness and a lower anisotropy response. Finally, all the hyperelastic anisotropic models considered in this study provided a reasonable approximation of the experimental data. The four-fiber model showed the best fitting.

*Key words:* Infrarenal abdominal aorta, layer separation, residual strains, uniaxial testing, constitutive modeling, elastic properties.

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# 1 Introduction

Loss of structural integrity of the aorta can result in potentially life threatening aneurysms or dissections with a significant risk of rupture (Sassani et al., 2015a). There is, therefore, a pressing need to understand better the mechanisms underlying the stiffness and structural integrity of central arteries, both healthy and diseased. Healthy arteries are composed of three clearly defined layers. The intima (the innermost layer) consists of a single layer of endothelial cells, a thin basal membrane and a subendothelial layer; the media (the middle layer) is composed of a 3D network of elastin, smooth muscle cells and collagen fibres; and the adventitia (the outer layer) consists of fibroblasts, fibrocytes, ground matrix and thick bundles of collagen fibres (Rhodin, 1980). Given that the arterial wall is a non-homogeneous material, the best approach is to model the heterogeneity of the arterial wall by considering it as a multi-layer structure while incorporating its architecture and its different layers, the intima, media and adventitia (Holzapfel and Ogden, 2010b; Díaz et al., 2021). To the best of the authors' knowledge, the studies by Sommer et al. (2010) on human carotid arteries, Peña et al. (2015) on porcine thoracic descending aortas, Sokolis et al. (2012); Sassani et al. (2015b,a) on thoracic and abdominal aortic aneurysms and Amabili et al. (2019); Amabili et al. (2020) on human descending thoracic aorta are the only works that present the layer-specific mechanical properties and residual stresses at the same time.

The preferred methodology to describe and reproduce the mechanical behavior of arteries is the definition of a strain energy function (SEF) from which the stress response is derived, see e.g. (Alastrué et al., 2009; Holzapfel et al., 2000; Zullinger et al., 2004; Gasser et al., 2006; Holzapfel and Ogden, 2010a; Sokolis, 2010) and references therein. The response of fibers are typically assumed to be governed by exponential functions (Holzapfel et al., 2000, 2005). However, structurally-motivated material models may provide increased insights into the underlying mechanics and physics of arteries and could overcome this drawback (Weisbecker et al., 2015). The work by Gasser et al. (2006) included structural information in the model by means of the assumption of a fiber orientation following a von Mises distribution function. More recently, models including fiber dispersion from a micro-structurally based approach

have been proposed using an axially symmetric von Mises or Bingham orientation distribution function (ODF) around two preferred mean directions (Alastrué et al., 2009) and (Alastrué et al., 2010).

Several experimental studies have been conducted to determine and model the mechanical properties of human (Amabili et al., 2019; Choudhury et al., 2009; Haskett et al., 2010; Kamentskiy et al., 1998; Sokolis, 2015; deGeest et al., 2004; Weisbecker et al., 2012), porcine (Guo and Kassab, 2004; Kim and Baek, 2011; Lillie et al., 2010; Peña et al., 2015, 2018; Silver et al., 2003; Sokolis, 2007; Zeinali-Davarani et al., 2013), murine (Guo and Kassab, 2003) and ovine aortas (Haslach et al., 2011) by means of inflation, uniaxial and biaxial tests. To the best of the author’s knowledge the studies by Sassani et al. (2015a) and Weisbecker et al. (2012) are the only ones which analyze the layer-specific uniaxial mechanical properties of abdominal aorta. The elegant work by Sassani et al. (2015a) is the only work that presents the layer-specific mechanical properties and residual stresses simultaneously and analyzes the constitutive modeling for abdominal aorta. A number of candidate constitutive models were analyzed and compared for their efficacy in reproducing the material response of each layer. However they focused on abdominal aortic aneurysms. On the other hand, Weisbecker et al. (2012) conducted uniaxial tension tests on layer-separated human abdominal aortic tissue samples tested up to the supra-physiological loading range to analyze the damage of the tissue. However, in that paper there is no data about the mechanical response over a physiological range or residual strains.

The purpose of the current study was to quantify the axial pre-stretch and opening angle and performed uniaxial tests to study the mechanical behavior of both intact and layer-separated porcine infrarenal abdominal aorta under physiological loads and reported values of constitutive parameters for well-known strain energy functions. Finally, two structural models (Gasser et al., 2006; Baek et al., 2007) and one micro-structural model (Alastrué et al., 2009) were proposed to estimate the mechanical properties of the abdominal aorta by least-square fitting of the recorded in-vitro uniaxial test results.

## 55 2 Materials and methods

56 Seven abdominal porcine aortas were harvested from female pigs approximately  $3.5 \pm 0.45$   
57 months old. The experiments were approved by the Ethical Committee for Animal Research  
58 of the University of Zaragoza. The animals were sacrificed under general anesthesia through  
59 an intravenous injection of potassium chloride and sodium thiopental, and the infrarenal ab-  
60 dominal aorta (IAA) were harvested. Their *in situ* length was measured, then the specimens  
61 were dissected, and their *ex situ* length recorded. The axial stretch  $\lambda_z^0$ , defined as the ratio  
62 between the *in situ* and *ex situ* measured lengths, was then computed. After artery harvesting  
63 and cleaning, the IAA were kept frozen at  $-18^\circ\text{C}$  until testing.

### 64 2.1 Experiments

65 After being defrozen, the samples were preserved Krebs-Ringer solution at  $4\text{ }[^\circ\text{C}]$  until the  
66 preparation for testing was carried out. Two  $2\div 3\text{ [mm]}$  arterial rings and two  $5\times 25\text{ [mm]}$  longi-  
67 tudinal strips were cut. Following the protocol described in Peña et al. (2015), we locate suitable  
68 places where the layer separation process can be carried out. One ring and one longitudinal  
69 strip were carefully separated with minimal force with the aid of a microscope and using a  
70 scalpel, first separating the intima and then the media from the adventitia. Hematoxiline-eosine  
71 histological stains were prepared to confirm correct layer separation and that the separation  
72 did not induce damage. Samples with a faulty separation process were discarded. For intima,  
73 we used a threshold of 3 lamellas to exclude specimens with an incorrect intima-media layer  
74 separation. Three measurements at different locations were taken using a Mitutoyo Digimatic  
75 micrometer ( $202\text{ mm}^2$  of maximum contact area), which held the measurement when the con-  
76 tact force reached a value of  $0.5\text{ [N]}$ , to measure the length, width and thickness of the samples.  
77 The measurements were averaged.

78 Arterial ring segments (intact and layer-dissected) were arranged in Krebs-Ringer solution  
79 ( $25^\circ\text{C}$ ) in a Petri dish and then cut open by radial cuts. The OA was defined as the angle  
80 subtended by the lines connecting the midpoint of the inner circumference with the ends

of the ring. The opening angle and the stress free dimensions were measured using ImageJ software after 30 min to fully release the residual stress. The axial stretch with respect to the non-separated strips  $\lambda_z^*$  were also determined, so the total axial residual stretch for each layer could be computed as  $\lambda_z^{res} = \lambda_z^0 \lambda_z^*$  (Peña et al., 2015).

Simple tension tests of the circumferential and axial IAA rectangular strips (5x25 [mm]) were performed in a high precision drive Instron Microtester 5548 system using a 10 [N] load cell with a minimal resolution of 0.005 [N]. A non-contact Instron 2663-281 video-extensometer was used to measure the strain during the tests. To avoid specimen drying, we used an ultrasonic humidifier enabling humidity to be maintained during the test. Three loading and unloading stress cycle levels were applied: corresponding to approximately 60, 120 and 240 [kPa] uniaxial stress at 30%/min of strain rate (García et al., 2011) under load control. Five preliminary cycles at all load levels were applied in order to precondition the sample. The engineering stress (first Piola Kirchhoff stress tensor  $\mathbf{P}$ ) in the direction of the stretch was computed as  $P_{\theta\theta,zz} = \frac{F_{\theta,z}}{t_{\theta,z}w_{\theta,z}}$ , where  $F$  is the load registered by the Instron machine and  $t_{\theta,z}$  and  $w_{\theta,z}$  are the initial thickness and width in circumferential and longitudinal directions respectively.

It was considered helpful to measure the anisotropy of the samples at the estimated physiological stress state in the artery, approximated by a thin tube under a physiological pressure of 120 mmHg (using Laplace's law  $\sigma_{\theta\theta} = \frac{Pr}{t}$ ) that for IAA corresponds to 116 kPa. Anisotropy was analyzed by the difference in longitudinal and circumferential stretches divided by their average value (Kamenskiy et al., 1998).

## 2.2 Strain-energy functions

Only the elastic properties of the tissue were considered, so we take into account only the experimental tests at the second level (120 [kPa]) after preconditioning, i.e. the last curve obtained for that level (Peña et al., 2015).

### 105 2.2.1 Gasser-Ogden-Holzapfel model

106 The Gasser-Ogden-Holzapfel (GOH) model proposed by Gasser et al. (2006) as an extension  
 107 of the model of Holzapfel et al. (2000) by the application of a generalized structure tensor  
 108  $\mathbf{H} = \kappa \mathbf{1} + (1 - 3\kappa) \mathbf{M}_0$  (where  $\mathbf{1}$  is the identity tensor and  $\mathbf{M}_0 = \mathbf{m}_0 \otimes \mathbf{m}_0$  is a structure tensor  
 109 defined using unit vector  $\mathbf{m}_0$  specifying the mean orientation of fibers) is considered

$$\Psi = \mu (I_1 - 3) + \sum_{i=4,6} \left[ \frac{k_1}{2k_2} \left( \exp \{k_2 \hat{E}_i\} - 1 \right) \right], \quad (1)$$

110 where  $I_1 = \text{tr} \bar{\mathbf{C}}$  represents the first invariant of the Cauchy-Green tensor ( $\mathbf{C} = \mathbf{F}^T \mathbf{F}$ ) char-  
 111 acterizing the isotropic mechanical response of the elastin (Gundiah et al., 2009; Lillie et al.,  
 112 2010),  $\mathbf{F}$  is the deformation gradient (Spencer, 1971) and

$$\hat{E}_i = \kappa I_1 + (1 - 3\kappa) I_i - 1 \quad i = 4, 6 \quad (2)$$

113 where

$$I_4 = \lambda_\theta^2 \cos^2(\theta) + \lambda_z^2 \sin^2(\theta), \quad I_6 = \lambda_\theta^2 \cos^2(-\theta) + \lambda_z^2 \sin^2(-\theta). \quad (3)$$

114 In this equation  $I_1$  represents the first invariant of the Cauchy-Green tensor (Spencer, 1971)  
 115 characterizing the isotropic mechanical response of the elastin (Gundiah et al., 2009; Lillie  
 116 et al., 2010),  $\mu > 0$ ,  $k_1 > 0$  are stress-like parameters,  $k_2 > 0$  and  $\kappa$  are dimensionless. Here,  
 117  $\theta$  is the orientation angle relative to the circumferential direction.  $\kappa \in [0, 1/3]$  is a dispersion  
 118 parameter (the same for each collagen fiber family). When  $\kappa = 0$ , the model is the same as the  
 119 one published in Holzapfel et al. (2000), and when  $\kappa = 1/3$  it recovers an isotropic potential  
 120 similar to that used in Demiray (1972).

### 121 2.2.2 Four-Fiber-Family model

122 The second constitutive model, called Four Fiber Family (FFF), is a hyperelastic anisotropic  
 123 model proposed by Baek et al. (2007). The model is used for stress-strain description of human  
 124 aortas and aneurysms (Ferruzzi et al., 2011; Sassani et al., 2015b). The model represents an  
 125 elastin-dominated amorphous matrix reinforced by four families of (collagen) fibers (in axial,  
 126 circumferential and diagonal directions).

$$\Psi = \frac{c}{2} (I_1 - 3) + \sum_{i=1}^4 \frac{c_1^i}{4c_2^i} \left[ \exp \left( c_2^i [I_4^i - 1]^2 \right) - 1 \right], \quad (4)$$

127 In this equation  $c > 0$ ,  $c_1^i > 0$  are stress-like parameters,  $c_2^i > 0$ .  $I_4^i = \mathbf{M}_0^i \cdot \mathbf{M}_0^i \mathbf{C}$  represents  
 128 the square of the stretch of the  $i^{th}$ -fiber family. The fiber orientations are defined by the unit  
 129 vectors  $\mathbf{M}_0^i$ , which depend on angles  $\theta_0^i$  defined between directions of fiber reinforcement and  
 130 the circumferential direction. Hence, circumferential and axial fibres are fixed at  $\theta_0^1 = 0$  and  
 131  $\theta_0^2 = 90$ , respectively, while the diagonal fibers are accounted for by  $\theta_0^3 = -\theta_0^4 = \theta_0$ .

### 132 2.2.3 Microfiber model

133 Following Alastru   et al. (2010), we consider a microfiber model (microsphere-based model) to  
 134 account for the dispersion of the collagen fibers around a preferential direction. Consistent with  
 135 the constrained mixture approach (Humphrey and Rajagopal, 2003), the free energy function  
 136 takes the form  $\Psi = \mu (I_1 - 3) + \Psi_{\text{coll}}$ , where the subscripts *coll* refers to the collagen fibers  
 137 contribution.  $\Psi_{\text{coll}}$  is defined as the sum of the contributions of each collagen family of fibrils  
 138 as

$$\Psi_{\text{coll}} = \sum_{j=1}^N [\Psi_{\text{coll}}]^j = \sum_{j=1}^N \langle n \rho \psi_{\text{coll}} \rangle^j = \sum_{j=1}^N \frac{1}{4\pi} \int_{\mathbb{U}^2} (n \rho [\psi_{\text{coll}}])^j dA, \quad (5)$$

where  $N$  denotes the number of families of collagen fibers,  $N = 2$  according to the experimental results of orientation of the collagen fibers (Holzapfel et al., 2000), and applying a discretization to the continuous orientation distribution on the unit sphere  $\mathbb{U}^2$ ,  $[\Psi_{\text{coll}}]^j$  corresponds to the expression

$$[\Psi_{\text{coll}}]^j = \sum_{i=1}^m n \rho(\mathbf{r}^i; (\lambda_{\text{coll}}^i)) \quad (6)$$

where  $\mathbf{r}^i$  are the unit vectors associated with the discretization on the microsphere over the unit sphere  $\mathbb{U}^2$  and  $m$  is the number of discrete orientation vectors (Alastrué et al., 2009).  $\lambda_{\text{coll}}^i = \|\mathbf{F} \cdot \mathbf{r}^i\|$  the stretch in  $\mathbf{r}^i$  direction and  $\psi_{\text{coll}}^i(\lambda_{\text{coll}}^i)$  the strain energy function associated with  $\mathbf{r}^i$  direction.  $\rho$  is the orientation density function (ODF) to take into account the fibrils dispersion (Alastrué et al., 2009). A 3D bi- $\pi$ -periodic von Mises ODF were considered to the modeling of the IAA (Alastrué et al., 2010). This function is expressed as

$$\rho(\theta) = \rho_1(\theta) + \rho_2(\theta), \quad (7)$$

where  $\theta = \arccos(\mathbf{m} \cdot \mathbf{r})$  is the so-called mismatch angle and  $\mathbf{m}$  the preferred mean orientation of the collagen distribution, and

$$\rho_i(\theta) = 4 \sqrt{\frac{b}{2\pi}} \frac{\exp(b [\cos(2\theta) + 1])}{\text{erfi}(\sqrt{2b})}, \quad (8)$$

where the positive concentration parameter  $b$  constitutes a measure of the degree of anisotropy. Moreover,  $\text{erfi}(x) = -i \text{erf}(ix)$  denotes the imaginary error function.

Considering the affine kinematics to define the collagen fiber stretch  $\lambda_{\text{coll}}^i = \|\mathbf{t}^i\|$  in the fiber direction  $\mathbf{r}^i$ , the exponential-like strain energy function proposed by Holzapfel et al. (2000)



155 was used to deal with the fiber response

$$n\psi_{\text{coll}}^i(\lambda_{\text{coll}}^i) = \frac{c_{1\text{coll}}}{2c_{2\text{coll}}}(e^{c_{2\text{coll}}((\lambda_{\text{coll}}^i)^2-1)^2} - 1) \quad \text{if} \quad \lambda_i \geq 1 \quad \text{otherwise} \quad \psi_{fi}(\lambda_i) = 0, \quad (9)$$

156 since it is usually considered that collagen fibers only affect global mechanical behavior in  
 157 tensile states (Holzapfel et al., 2000). Finally,  $c_{1\text{coll}}$  and  $c_{2\text{coll}}$  are stress dimensional and dimen-  
 158 sionless material parameters respectively.

### 159 2.3 Data fitting

160 The fitting of the experimental data was developed by using a Nelder and Mead type  
 161 minimization algorithm (Nelder and Mead, 1965) defining the objective function  $\chi^2 =$   
 162  $\sum_{i=1}^n \left[ (P_{\theta\theta} - P_{\theta\theta}^{\Psi})^2 + (P_{zz} - P_{zz}^{\Psi})^2 \right]$  using HyperFit software ([www.hyperfit.wz.cz](http://www.hyperfit.wz.cz)). The tissue  
 163 was assumed as incompressible (Carew et al., 1968), i.e.  $\det(\mathbf{F}) = \lambda_1\lambda_2\lambda_3 = 1$ , where  $\mathbf{F}$   
 164 represents the deformation gradient tensor and  $\lambda_i$ ,  $i = 1, 2, 3$ , the stretches in the principal  
 165 directions.  $P_{\theta\theta}$  and  $P_{zz}$  are the First Piola-Kirchhoff (engineering) stress data obtained from  
 166 the tests, and  $P_{\theta\theta}^{\Psi} = \frac{\partial \Psi_{\text{iso}}}{\partial \lambda_{\theta}}$  and  $P_{zz}^{\Psi} = \frac{\partial \Psi_{\text{iso}}}{\partial \lambda_z}$  are the First Piola-Kirchhoff (engineering) for the  
 167  $i$ th point for a homogeneous pure uniaxial state  $\Psi$ , and  $n$  is the number of data points. The  
 168 coefficient of determination  $R^2 \in [0, 1]$  was computed for each fitting where  $R^2 \geq 0.85$  typically  
 169 represents a good fit to the experimental data. Finally, the normalized mean square root error  
 170  $\varepsilon \in [0, 1]$ ,  $\varepsilon = \frac{\sqrt{\frac{\chi^2}{n-q}}}{\varpi}$ , were computed for each fitting. In this equation,  $\varpi = \frac{\sum_{i=1}^n (\sigma)_i}{n}$  is the  
 171 mean value of the measured stresses,  $q$  is the number of parameters of the SEF, so  $n - q$  is the  
 172 number of degrees of freedom, and  $\mu$  the mean stress already defined above.  $\varepsilon \leq 0.15$  typically  
 173 represents a good fit to the experimental data.

## 174 2.4 Statistics

175 The Shapiro-Wilk Test was used to test for normal distribution . Welch's t test, with the  
176 two-sided significance level of  $p < 0.05$ , was used to test the difference between groups.

## 177 3 Results

178 In 4 layer samples, the layer separation process was not successful, the failure point was reached  
179 before the 120 kPa cycle due to damage of the samples or slippage of the tissue was presented.  
180 In those cases, a new sample was dissected to have at least one sample in circumferential and  
181 longitudinal directions for each layer per animal.

### 182 3.1 Experiments

183 The thickness of the total wall for all samples of the IAA was:  $1.06 \pm 0.10$  [mm] while the  
184 thickness of the individual layers was  $0.13 \pm 0.02$  [mm] for the intima,  $0.53 \pm 0.13$  [mm] for  
185 the media, and  $0.51 \pm 0.12$  [mm] for the adventitia, see Figure 1.a. The inner diameter of the  
186 IAA was  $6.52 \pm 1.530$  [mm] and for each arterial layer, –intima, media, and adventitia–, it was  
187  $7.37 \pm 0.33$  [mm],  $7.75 \pm 0.52$  [mm] and  $8.58 \pm 0.56$  [mm], respectively for all the specimens, see  
188 Figure 1.b. The ratio of total wall thickness to inner diameter of all the IAA specimens was  
189  $0.18 \pm 0.02$  and for the intima, media, and adventitia the ratio was  $0.02 \pm 0.004$ ,  $0.07 \pm 0.02$ , and  
190  $0.06 \pm 0.02$ , respectively, see Figure 1.c. Finally, the ratio of layer-thickness to total wall thick-  
191 ness was  $0.11 \pm 0.02$  for the intima, for the media  $0.38 \pm 0.09$ , and  $0.43 \pm 0.24$  for the adventitia,  
192 see Figure 1.d.

193 [Fig. 1 about here.]

194 Figure 2.a shows column plots of the opening angle values after 30 min of equilibration in the  
195 Krebs-Ringer solution for the IAA corresponding to the rings for the whole artery and the

196 dissected layers. The OA value for the intact layer was  $70.61^{\circ} \pm 17.11$ . For the separated layers  
 197 the values were  $138.87^{\circ} \pm 27.31$  for the intima,  $40.01 \pm 20.58$  for the media, and  $91.34^{\circ} \pm 12.34$   
 198 for the adventitia. The axial *in situ* stretch ( $\lambda_z^0$ ) was  $1.60 \pm 0.06$ . The column plots in Figure 2.b  
 199 represent the total pre-stretches (mean values and associated standard deviations) of the IAA  
 200 axial strips after separation into their three layers. Figure 2.b indicates that the media seems to  
 201 be slightly stretched in the environment of the intact arterial strip. The total pre-stretch values  
 202 ( $\lambda_z^{es}$  for the intima, media and adventitia were  $1.49 \pm 0.08$ ,  $1.66 \pm 0.07$  and  $1.59 \pm 0.10$ , respec-  
 203 tively. We note that the intima is the shortest of the three layers after separation, indicating  
 204 that the intima is under compression in the unloaded state.

205 [Fig. 2 about here.]

206 Figure 3 shows the mechanical responses of the intact arterial tissue in the circumferential and  
 207 longitudinal directions. All samples exhibit a pronounced nonlinear mechanical response in  
 208 both directions with a soft transition from the low stiffness region to the high stiffness portion  
 209 of the curve. Specimens are stiffer in the circumferential direction than in the longitudinal  
 210 direction showing remarkable anisotropy.

211 [Fig. 3 about here.]

212 Representative mechanical responses of dissected intima, media and adventitia layers obtained  
 213 from the IAA are shown in Figure 6. Different mechanical behaviors between circumferential  
 214 and longitudinal directions are clearly depicted for all the layers, see also Table 1. The cir-  
 215 cumferential curves are stiffer and present, in general, a lower dispersion than the longitudinal  
 216 ones. The adventitia and intima samples present a tendency to be stiffer than the correspond-  
 217 ing media samples in the longitudinal direction, see Table 1, where stretches at 60 kPa and 120  
 218 kPa for all the layers are summarized. The intima samples show quasi-isotropic behavior and  
 219 the lowest pronounced nonlinearity (Figure 6 and Table 1). Welch's t test reveals significant  
 220 differences ( $p < 0.01$ ) in the anisotropy between whole arteries and dissected layers.

221 [Fig. 4 about here.]

222 [Table 1 about here.]

### 223 3.2 *Histology*

224 Transverse histological cuts of the specimens stained with Hematoxiline-eosine are shown in  
225 Figure 5. Anatomic separation of the arterial sample into its three layers were checked. For  
226 most specimens only a few laminae of the media are still attached to the intima or adventitia.

227 [Fig. 5 about here.]

### 228 3.3 *Data fitting*

229 Material parameters for the intact arteries and their related intima, media and adventitia  
230 samples are summarized in the Tables 2, 3 and 4. The values obtained of  $\varepsilon$  are very low for all the  
231 fitted data clearly demonstrating the goodness of the fitting. All SEFs performed adequately  
232 ( $\varepsilon < 0.15$ ) with whole data, but only the four family model afforded proper simulation of  
233 the mechanical response for the intima, media and adventitia ( $\varepsilon = 0.0468 \pm 0.0165$ ,  $\varepsilon =$   
234  $0.0502 \pm 0.0350$  and  $\varepsilon = 0.0494 \pm 0.0173$ , respectively). Less accurate but altogether good  
235 simulations were obtained with the GOH and microfiber models.

236 The GOH dispersion parameter  $\kappa$  was  $0.1392 \pm 0.0710$  for whole artery,  $0.2753 \pm 0.0245$  for the  
237 intima layer,  $0.1175 \pm 0.0776$  for the media and  $0.2529 \pm 0.0678$  for the adventitia, showing high  
238 dispersion or a more isotropic response for the intima and adventitia. Equivalent results were  
239 obtained by the microfiber model where the dispersion parameter  $b$  had values of  $9.4754 \pm 3.0455$   
240 for the whole artery,  $2.1143 \pm 1.2463$  for the intima layer,  $3.4245 \pm 3.3857$  for the media and  
241  $3.1142 \pm 2.8994$  for the adventitia. There is no equivalent dispersion parameter for the four  
242 family model.

243 [Table 2 about here.]

244 [Table 3 about here.]

245 [Table 4 about here.]

## 4 Discussion

In this paper, we analyze the layer-separated residual stresses and mechanical properties of the infrarenal abdominal aorta (IAA). We measured the axial pre-stretch and opening angle and performed uniaxial tests to study and compare the mechanical behavior of both intact and layer-separated porcine IAA samples under physiological loads.

Regarding the geometry and *in situ* pre-stretch, we found that the opening angles for the whole artery and media layer are smaller than for the intima and adventitia layers. In all cases, we found the OA in the media layer is lower than in the whole artery, the intima and the adventitia. These results are comparable with those reported by Stergiopoulos et al. (2001) for carotid or Holzapfel et al. (2007) for human aorta where the residual stress on intima and adventitia is "compensated" by the media as a composite. However, Sokolis (2019) obtained a contrary tendency to that obtained in our work; the adventitia and the media-intima layers showed OAs higher than the intact artery for porcine IAA. These differences can be explained by the fact that the experiments of Sokolis (2019) dissected the aorta in two layers: intima-media and adventitia. For the axial pre-stretch, we found that the adventitia and the media were slightly stretched in the environment of the intact arterial strip for each orientation, whereas the intima seems to be compressed. Only the works of Sokolis (2019) provide data for the porcine dissected layer abdominal aorta. They found the intima-media layer compressed and the adventitia stretched. Sokolis et al. (2017) obtained an OA for human abdominal artery between  $60^\circ$  and  $160^\circ$  for young patients (age less than 40 years), as well as diameters around 7 and 7.5 mm and 200 to  $250^\circ$  OA and 8.3 and 8.7 mm diameter for older patients. Our results for porcine abdominal artery without pathologies are similar to those of young human patients although slightly smaller between  $60^\circ$  and  $90^\circ$  of OA and between 6.5 and 8 mm of diameter. There was no data about the axial *in situ* stretch. Again, the lack of separation between the intima and media layers hinder a comparison with our data. Holzapfel et al. (2007) obtained for human aorta a similar tendency to that presented herein. However, they found axial *in*

273 *situ* stretches for human abdominal aorta of 1.196 which is lower than that obtained by (Hang  
274 and Fung, 1995) and that obtained in our work (1.6) for young pigs. This is due to the fact  
275 that the axial pre-stretch strongly depends on the age, and the human data of Holzapfel et al.  
276 (2007) was obtained for aged patients.

277 The uniaxial test data show that the media seems to be the softest layer over the whole defor-  
278 mation domain, and that the intima and adventitia exhibit considerable stiffness, particularly  
279 in the high loading domain in the longitudinal direction. However, there are no differences in  
280 the mechanical response of the whole artery and each layer for the circumferential directions.  
281 On basis of these results, a single-layer approach for characterizing the mechanical response  
282 of thoracic aorta would be inappropriate. The whole artery and media samples show the most  
283 pronounced anisotropy presenting a higher anisotropic index than the intima and adventi-  
284 tia. The apparent lower anisotropy for the intima, may be caused by the organization of the  
285 collagen fibers as pointed out by Polzer et al. (2015). Regarding the layer specific mechan-  
286 ical properties, Holzapfel et al. (2005) found similar results for the human coronary artery.  
287 However, they found that the intima and adventitia of coronaries show the most pronounced  
288 nonlinearity and isotropy similarly to our IAA data. Finally, Amabili et al. (2019) is the only  
289 work that present simultaneously the layer-specific mechanical properties and residual stresses  
290 for the human thoracic descending aorta. They reported that the intima layer is generally the  
291 stiffest, with insignificant differences in behavior for the axial and circumferential.

292 In this work, we study a series of constitutive models, some with a phenomenological approach  
293 and others which are micro-structural and physically-oriented, describing the features of the  
294 arterial wall with greater accuracy. The fitted GOH, four-family and microfiber hyperelastic  
295 models are presented in Tables 2, 3 and 4, respectively. The stress-stretch curves obtained  
296 were fitted with the hyperelastic anisotropic models providing a reasonable approximation to  
297 the experimental data. The GOH model (Holzapfel et al., 2000) and the microfiber model  
298 (Alastrué et al., 2010) were not able to capture the uniaxial properties of the intact and  
299 media layer of IAA over a lower range of uniaxial deformations, showing the best prediction  
300 at high stretches. The RMSE of the GOH model and the micro-structured model with the von  
301 Mises ODF function were similar for all positions. The errors of the fitting procedure might be

302 explained by the coupling effect (overparameterization) of the constitutive model, and different  
303 combinations of material parameters may have similar stress-strain response. This nonlinear  
304 coupling has resulted in identification difficulties in the optimization-based fitting approaches.  
305 The lowest values of RMSE were obtained for the four family of fibers for the whole artery  
306 and each separated layer. This is due to the fact that in the four-family fibers model, where  
307 the number of fiber families increases from 2 to 4, there is significant improvement in the  
308 goodness-of-fit between the model predictions and experimental results. However, if we want  
309 to use the histological (microstructural) data obtained, we cannot correlate the measurements  
310 with the four-fiber family model.

311 The findings of this study should be interpreted within the context of its limitations. Regarding  
312 the experimental analysis, a small number of tissue samples ( $n=7$ ) were investigated. Another  
313 relevant limitation relates to the use of uniaxial tension tests for separated layers instead of  
314 biaxial tests. As pointed out by Holzapfel et al. (2005), an anatomic separation of arteries into  
315 their tissue components in young samples is difficult, even impossible for square samples such  
316 as we needed for the biaxial tests. Also, dog-bone samples were not possible to obtain and  
317 rectangular samples with a 5:1 length-width ratio were used in the uniaxial tests. The aortas  
318 were kept frozen at  $-20^{\circ}\text{C}$  until testing. No significant difference was found between the elastic  
319 modulus of porcine aortic tissue before and after freezing at  $-20^{\circ}\text{C}$  and it was unaffected by the  
320 storage time (O’Leary et al., 2014). With regard to the material fitting, only data in the range  
321 used to fit the model is theoretically predictable (until 120 kPa). The orientation of collagen  
322 fibers was not included by a probability density function and the dispersion parameters  $\kappa$  and  
323  $b$  and the mean fiber orientation angle are estimated during the fitting procedure, so it should  
324 be analyzed as phenomenological parameter.

325 The results obtained correspond to young samples without pathologies whose results are equiv-  
326 alent to those obtained by Sokolis et al. (2017) for human abdominal aorta from young patients.  
327 Obtaining human samples from young patients without pathology is difficult. Therefore, data  
328 on the behavior of the aorta before the onset of pathologies can help to understand how and  
329 why, for example, aneurysms, aortic dissection or atheromatous plaques might develop.

## 330 5 Conclusions

331 There are three main findings from this study: first, the residual stresses are layer dependent.  
332 The intima circumferentially opened by  $138^\circ$  on average, becoming quasi-flat, whereas the  
333 media opened similarly to the intact wall. In all cases, we found that the OA in the media  
334 layer is lower than in the whole artery, intima and adventitia. For the axial pre-stretch, we  
335 found that the adventitia and the media were slightly stretched in the environment of the  
336 intact arterial strip for each orientation, whereas the intima seems to be compressed. Second,  
337 the media seems to be the softest layer over the whole deformation domain showing high  
338 anisotropy. The intima and adventitia exhibit considerable stiffness and a lower anisotropy  
339 response. Finally, all the hyperelastic anisotropic models considered in this study provided  
340 a reasonable approximation of the experimental data, the four-fiber model showing the best  
341 fitting.

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## 351 7 Conflict of interest

352 None.



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	$\lambda_{\theta}^{120}$	$\lambda_z^{120}$	$A^{120}$	$\lambda_{\theta}^{60}$	$\lambda_z^{60}$	$A^{60}$
Whole artery	1.19±0.04	1.36±0.08	0.16±0.03	1.14±0.04	1.33±0.05	0.16±0.026
Intima	1.17±0.07	1.27±0.04	0.09±0.05	1.12±0.04	1.24±0.03	0.10±0.03
Media	1.16±0.04	1.47±0.08	0.24±0.05	1.12±0.04	1.37±0.05	0.19±0.04
Adventitia	1.18±0.06	1.37±0.08	0.15±0.02	1.14±0.04	1.31±0.06	0.14±0.03

Table 1

Circumferential and longitudinal stretches and anisotropy measurements corresponding to 60 kPa and 120 kPa during uniaxial tests. Values are presented as Average±Standard Deviation

Specimen	$\mu$	$k_1$	$k_2$	$\theta$	$\kappa$	$R^2$	$\varepsilon$
Whole artery							
<i>I</i>	12.6365	458.7309	673.4996	28.83	0.2752	0.9928	0.0479
<i>II</i>	20.9022	982.9519	708.2242	37.46	0.1379	0.9972	0.03062
<i>III</i>	16.7504	134.7933	70.1169	38.52	0.1264	0.9984	0.02318
<i>IV</i>	10.9810	401.0243	43.1162	39.15	0.0566	0.9992	0.0164
<i>V</i>	29.3678	5.8513	300.6832	34.19	0.2136	0.9844	0.0725
<i>VI</i>	17.9142	349.8984	227.4454	36.73	0.1518	0.9977	0.0257
<i>VII</i>	18.8423	403.6538	0.1615	39.69	0.1152	0.9951	0.0395
<i>Mean</i>	17.3934	213.3840	76.9163	36.1818	0.1392	0.9950	0.0328
<i>SD</i>	6.0233	308.4709	294.1968	3.7924	0.0710	0.0051	0.0190
<i>Mean curve</i>	11.8467	1578.1744	33.1316	39.78	0.0636	0.9926	0.0501
Intima							
<i>I</i>	5.1226	853.8510	211.3070	37.21	0.2484	0.9979	0.0392
<i>II</i>	27.0706	7302.9946	6.9407	6.58	0.3083	0.9877	0.0568
<i>III</i>	11.6378	1525.2551	0.0019	37.07	0.2866	0.9868	0.1033
<i>IV</i>	13.6154	1008.4663	22.0936	37.63	0.2765	0.9671	0.1053
<i>V</i>	8.2341	1217.5817	2.98	15.96	0.2910	0.9398	0.1381
<i>VI</i>	13.0162	22.4826	1176.3743	31.85	0.2386	0.9979	0.0261
<i>VII</i>	0.0105	6449.9160	9.8333	26.41	0.2843	0.9754	0.1196
<i>Mean</i>	4.2423	1078.1611	8.0136	15.0681	0.2753	0.9788	0.0724
<i>SD</i>	8.4865	2950.3424	435.3566	15.4724	0.0245	0.0206	0.0430
<i>Mean curve</i>	6.9257	2846.3490	15.4171	7.33	0.1281	0.9849	0.0653
Media							
<i>I</i>	21.8548	762.9170	7.6170	10.31	0.1175	0.9959	0.0372
<i>II</i>	19.7914	1760.7891	1.2631	36.66	0.0700	0.9927	0.0453
<i>III</i>	17.9965	82.2915	57.7442	38.39	0.0732	0.9881	0.0636
<i>IV</i>	8.5614	331.6519	23.0200	38.44	0.0634	0.9868	0.1421
<i>V</i>	33.3931	34.2622	257.6528	5.87	0.2666	0.98024	0.0791
<i>VI</i>	11.1638	828.1872	10.4041	25.70	0.2072	0.9850	0.1398
<i>VII</i>	7.1638	1289.8882	10.4207	10.96	0.1465	0.9884	0.0610
<i>Mean</i>	15.0877	388.7532	16.6668	12.71	0.1175	0.9882	0.0722
<i>SD</i>	9.1559	638.8697	92.3459	16.4324	0.0776	0.0051	0.0430
<i>Mean curve</i>	26.8563	326.4881	144.4521	16.04	0.1091	0.9911	0.0539
Adventitia							
<i>I</i>	13.7889	877.5483	876.1438	5.04	0.3037	0.9960	0.0363
<i>II</i>	12.5737	5811.7885	17.4556	36.83	0.1144	0.9930	0.0485
<i>III</i>	26.06651	690.6917	41.9081	4.1411	0.2952	0.9946	0.0408
<i>IV</i>	28.1246	597.0324	0.9927	5.84	0.3010	0.9938	0.0443
<i>V</i>	20.0771	166.5962	98.4039	7.95	0.2984	0.9763	0.0880
<i>VI</i>	1.9299	703.9918	74.4546	20.55	0.2751	0.9473	0.1305
<i>VII</i>	8.8685	1758.2219	167.7915	9.54	0.2614	0.984881	0.0673
<i>Mean</i>	12.3442	887.4973	50.0084	9.5026	0.2529	0.9836	0.0589
<i>SD</i>	9.4019	1954.7365	310.9273	11.9393	0.0678	0.0175	0.0340
<i>Mean curve</i>	7.9832	1297.9849	35.7531	11.53	0.3004	0.9932	0.0477

Table 2

Material constants of GOH model (Gasser et al., 2006) obtained for the IAA curves. Constants  $\mu$  and  $k_1$  in kPa,  $\theta$  in degrees,  $k_2$ ,  $\kappa$  and  $\varepsilon$  dimensionless.



Specimen	$c$	$c_1^1$	$c_2^1$	$c_1^2$	$c_2^2$	$c_1^{3,4}$	$c_2^{3,4}$	$\theta_0$	$R^2$	$\varepsilon$
Whole artery										
<i>I</i>	34.7544	0.4398	11.6530	32.2330	24.6783	0.0506	7.6554	6.99	0.9933	0.0469
<i>II</i>	66.2017	0.6106	9.3837	126.9770	25.9115	0.0395	0.001	1.28	0.9954	0.0362
<i>III</i>	42.7063	2.3646	2.6128	40.4117	0.7826	1.8748	14.7557	12.20	0.9928	0.0490
<i>IV</i>	31.0096	4.4856	1.9824	41.9580	5.9160	1.9446	7.9652	5.72	0.9965	0.03268
<i>V</i>	33.3510	7.2875	1.7555	0.4914	1.5480	2.6395	15.3836	8.93	0.9950	0.0388
<i>VI</i>	43.1379	3.2313	3.6625	40.3492	17.5084	1.6489	21.6301	5.21	0.9981	0.0242
<i>VII</i>	40.2375	6.7574	7.3470	89.6690	27.2213	0.9401	0.1710	12.05	0.9984	0.0228
<i>Mean</i>	40.4239	2.3959	4.2903	27.6445	8.0466	0.6054	1.7546	6.1947	0.9956	0.0345
<i>SD</i>	11.8163	2.7367	3.9678	41.7251	11.7877	0.9951	8.0853	3.9200	0.0022	0.0102
<i>Mean curve</i>	39.6333	4.1275	3.6540	34.1404	13.5602	1.7503	19.8894	8.02	0.9978	0.0265
Intima										
<i>I</i>	27.3095	6.5057	6.8864	43.0056	12.4125	1.2055	14.8318	8.93	0.9968	0.0328
<i>II</i>	79.2891	12.3243	10.6707	177.7176	28.44958	0.0124	9.9304	0	0.9881	0.0554
<i>III</i>	39.4479	10.6809	6.3330	95.4495	1.1390	1.6924	9.1107	6.41	0.9978	0.0267
<i>IV</i>	47.8856	7.2929	5.4621	55.1281	2.6780	1.6846	8.3388	10.82	0.9940	0.0441
<i>V</i>	39.6084	4.2185	6.2471	79.9296	1.9043	1.3278	10.4852	11.17	0.9858	0.0691
<i>VI</i>	39.8955	7.3424	4.7460	113.7596	20.5791	0.0038	11.2351	2.34	0.9931	0.0483
<i>VII</i>	45.8204	4.7734	13.9839	196.2964	29.0005	0.1271	1.2142	5.78	0.9808	0.0690
<i>Mean</i>	43.5301	7.1154	7.2510	95.3740	7.4078	0.2229	7.6970	1.9125	0.9909	0.0468
<i>SD</i>	16.2330	2.9607	3.3332	58.6674	12.3762	0.7852	4.1329	4.2120	0.0062	0.0165
<i>Mean curve</i>	40.7983	6.7224	7.4419	115.8015	5.7599	0.0246	3.0275	14.32	0.9982	0.0245
Media										
<i>I</i>	66.2919	2.9928	2.6876	87.3955	9.3524	0.0012	80.7890	8.25	0.9601	0.1164
<i>II</i>	49.6283	6.1010	2.2243	164.3806	10.9468	0.8753	12.5586	4.12	0.9881	0.0620
<i>III</i>	21.783466	12.0235	0.9418	58.31692	1.5201	1.1960	22.4120	20.79	0.9947	0.0393
<i>IV</i>	32.4433	9.9442	0.86423	9.1471	0.1198	5.6519	12.2345	6.81	0.9964	0.0334
<i>V</i>	58.8459	1.8615	1.3428	0.001	0.001	0.3691	47.8567	17.88	0.9718	0.0931
<i>VI</i>	0.1131	28.2814	0.2878	176.4606	14.4930	2.7854	4.6957	15.41	0.9991	0.0161
<i>VII</i>	41.65416	4.3507	4.2678	115.0859	9.3625	1.4912	7.8380	6.47	0.9902	0.0567
<i>Mean</i>	18.1329	6.5184	1.3465	14.8012	1.1418	0.5243	17.4365	9.7834	0.9857	0.0502
<i>SD</i>	22.7654	9.1099	1.3642	69.7998	5.8839	1.9321	27.8103	6.5133	0.0144	0.0350
<i>Mean curve</i>	36.2677	9.29595	1.1888	56.2004	10.8995	2.1084	0.6052	14.78	0.9969	0.0320
Adventitia										
<i>I</i>	41.7246	0.8141	11.4910	27.7764	23.6147	1.7719	49.8519	3.95	0.9985	0.02191
<i>II</i>	49.3751	0.8230	11.5591	28.9208	30.7391	1.8411	55.2051	6.35	0.9925	0.0438
<i>III</i>	57.5362	4.4357	2.4567	87.7237	1.2325	1.6370	17.4169	13.90	0.9842	0.0601
<i>IV</i>	77.7697	1.0317	0.5027	44.2300	2.1136	2.5457	49.0579	44.06	0.9816	0.0742
<i>V</i>	36.7046	1.1449	2.9021	35.9578	0.001	2.4020	29.4106	29.79	0.9943	0.0439
<i>VI</i>	19.3277	0.35499	4.87739	71.8832	6.57867	11.40906	0.2442	23.20	0.98759	0.0638
<i>VII</i>	54.1546	0.0761	15.5743	60.8469	23.4894	2.0797	2.28349	30.19	0.9893	0.0595
<i>Mean</i>	44.6564	0.7143	4.4790	46.7793	2.2503	2.5867	12.1267	16.4105	0.9897	0.0494
<i>SD</i>	18.2846	1.4582	5.7534	23.0239	12.9298	3.5544	23.0897	14.4409	0.0059	0.0173
<i>Mean curve</i>	16.5409	15.5141	2.2653	22.3355	2.6090	43.3966	6.4583	11.45	0.9971	0.0293

Table 3

Material constants of the FFF model (Baek et al., 2007) obtained for the IAA curves. Constants  $c$  and  $c_1^i$  in kPa,  $\alpha_0$  in degrees,  $c_2^i$  and  $\varepsilon$  dimensionless.

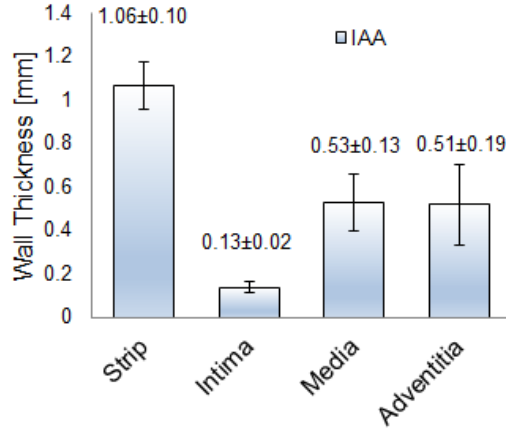
Specimen	$\mu$	$k_1$	$k_2$	$\theta$	$b$	$R^2$	$\varepsilon$
Whole artery							
<i>I</i>	54.9964	11.4754	31.8141	17.60	7.6169	0.9689	0.0981
<i>II</i>	55.0442	149.0229	20.5088	28.95	10.0469	0.9804	0.0761
<i>III</i>	40.5664	45.738	10.1622	35.09	15.5046	0.9818	0.0776
<i>IV</i>	40.3181	42.8590	8.5568	31.39	10.9163	0.98614	0.0680
<i>V</i>	63.8841	6.2323	10.6527	18.33	6.4819	0.9709	0.1652
<i>VI</i>	57.5288	61.5486	21.8151	30.93	7.558	0.9918	0.0970
<i>VII</i>	64.0294	93.9274	30.8552	30.79	10.8074	0.9932	0.0998
<i>Mean</i>	52.9380	38.2951	16.9791	26.7484	9.4754	0.9818	0.0936
<i>SD</i>	9.8327	49.6811	9.7598	6.8250	3.0455	0.0095	0.0324
<i>Mean curve</i> 54.3857	32.7026	11.4646	22.91	5.9280	0.9613	0.1122	
Intima							
<i>I</i>	55.0961	17.1556	18.2956	20.77	3.8044	0.9956	0.0627
<i>II</i>	49.7575	201.0553	12.5575	5.75	1.7426	0.9916	0.0895
<i>III</i>	59.6252	42.2675	7.3476	4.53	0.7741	0.9920	0.1130
<i>IV</i>	36.4593	58.8701	4.8751	24.63	1.1116	0.9791	0.0839
<i>V</i>	12.5659	89.2209	4.2606	35.95	2.8082	0.9518	0.1115
<i>VI</i>	69.0247	66.9910	12.3834	6.83	3.8044	0.9914	0.0926
<i>VII</i>	30.1694	117.7335	24.0989	18.59	3.0994	0.9971	0.0654
<i>Mean</i>	39.7189	66.9666	10.0650	12.9422	2.1143	0.9854	0.0864
<i>SD</i>	19.4068	60.5444	7.2890	11.6834	1.2463	0.0160	0.0199
<i>Mean curve</i>	19.6922	97.2772	7.3289	11.45	1.4101	0.9984	0.0231
Media							
<i>I</i>	1.5901	179.8450	1.2064	8.76	1.4333	0.9936	0.0322
<i>II</i>	1.091	219.0568	1.2825	24.26	2.5102	0.9581	0.0958
<i>III</i>	2.4181	76.8744	1.2900	9.59	1.3415	0.9342	0.1196
<i>IV</i>	72.1454	1.8812	15.2560	10.08	5.1965	0.9211	0.1563
<i>V</i>	25.4308	503.0956	2.0039	28.15	6.7839	0.9750	0.1595
<i>VI</i>	25.2593	313.0571	2.9081	26.43	3.0510	0.9856	0.0609
<i>VII</i>	1.3220	598.1179	3.8508	37.01	10.6384	0.9963	0.0352
<i>Mean</i>	5.9272	127.1298	2.5407	17.7978	3.4245	0.9659	0.0793
<i>SD</i>	26.1861	217.4690	5.0732	11.1486	3.3857	0.0295	0.0535
<i>Mean curve</i>	1.6386	463.7468	1.0060	27.34	7.8665	0.9650	0.0931
Adventitia							
<i>I</i>	61.5855	18.2281	25.6480	10.2943	4.8062	0.9639	0.1107
<i>II</i>	10.7132	156.5842	11.1898	37.98	9.9076	0.9859	0.08519
<i>III</i>	25.4911	100.16145	1.5610	24.78	2.0010	0.9953	0.0545
<i>IV</i>	14.4963	110.6977	0.6517	29.73	1.5385	0.9919	0.0498
<i>V</i>	21.9789	27.7524	3.7357	21.71	2.9484	0.9970	0.0305
<i>VI</i>	7.9750	59.3600	4.4763	24.98	2.6208	0.9890	0.055
<i>VII</i>	0.2204	90.6244	10.8757	1.54	2.5080	0.9717	0.0979
<i>Mean</i>	9.9148	64.6583	4.7316	15.7513	3.1142	0.9849	0.0636
<i>SD</i>	20.0621	48.8139	8.7111	12.1530	2.8994	0.0125	0.0291
<i>Mean curve</i>	11.3712	88.8978	3.6571	14.78	1.8019	0.9863	0.06198

Table 4

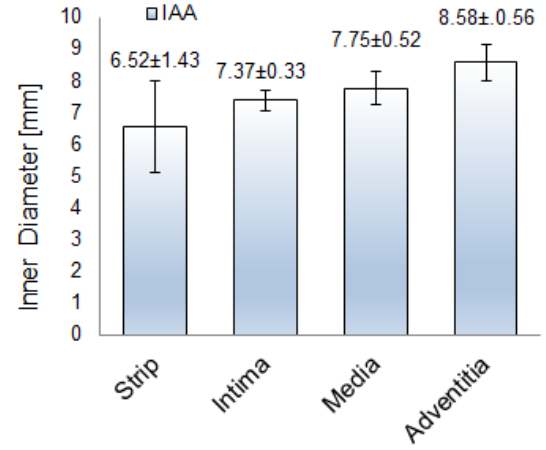
Material constants of the microfiber model (Alastru   et al., 2010) obtained for the IAA curves. Constants  $\mu$  and  $k_1$  in kPa,  $k_2$ ,  $\theta$  in degrees,  $b$  and  $\varepsilon$  dimensionless.

## List of Figures

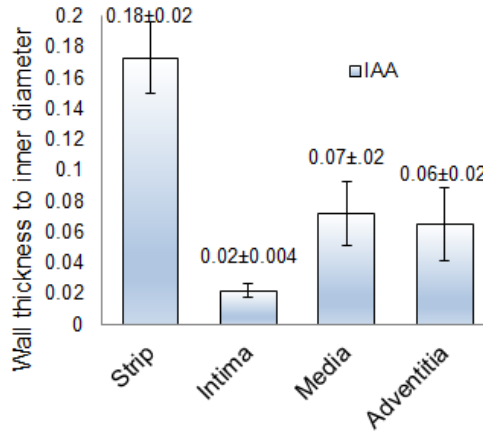
- 1 Column plots of the thickness [mm], inner diameter [mm], ratio of total wall thickness to inner diameter [-] and ratio of layer-thickness to total wall thickness [-] of the IAA samples and the corresponding separated layers (intima, media and adventitia) after 30 min of equilibration. The error bars represent standard deviations. 28
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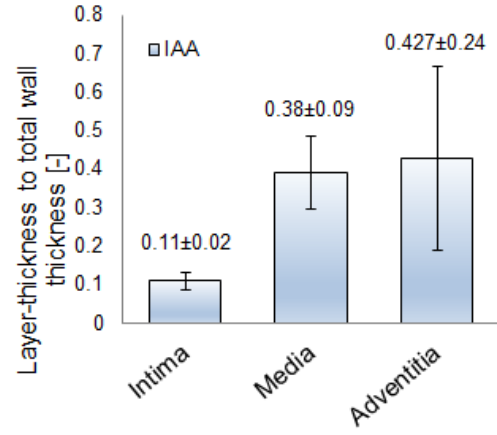
(a) Wall Thickness



(b) Inner Diameter

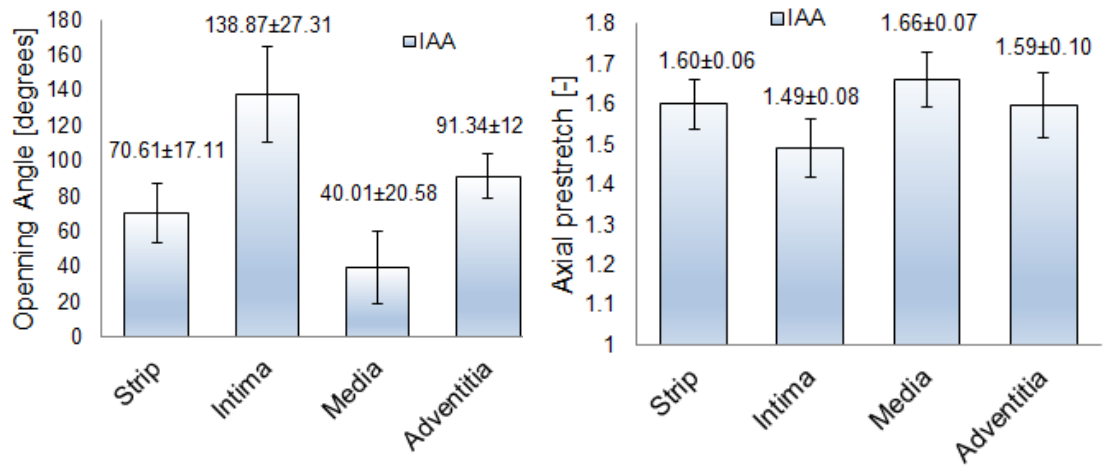


(c) Total wall thickness to inner diameter



(d) Layer-thickness to total wall thickness

Fig. 1. Column plots of the thickness [mm], inner diameter [mm], ratio of total wall thickness to inner diameter [-] and ratio of layer-thickness to total wall thickness [-] of the IAA samples and the corresponding separated layers (intima, media and adventitia) after 30 min of equilibration. The error bars represent standard deviations.



(a) Opening Angle

(b) Axial Prestretch

Fig. 2. Column plots of the opening angle [°] and axial prestretch [-] of the IAA samples and the corresponding separated layers (intima, media and adventitia) after 30 min of equilibration. The error bars represent standard deviations.

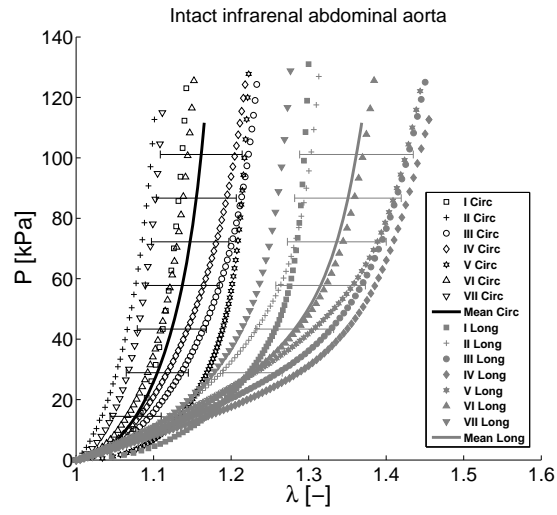


Fig. 3. Uniaxial tensile stress-stretch curves for intact samples I-VII of IAA. Black lines are circumferential directions and grey curves are longitudinal directions. Solid lines are mean curves of experimental data.

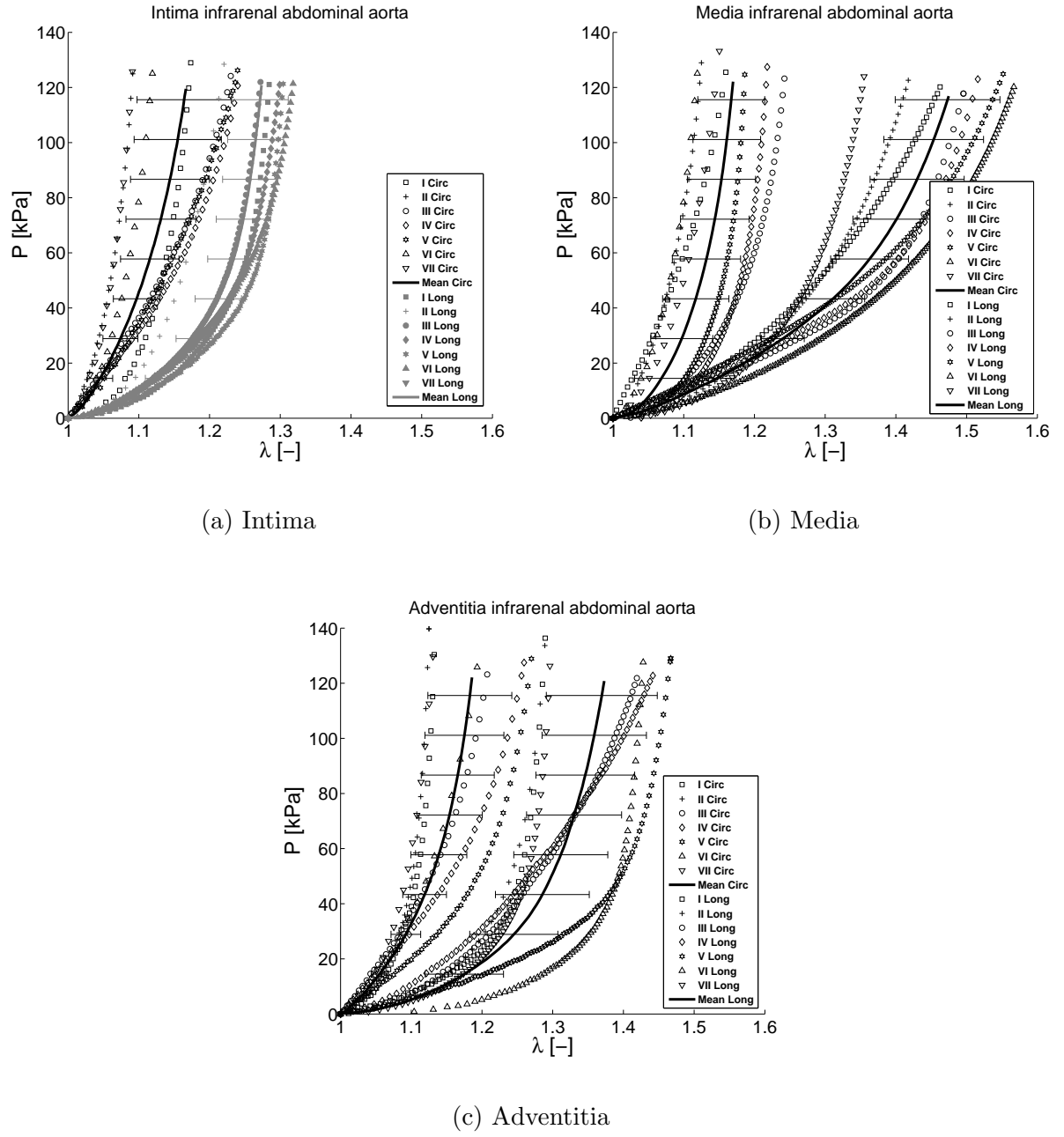
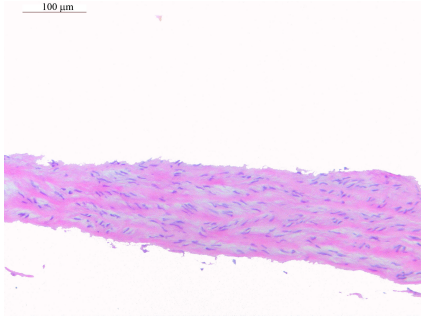
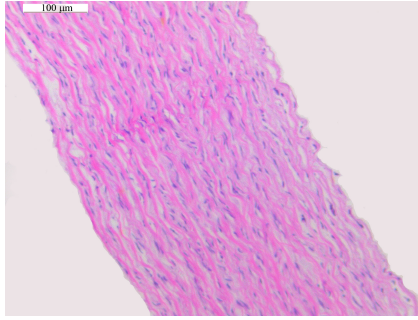


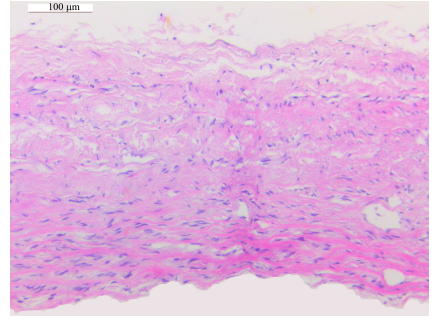
Fig. 4. Uniaxial tensile stress-stretch curves for layer-dissected samples I-VII of IAA. Black lines are circumferential directions and grey curves are longitudinal directions. Solid lines are mean curves of experimental data.



(a) Intima



(b) Media



(c) Adventitia

Fig. 5. Hematoxylin-and-eosin-stained sections 5  $\mu m$  from wall layers after anatomic separation of the IAA. Bar measure 100  $\mu m$



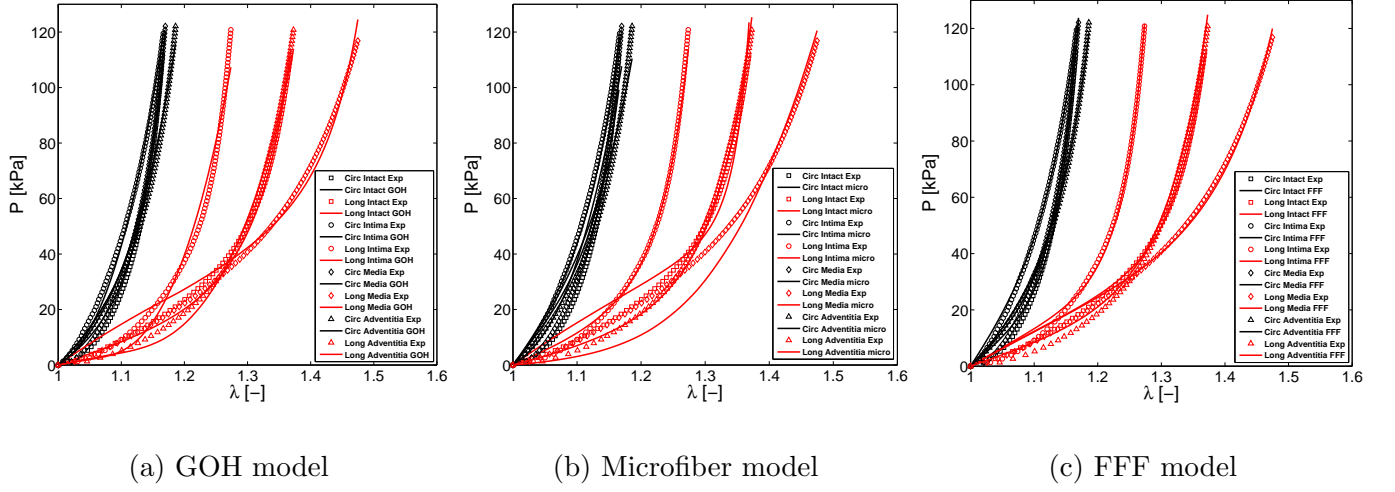


Fig. 6. Mean uniaxial tensile IAA stress-stretch and simulation results with the proposed constitutive models. a) Gasser-Ogden-Holzapfel model (Gasser et al., 2006), b) Microfiber model (Alastru  et al., 2009) and c) Four-Fiber-Family model (Baek et al., 2007).