





RESEARCH ARTICLE

Integrating microbial abundance time series with fermentation dynamics of the rumen microbiome *via* mathematical modelling

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Abstract

The rumen represents a dynamic microbial ecosystem where fermentation metabolites and microbial concentrations change over time in response to dietary changes. The integration of microbial genomic knowledge and dynamic modelling can enhance our system-level understanding of rumen ecosystem's function. However, such an integration between dynamic models and rumen microbiota data is lacking. The objective of this work was to integrate rumen microbiota time series determined by 16S rRNA gene amplicon sequencing into a dynamic modelling framework to link microbial data to the dynamics of the volatile fatty acids (VFA) production during fermentation. For that, we used the theory of state observers to develop a model that estimates the dynamics of VFA from the data of microbial functional proxies associated with the specific production of each VFA. We determined the microbial proxies using CowPi to infer the functional potential of the rumen microbiota and extrapolate their functional modules from KEGG (Kyoto Encyclopedia of Genes and Genomes). The approach was challenged using data from an *in vitro* RUSITEC experiment and from an *in vivo* experiment with four cows. The model performance was evaluated by the coefficient of variation of the root mean square error (CRMSE). For the *in vitro* case study, the mean CVRMSE were 9.8% for acetate, 14% for butyrate and 14.5% for propionate. For the *in vivo* case study, the mean CVRMSE were 16.4% for acetate, 15.8% for butyrate and 19.8% for propionate. The mean CVRMSE for the VFA molar fractions were 3.1% for acetate, 3.8% for butyrate and 8.9% for propionate. Ours results show the promising application of state observers integrated with microbiota time series data for predicting rumen microbial metabolism.

[org/10.5281/zenodo.8401851](https://doi.org/10.5281/zenodo.8401851). The data and scripts of the implementation of the observer for each case study are available at <https://doi.org/10.5281/zenodo.8386786> [48]. Sequencing data for the *in vitro* case study are accessible at the EBI Short Read Archive from the European Nucleotide Archive (accession number PRJEB20255). The sequencing data for the *in vivo* case study are accessible at NCBI SRA under the BioProject PRJNA1023082.

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Introduction

The function of the rumen microbiota affects animal production phenotypes, feed efficiency and methane emissions [1]. Our knowledge on the structure and function of the rumen microbiota has been greatly improved due to the progress on culture independent omic techniques [2, 3]. A powerful use of these techniques is the analysis of microbial time series data allowing to characterise the dynamics of the rumen microbial ecosystem. Applications include the study of microbial colonization of feed particles [4–6], microbial resilience in response to perturbations [7], impact of acidotic challenge on microbial function [8], activity of methanogens in response to the supplementation of a methane inhibitor [9] and evolution of gut microbiota through weaning transition [10, 11].

In parallel to the use of omics techniques to characterise rumen microbiota patterns, dynamic models have been developed to represent the rumen fermentation profile under *in vitro* [12, 13] and *in vivo* [14–16] conditions. Existing models of rumen function consider an aggregated representation of the rumen microbiota and its metabolic function. However, none of these models integrate microbial genomic knowledge and thus do not capitalize on the rich information that microbial genomic sequencing provides. Integration of dynamic modelling and microbial data has the potential to improve the understanding of the rumen ecosystem, to enhance predictive power of rumen models and to help the design of microbial manipulation strategies to improve rumen function [17]. Recently, some studies have applied the genome-scale metabolic approach to reconstruct metabolic networks of rumen microbes species [18–20] and to predict the metabolism of minimal rumen microbial consortium [21]. Another model approach consists in exploiting microbial time series data, with a variety of dedicated mathematical approaches [22] including the generalized Lotka-Volterra (gLV) model [23, 24]. In its standard form, the gLV approach determines interactions between microbes but it does not provide either mechanistic insights or predictions on the dynamics of microbial metabolism. An attempt to couple the gLV approach with a kinetic metabolic model that integrates both microbial interactions and metabolism in a nitrification reactor was developed in [25]. The model was useful to identify qualitative aspects of the system such as the coexistence of two competing bacteria. However, this type of modelling approach based on pairwise microbial interactions is limited to ecosystems with few species due to the high number of parameters that need to be estimated.

In this work, we aim at integrating microbial time series within a dynamic modelling framework *via* the application of state observers (also called software sensors). An observer is an algorithm that combines measurements and a mathematical model to estimate unmeasured variables (see, *e.g.*, [26] for a review). Within the classes of state observers, asymptotic observers are of particular interest since they do not require knowledge on the kinetic functions representing the reaction rates. Asymptotic observers have been applied in simple microbial processes with few microbial species or in processes where the microbiota is represented in aggregated fashion by few microbial functional groups [27, 28]. Observers in combination with optimization routines have been used to assign the metabolic functions of species (Operational Taxonomic Units—OTUs) participating in a nitrification process [29, 30]. In these previous works, the functional assignment of species was translated into an optimization problem which assumes that one species participates only in one reaction. Such a hypothesis might hold for the nitrification process. However, the assumption of single microbial function does not seem to apply to the rumen microbiota, since microbes participate in various metabolic pathways simultaneously. To circumvent the single functional constraint, here we propose a novel approach that uses OTU data to derive microbial functional proxies for specific process of rumen metabolism such as volatile fatty acid (VFA) production. Our approach was tested

firstly using published experimental data from an *in vitro* study [5]. We presented preliminary results of this approach at the 10th Workshop on Modelling Nutrient Digestion and Utilization in Farm Animals (MODNUT, 18th–21st September 2022, Sardinia, Italy). The corresponding abstract is published in the conference proceedings [31]. We performed further an experiment with four cows to assess the modelling approach under *in vivo* conditions. Following open science practices [32], the data and scripts are freely available.

Material and methods

In this section, we provide a general overview of the experimental case studies. Next, we describe the modelling approach.

In vitro case study

We used data from an *in vitro* experiment carried out in RUSITEC (Rumen Simulation Technique) systems [5] to study the feed microbial colonization dynamics of fresh ryegrass or ryegrass hay. Rumen inoculum was obtained from rumen fistulated cows, and the incubation ran for 18 consecutive days in 16 vessels. Fermentation vessels (800 mL effective volume) were inoculated with rumen fluid and incubated with the experimental diets (80:20 forage to concentrate ratio). One bag containing feed (11.25 g DM) was daily supplied to each vessel and incubated for 48h. Artificial saliva was continuously infused at a dilution rate of 3.35%/h (equivalent to 645 mL/d). After 14 days of adaptation to the experimental diets, the fermentation dynamics was monitored during 3 consecutive days. For each day, samples were taken at 2, 4, 8 and 24 h for determination of acetate, butyrate and propionate and for microbial characterization. Metabolite concentrations for each sampling time was reported as the mean value of the three samples. For microbial characterization, the samples were pooled per time point. The microbial RNA was extracted from the liquid and solid phases and the bacterial community structure was characterized by 16SrRNA (cDNA) Next Generation Sequencing (NGS) as previously described [5]. Raw sequence reads are accessible at the EBI Short Read Archive from the European Nucleotide Archive (accession number [PRJEB20255](https://doi.org/10.1093/bioinformatics/btad025)).

In vivo experiment

We conducted an experiment with four Nordic Red dairy cows, selected based on similar calving dates and equipped with rumen fistulas to provide dynamic data to assess our modelling approach *in vivo*. For 10 days of diet adaptation period, cows were offered total mixed ration consisting of grass silage (timothy-meadow fescue sward) preserved with formic acid based additive (AIV Ässä Na; 5 litres/tonne) provided at 45:55 forage to concentrate ratio on a dry matter basis. Concentrate mixture consisted of barley 210, oats 210, wheat 100, sugar beet pulp 220, rapeseed meal 230, and a mixture of minerals and vitamins 30 g/kg on as fed basis. Following the adaptation period, cows were located to metabolic chambers. Day 1 was dedicated to adaptation to the chamber conditions, while on d 2 and d 3 gas exchanges were measured for 48 h (for details see [33]). To determine circadian changes in rumen fermentation and rumen microbial community composition, on chamber d 4 and d 5 for 48 h period rumen liquid samples were collected every 3 h through ruminal fistula from the ventral site of the rumen using 500-mL bottle. Two sub-samples were taken for VFA and ammonia-N determination as described in [11] and were stored at -20°C for later analysis. Rumen liquid samples for microbial analysis were mixed to get homogenous distribution of microorganisms in the liquid, aliquoted into 2-mL sterile screw cap tubes, snap frozen on dry ice and stored at -80°C until DNA extraction. The total DNA was extracted from 500 μL of rumen liquid following protocol described in [34]. Libraries of the bacterial 16S ribosomal RNA (rRNA) V4 region were

prepared using 515F and 806R primers [35] and sequenced on Illumina MiSeq (Finnish Functional Genomics Centre, Turku) using the Paired-End approach and 2 x 250 bp chemistry. The sequencing data are accessible at NCBI SRA under the BioProject [PRJNA1023082](https://www.ncbi.nlm.nih.gov/bioproject/PRJNA1023082).

The cow experiments were conducted at the Luke Minkiö research dairy barn (Finland) and all experimental procedures were approved by the Project Authorisation Board (Regional Administrative Agency for Southern Finland, Hämeenlinna, Finland; ESAVI/34265/2019) in accordance with the guidelines established by the European Community Council Directive 86/609/EEC.

Asymptotic observer and microbial functional proxies

Let us consider a metabolic process occurring in a continuous reactor where n microbial species x_i grow at specific kinetic rates r_i and produce the compound s . We consider that the reactor has a known dilution rate D and that the microbes leave the system at a lower rate than the dilution rate, which implies that the residence time of microbes is higher than the residence time of soluble compounds. The higher microbial residence time results from biological phenomena such as attachment to solid particles and formation of microbial aggregates. A simple way to model this phenomena is by adding a residence time factor α [36]. The dynamics of s and a microbial species x_i follow:

$$\frac{dx_i}{dt} = r_i - \alpha Dx_i$$

$$\frac{ds}{dt} = \sum_{i=1}^n Y_{s,i} r_i - Ds$$

with $Y_{s,i}$ the production yield for the reaction r_i . The kinetic rates r_i can be represented by a mathematical function like the Monod or Haldane equations. These kinetic functions are defined by specific parameters for each microbe x_i . The model equations [1, 2] assume that the microbe x_i participates only in reaction r_i which does not hold for many rumen microbes. We developed here an alternative approach adapted to the rumen microbiota that overpasses the need of assigning functionalities to microbial species. As observed in equation [2], the production of s results from the collective metabolic activity of the microbial consortium. In our approach, we assumed that the production of s can be related to a subunit of the specific metabolic pathways involved in the production of s . This subunit gathers the functional activity of the full consortium and can be used as a proxy of microbial activity of the rumen microbiome. The construction of the microbial proxy will be detailed later on. We will call m_j the microbial proxy associated with the production of s_j . Here, our compounds s_j are the major VFA from rumen fermentation: acetate (s_{ac}), butyrate (s_{bu}) and propionate (s_{pr}).

For the compound s_j , the resulting model is defined by two equations

$$\frac{dm_j}{dt} = \rho_j - \alpha Dm_j$$

$$\frac{ds_j}{dt} = Y_j \rho_j - Ds_j$$

Where ρ_j represents the reaction rate catalysed by the microbial proxy m_j . The next step of the approach consists of building an asymptotic observer that will enable us to estimate the dynamics of s_j from measurements of m_j . For that, let us consider the following state transformation:

$$z_j = s_j - Y_j m_j$$

By deriving in time [5], we get

$$\frac{dz_j}{dt} = -D \left[z_j + (1 - \alpha) Y_j m_j \right]$$

Let us denote \hat{z}_j an on-line estimate of z_j . The dynamics of \hat{z}_j follows

$$\frac{d\hat{z}_j}{dt} = -D \left[\hat{z}_j + (1 - \alpha) Y_j m_j \right]$$

To simulate \hat{z}_j , we require dynamic data of m_j and the parameters α , Y_j to be known. Under these conditions, we can use the estimate \hat{z}_j and the dynamic data m_j to provide an estimate \hat{s}_j at each sampling time:

$$\hat{s}_j = \hat{z}_j + Y_j m_j$$

The asymptotic observer is the conjunction of the measurements m_j with equations [7, 8]. As mentioned before, the approach does not require an explicit definition of the kinetic rate function ρ_j . We applied this development for acetate, butyrate and propionate, which requires measurements of the microbial proxies m_{ac} , m_{bu} , m_{pr} and the yields Y_{ac} , Y_{bu} , Y_{pr} .

For both *in vitro* and *in vivo* case studies, the specific microbial proxy associated to the production of each VFA was derived from rumen microbial time series data determined by 16S rRNA gene amplicon sequencing. Raw data were analyzed using QIIME2 (version 2021.8) [37] using the script (run-samples) in <https://github.com/frubino/cowpi> and <https://doi.org/10.5281/zenodo.8401851>. Data were imported and denoised using the trim length option set at 400 and clustered using vsearch [38], in particular the ‘cluster-features-de-novo’ command with a percent identity set to 0.99. Classification was performed using the ‘feature-classifier-classify-consensus-blast’ that uses BLAST [39] to classify the representative sequences, using default options and the Silva database (version 138) [40]. Finally, the OTU table representing microbial abundance time series was exported to be used in subsequent analysis steps. The resulting OTU table and representative sequences were then analyzed using CowPI [41] and modified using the information available at <https://github.com/frubino/cowpi>. The approach used here includes scaling data using DESeq2 [42] and infers modules from KEGG [43] instead of pathways, using the information in CowPi data. The pipeline for the inference of the functional modules is available at <https://github.com/frubino/cowpi>. KEGG modules resolve more specific processes and allow for greater precision when performing metabolic analysis, and like pathways, genes are their building blocks, so CowPI data can be used. For our analysis, modules allowed us to focus on more detailed aspects of metabolism for our model that pathways would not permit. Consequently, we used information about modules instead of pathways. However, there was no module in KEGG to present the butyrate metabolism. Therefore, an additional module for the metabolism of butyrate was introduced using information from [44]. These modules are the microbial proxies m_j . The abundances of the microbial proxies are relative measurements. However, since the data are scaled, we assumed that the absolute concentrations of microbial proxies are proportional to their relative abundances. As mentioned above, the asymptotic observer requires α and the yield factors to be known. The factor α was set to 0.85 according to [45]. We estimated the yield factors *via* the maximum likelihood (ML) approach as implemented in the Matlab IDEAS toolbox [46], which is freely available at <http://genome.jouy.inra.fr/logiciels/IDEAS>. For the optimization step, the Nelder–Mead Simplex method [47] implemented in the fminsearch function was used. The model performance was

assessed by computing the coefficient of variation of the root mean squared error (CVRMSE). The Matlab scripts are available at [48] <https://doi.org/10.5281/zenodo.8386786>.

Results

The scripts for the inference of the functional microbial modules are available at <https://github.com/frubino/cowpi> and <https://doi.org/10.5281/zenodo.8401851>. The abundances of each module for each case study are in the Tables modules.Rusitec.xls and modules.Cows in [48]. A total of 308 modules were identified. The microbial proxies for VFA production are named as M00579 (m_{ac}), M99999 (m_{bu}), M00013 (m_{pr}). The implementation of the observer for each case study is available at [48].

In vitro case study

Table 1 shows the estimated abundance of the microbial proxies of VFA production. The values are the sum of the abundances from the liquid and solid phase. Fig 1 shows the dynamics of VFA (acetate, butyrate, and propionate) compared to the estimated VFA concentrations by the observer for the *in vitro* experiments with grass and hay using the rumen inoculum from two cows. Table 2 shows the model evaluation in terms of the CVRMSE. The model performance is satisfactory with average CVRMSE for acetate, butyrate and propionate of 9.8%, 14% and 14.5%. Table 3 shows the estimated yield factors for each diet and inoculum. The average values of the yields of acetate, butyrate and propionate are 0.13×10^{-6} , 0.39×10^{-7} and 0.49×10^{-6} .

In vivo case study

Table 4 shows the estimated abundance of the microbial proxies of VFA production from the liquid phase. Fig 2 shows the dynamics of VFA compared to the estimated VFA concentrations by the observer.

Table 5 shows the CVRMSE for the VFA concentrations. The model performance is adequate with average CVRMSE for acetate, butyrate and propionate of 16.4%, 15.8% and 19.8%. As shown in Table 6, the model performance is very satisfactory with regard to prediction of VFA molar proportions. The CVRMSE for the molar proportions of acetate, butyrate and

Table 1. Microbial abundance time series of functional proxies of VFA production for the *in vitro* case study. Values are the sum of the abundances from the liquid and solid phase.

		Sampling time (h)			
		2	4	8	24
Rumen inoculum 1-Grass	m_{ac}	33139	37601	60680	70338
	m_{bu}	52574	57719	116469	109282
	m_{pr}	3503	3669	8181	8971
Rumen inoculum 1-Hay	m_{ac}	14487	42303	36663	82646
	m_{bu}	18600	61808	49934	118876
	m_{pr}	640	4323	3673	13470
Rumen inoculum 2-Grass	m_{ac}	87093	91845	105360	83174
	m_{bu}	184833	206660	227768	235760
	m_{pr}	23114	27944	24257	36697
Rumen inoculum 2-Hay	m_{ac}	111166	106780	101168	102789
	m_{bu}	240822	240218	194157	218833
	m_{pr}	31287	31758	22945	22005

m_{ac} , m_{bu} , m_{pr} : abundances of microbial functional proxies for acetate, butyrate and propionate production.

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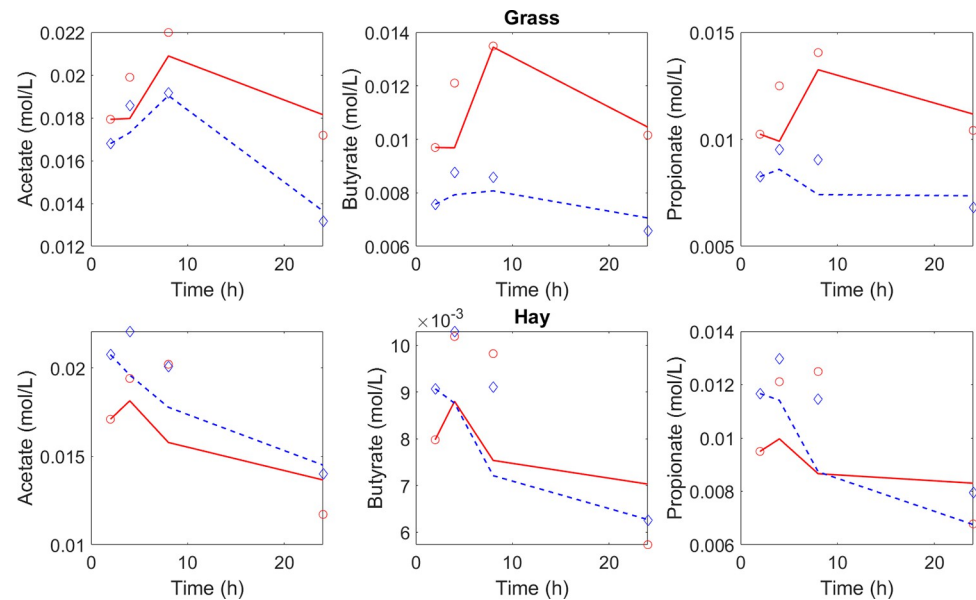


Fig 1. Experimental data of VFA concentrations from a RUSITEC experiment with two feeds (grass and hay) and rumen fluid from two cows (○: cow 1; ◇: cow 2) are compared against the estimated concentrations by the state observer (red solid line for cow 1, dashed blue line for cow 2).

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propionate are 3.1%, 3.8% and 8.9%. Table 7 shows the estimated yield factors for each cow. The average values of the yields of acetate, butyrate and propionate are 1.43×10^{-6} , 1.62×10^{-7} and 2.43×10^{-6} .

Discussion

The objective of this work was to integrate rumen microbiota time series determined by 16S rRNA gene amplicon sequencing into a mathematical model linking microbial data to the dynamics of the volatile fatty acids (VFA) production during rumen fermentation. This objective followed the rationale that microbial data can be used to enhance predictive capabilities of rumen fermentation models. Our model development provided satisfactory results for estimating the dynamics of VFA from microbial data. The *in vivo* study showed that yield factors for the specific VFA production are similar between the cows. It will be useful to test our approach with animals fed at different diets including diets supplemented with additives impacting rumen fermentation patterns.

Given the limited number of animals used in our study, it is difficult to provide a fair comparison with existing rumen models. Furthermore, few rumen modelling studies have compared model predictions against dynamic data of VFA concentrations, with the exception of

Table 2. Coefficient of variation of the root mean square error (%) for the observer applied to *in vitro* data of VFA concentrations.

	Acetate	Butyrate	Propionate
Rumen inoculum 1- Grass	7.1	11.8	13.2
Rumen inoculum 2- Grass	4.6	7.8	1.3
Rumen inoculum 1- Hay	16.9	20	25.6
Rumen inoculum 2- Hay	10.5	16.4	18
Mean \pm s.d.	9.8 ± 5.3	14 ± 5.3	14.5 ± 10.2

<https://doi.org/10.1371/journal.pone.0298930.t002>

Table 3. Estimated yield parameters for the *in vitro* data.

	Y_{ac}	Y_{bu}	Y_{pr}
Rumen inoculum 1- Grass	0.19×10^{-6}	0.77×10^{-7}	0.93×10^{-6}
Rumen inoculum 2-Grass	0.17×10^{-6}	0.26×10^{-7}	0.14×10^{-6}
Rumen inoculum 1-Hay	0.07×10^{-6}	0.30×10^{-7}	0.29×10^{-6}
Rumen inoculum 2-Hay	0.11×10^{-6}	0.22×10^{-7}	0.23×10^{-6}
Mean \pm s.d.	$0.13 \times 10^{-6} \pm 5.3 \times 10^{-8}$	$0.39 \times 10^{-7} \pm 2.54 \times 10^{-8}$	$0.40 \times 10^{-6} \pm 3.61 \times 10^{-7}$

Y_{ac} , Y_{bu} , Y_{pr} : yields of acetate, butyrate and propionate production (mol VFA / microbial functional proxy abundance).

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the work of [16]. Under this context, however, it should be mentioned that the CVRMSE of our modelling approach are lower than those reported in [16], which strengthens our model development. From the modelling perspective, the structure of the model developed here is very simple compared to the structure of the existing rumen models. This parsimonious property is of usefulness for the development of *in silico* tools to predict rumen function from microbial data within a Precision Livestock Farming context. It should be said, however, that our study is a theoretical work that demonstrates the proof of concept that rumen microbial data can be used to predict rumen fermentation variables. However, the application of our modelling approach in farm conditions is currently unfeasible due to the need of rumen sampling and the costs of microbial analysis. To overcome the obstacle of rumen accessibility, it will be useful to test our approach using buccal microbial samples as proxies of the rumen microbiota [49, 50]. Buccal sampling might be a solution for getting quick samples and if it is coupled with easy sequencing instrument, it might become possible to use this approach to estimate rumen VFA using our modelling approach.

The fundamental aspect of our approach is the definition of the microbial proxies for each VFA. The microbial proxies here developed followed the principle that the rumen ecosystem operates as supra-organism provided with all the metabolic capabilities of its species. This approach does not account for species connectivity which is a relevant aspect in gut microbial ecosystems [51]. It is indeed interesting that the aggregated microbial proxies provided an

Table 4. Microbial abundance time series of functional proxies of VFA production for the *in vivo* case study. Values are from the liquid phase.

		Sampling time (h)															
		7	10	13	16	19	22	25	28	31	34	37	40	43	46	49	52
Cow 1	m_{ac}	47708	45126	55602	57647	64097	56031	54965	65061	54497	69391	57204	67378	63766	67489	57861	56384
	m_{bu}	76650	72740	92161	95845	108538	89023	90047	108791	90950	117048	94074	115549	109147	112391	96751	97451
	m_{pr}	7229	6963	10052	9955	11753	8104	8651	11608	9396	12755	10278	13197	11730	11249	10067	11329
Cow 2	m_{ac}	49745	48073	52536	49837	59831	58632	58376	40248	66988	69821	67276	54960	64366	50587	58103	54381
	m_{bu}	80804	80864	87082	84439	98867	102169	97994	67514	113688	118291	114353	94216	110819	87848	100618	96853
	m_{pr}	8064	8626	9009	8991	9808	11502	9774	6934	12201	12928	12633	10080	12292	9732	11186	10745
Cow 3	m_{ac}	42144	48535	50274	55855	45496	58116	49365	54277	52852	66731	60735	53184	54231	65121	49727	51256
	m_{bu}	73426	84226	85419	97337	78949	102467	80924	93929	89409	111399	102816	90607	92020	110914	84625	91281
	m_{pr}	8149	9554	9264	11066	8440	11366	7839	10324	9596	11580	11227	10341	9335	11322	9163	10974
Cow 4	m_{ac}	46298	12944	58665	60244	54556	55437	53430	54539	60154	64751	56813	56088	58200	53288	52679	57640
	m_{bu}	77495	24482	99615	100443	90413	95868	86833	90640	103506	114801	93832	93850	101479	89818	91936	98357
	m_{pr}	8128	2847	10811	10838	9539	10574	8927	9399	12079	13578	10265	9756	11216	9414	10771	11167

m_{ac} , m_{bu} , m_{pr} : abundances of microbial functional proxies for acetate, butyrate and propionate production.

<https://doi.org/10.1371/journal.pone.0298930.t004>

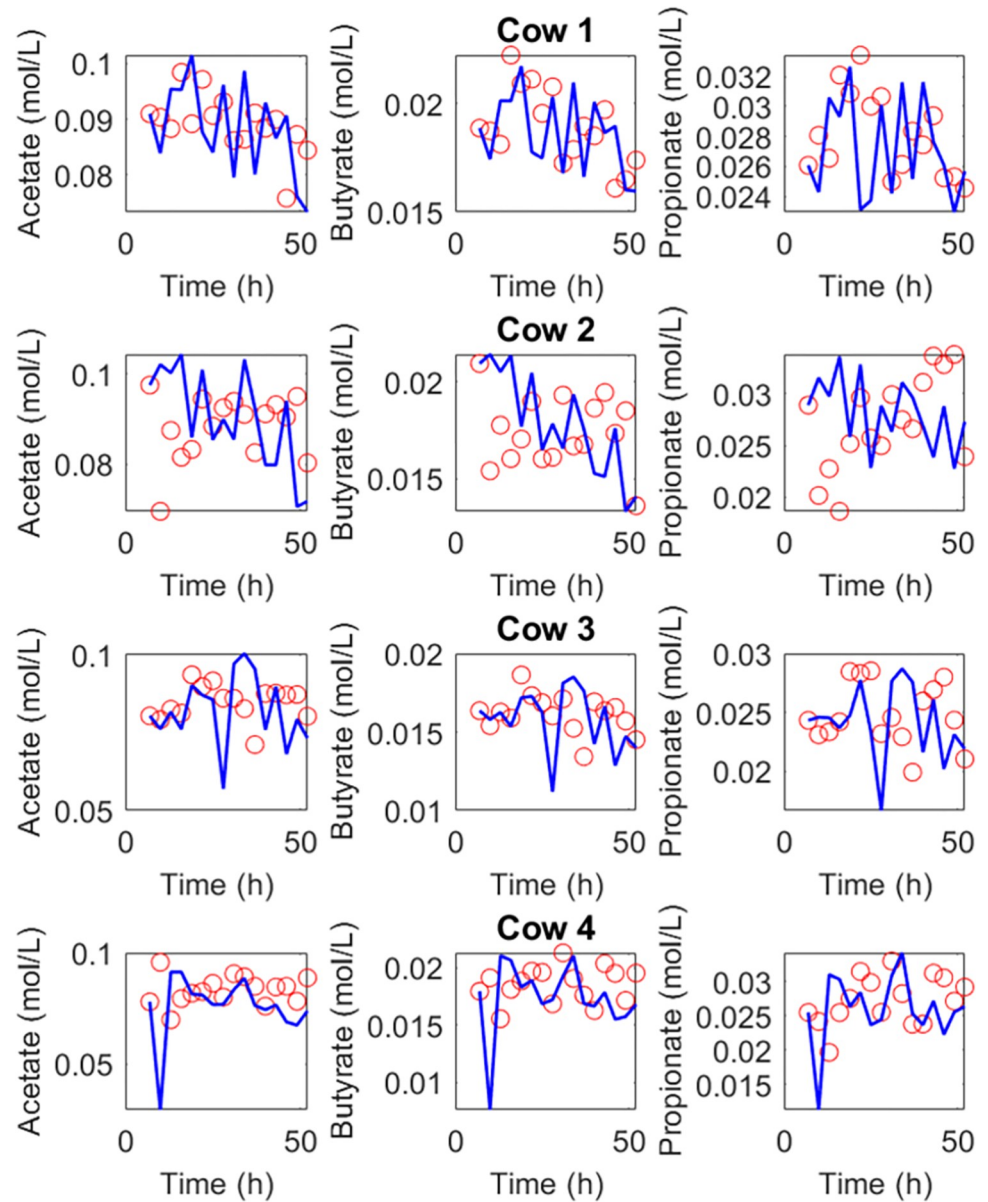


Fig 2. Experimental data of VFA concentrations (o) from an *in vivo* experiment with four cows are compared against the estimated concentrations by the state observer (blue solid line).

<https://doi.org/10.1371/journal.pone.0298930.g002>

Table 5. Coefficient of variation of the root mean square error (%) for the observer applied to *in vivo* data of VFA concentrations.

	Acetate	Butyrate	Propionate
Cow 1	10.1	10.2	14.7
Cow 2	15.4	14.1	17.1
Cow 3	16.5	18.4	25.9
Cow 4	23.8	20.5	21.3
Mean ± s.d.	16.4 ± 5.6	15.8 ± 4.6	19.8 ± 4.9

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Table 6. Coefficient of variation of the root mean square error (%) for the observer applied to *in vivo* data of VFA molar proportions.

	Acetate	Butyrate	Propionate
Cow 1	2.9	3.4	8.3
Cow 2	1.8	2.8	5.7
Cow 3	3.6	4.6	10.9
Cow 4	4.2	4.5	10.5
Mean ± s.d.	3.1 ± 1.0	3.8 ± 0.9	8.9 ± 2.4

<https://doi.org/10.1371/journal.pone.0298930.t006>

Table 7. Estimated yield parameters for the *in vivo* data.

	Y_{ac}	Y_{bu}	Y_{pr}
Cow 1	1.38×10^{-6}	1.73×10^{-7}	2.37×10^{-6}
Cow 2	1.52×10^{-6}	1.55×10^{-7}	2.16×10^{-6}
Cow 3	1.43×10^{-6}	1.50×10^{-7}	2.64×10^{-6}
Cow 4	1.39×10^{-6}	1.83×10^{-7}	2.54×10^{-6}
Mean ± s.d.	$1.43 \times 10^{-6} \pm 6.28 \times 10^{-8}$	$1.62 \times 10^{-7} \pm 1.56 \times 10^{-8}$	$2.43 \times 10^{-6} \pm 2.10 \times 10^{-7}$

Y_{ac} , Y_{bu} , Y_{pr} : yields of acetate, butyrate and propionate production (mol VFA / microbial functional proxy abundance).

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adequate representation of VFA dynamics. Although the results are promising, future research is needed to refine the definition of these proxies, by taking into account quantitative transcriptomic information to identify the actual metabolic activity.

Our study has taken a step in the direction of capitalizing on microbial data to predict rumen function. In this first step, we used asymptotic state observers due to its simple structure and the advantage of not requiring information on the mathematical functions describing the metabolic kinetic rates. However, asymptotic observers have the limitation that the convergence rate cannot be tuned because it is determined by operational conditions (*e.g.*, ruminal fractional passage rate). This limitation can be overcome by other observers. However, more sophisticated technicalities are needed for the design and implementation of such observers [26]. Our approach was applied to estimate VFA dynamics. We think that the approach can be extended to estimate other metabolites including methane production by the rumen methanogenic archaea. Such an application will be of great interest for the monitoring of methane emissions and for the evaluation of methane inhibition strategies.

Conclusions

Existing mechanistic models of rumen fermentation consider an aggregated representation of the rumen microbiota and its metabolic function. However, none of these models integrate microbial genomic knowledge and thus do not capitalize on the rich information of microbial genomic sequencing. In this work, we integrated microbial time series of the rumen microbiota determined by 16S rDNA into a dynamic model of the rumen microbiome. Our results showed the estimated VFA concentrations converge towards the real VFA concentration dynamics demonstrating the promising potential of our approach.

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