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# Large sub-Kelvin magnetocaloric effect and phase behavior of gadolinium nitrate hexahydrate

Cite as: APL Mater. 14, 031119 (2026); doi: 10.1063/5.0316768

Submitted: 15 December 2025 • Accepted: 10 March 2026 •

Published Online: 25 March 2026



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## ABSTRACT

We report a comprehensive magnetothermal study of the classical gadolinium salt  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at temperatures approaching absolute zero. Despite its long-standing availability as a commercial compound, its magnetocaloric properties have remained unexplored. Using electron paramagnetic resonance, magnetic susceptibility, heat capacity, and direct measurements of the magnetocaloric effect, we reveal that weak dipolar interactions combined with axial crystal-field anisotropy drive antiferromagnetic ordering at  $T_N = 0.21$  K. Remarkably,  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  exhibits an isothermal magnetic entropy change of  $-\Delta S_m = 26.1 \text{ J K}^{-1} \text{ kg}^{-1}$  at  $T = 0.6$  K for a modest field variation of  $\Delta B = 1$  T and an adiabatic temperature change of  $\Delta T_{\text{ad}} = 5.0$  K at  $T = 1.6$  K for the same  $\Delta B$ , placing its performance among the strongest reported for Gd-based refrigerants under comparable low-field and sub-Kelvin conditions. These results provide a reference for understanding magnetocaloric behavior in hydrated salts and highlight the interplay between dipolar coupling and crystal-field anisotropy.

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## I. INTRODUCTION

The adiabatic demagnetization refrigerator (ADR) operates based on the magnetocaloric effect (MCE), which describes the reversible changes in isothermal magnetic entropy,  $\Delta S_m$ , and adiabatic temperature,  $\Delta T_{\text{ad}}$ , which occur in magnetocaloric materials under variations of the applied magnetic field,  $\Delta B$ .<sup>1,2</sup> The ADR was the first technology developed to achieve temperatures approaching absolute zero, nearly a century ago.<sup>3</sup> Since then, it has been widely employed, particularly in situations where the use of cryogenic fluids is impractical.<sup>4,5</sup> For example, ADRs are frequently used in zero-gravity environments to cool down x-ray detectors or sensors onboard space observatories and telescopes. Moreover, recent advances in multi-stage ADR systems, together with the increasing scarcity and high cost of the rare <sup>3</sup>He isotope,<sup>6,7</sup> have further increased interest in ADR technology. As a result, modern applications that require sub-Kelvin temperatures, such as quantum devices, are increasingly adopting ADRs to achieve these extreme conditions.<sup>8</sup>

Over the past century, numerous magnetocaloric materials have been investigated for integration into ADR systems operating at the lowest temperatures. The design of efficient refrigerants requires materials that simultaneously exhibit (i) high magnetic density, (ii) low crystal-field anisotropy, and (iii) the absence of magnetic phase transitions at least down to the operational temperature.<sup>9</sup> In this context, the rare-earth ion  $\text{Gd}^{3+}$  is often favored for cryogenic magnetocaloric applications due to its isotropic <sup>8</sup>S<sub>7/2</sub> electronic ground state, which enables a large MCE that remains significant at very low temperatures. For that reason, a wide range of  $\text{Gd}^{3+}$ -based compounds have been explored, including  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$  (GGG),<sup>10</sup>  $\text{GdLiF}_4$ ,<sup>11</sup>  $\text{Gd}(\text{HCOO})_3$ ,<sup>12</sup>  $\text{GdPO}_4$ ,<sup>13</sup>  $\text{GdF}_3$ ,<sup>14</sup>  $\text{GdVO}_4$ ,<sup>15</sup>  $\text{Gd}(\text{OH})\text{F}_2$ ,<sup>16</sup>  $[\text{GdCl}_3] \cdot 6\text{H}_2\text{O}$  and  $[\text{Gd}_2(\text{SO}_4)_3] \cdot 8\text{H}_2\text{O}$ ,<sup>17</sup>  $\{\text{Gd}_2\}$ ,<sup>18</sup>  $\{\text{GdW}_{10}\}$  and  $\{\text{GdW}_{30}\}$ ,<sup>19</sup>  $\{\text{GdZn}\}$ ,<sup>20</sup>  $\{\text{Gd}_7\}$ ,<sup>21</sup>  $\text{Ba}_2\text{GdSbO}_6$  and  $\text{Sr}_2\text{GdSbO}_6$ ,<sup>22</sup>  $\text{KBaGd}(\text{BO}_3)_2$ ,<sup>23</sup>  $\{\text{Gd}_{12}\text{Na}_6\}$ ,<sup>24</sup> or  $\text{Gd}_{9,33}[\text{SiO}_4]_6\text{O}_2$ .<sup>25</sup> However, despite the historical relevance of  $\text{Gd}^{3+}$ -based materials, the magnetothermal and magnetocaloric properties of the classical gadolinium salt  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ , originally proposed as a refrigerant decades ago<sup>26</sup> and later employed as a precursor for

synthesizing more complex refrigerants,<sup>27–33</sup> remain largely unexplored. To the best of our knowledge, only a few studies have addressed its magnetic susceptibility (limited to temperatures down to 2 K)<sup>34,35</sup> and its spectroscopic properties.<sup>36</sup>

Herein, we present, for the first time, a comprehensive investigation of the magnetic and magnetocaloric properties of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at temperatures approaching absolute zero. To complete its physical characterization, we performed measurements on 1% diluted samples of  $[\text{R}_{0.99}\text{Gd}_{0.01}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  (hereafter denoted as  $[\text{Gd@R}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ ), where R represents various trivalent host ions. Our results reveal that  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  undergoes antiferromagnetic ordering at the Néel temperature  $T_N = 0.21$  K, driven by dipolar interactions combined with crystal-field anisotropy. Furthermore, a significant MCE is observed at sub-Kelvin temperatures under low magnetic fields, positioning  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  among the leading  $\text{Gd}^{3+}$ -based candidates for ADR operation in this temperature regime.

## II. MATERIALS AND METHODS

$[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  and  $[\text{Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were obtained from commercial sources (Sigma-Aldrich, 99.90%) and used without further purification. Both materials crystallize in the triclinic space group *P*-1 (see CIF files with CCDC reference numbers 1632 729 and 1541 802, respectively). For the synthesis of 1% diluted polycrystalline powder of  $[\text{Gd@Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ , 4.63 mg of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  (0.01 mmol) and 450.90 mg of  $[\text{Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  (1.18 mmol) were mixed and dissolved in the minimum volume of distilled water. The resulting solutions were dried under active vacuum. After several days, a white powder was obtained. All compounds remained structurally stable under our experimental conditions, with no indication of measurable dehydration.

Continuous-wave electron paramagnetic resonance (EPR) measurements on a 1% diluted polycrystalline sample of  $[\text{Gd@Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were recorded using a Bruker Elexys 580 spectrometer operating in the X-band (9.715 GHz). The setup included an Oxford CF900 continuous gas-flow cryostat and a Mercury iTC temperature controller, which employed liquid helium for cooling and provided precise temperature regulation. A Bruker MD5 resonator was used with an external field modulation of 0.2 mT at 100 kHz. Spectra collected at 5 and 10 K were identical within experimental resolution. The microwave power was adjusted to avoid saturation effects, and the magnetic field was measured with a Bruker ER035 gaussmeter. Simulations of the spectra were performed with the EasySpin toolbox for MATLAB.<sup>37</sup>

Direct-current (DC) magnetic measurements on  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were performed on a Quantum Design MPMS-3 system. A polycrystalline powder sample (~5 mg) was loaded into a plastic capsule and immobilized with eicosane wax to prevent grain movement. Isothermal magnetization curves were collected in magnetic fields between 0 and 7 T over the temperature range 2–10 K. DC magnetic susceptibility data were recorded over the same temperature range under a constant applied magnetic field of  $B = 0.1$  T. All data obtained were corrected for diamagnetic contributions coming from both the sample holder and eicosane wax. In addition, the complex alternating-current (AC) magnetic susceptibility,  $\chi' - i\chi''$ , was measured under zero applied magnetic

field over the temperature range of 0.05–4 K, using a frequency of 525 Hz and an AC field amplitude of  $2 \times 10^{-4}$  T. Measurements were performed with a Quantum Design PPMS DynaCool equipped with the  $^3\text{He}$ - $^4\text{He}$  dilution refrigerator (DR) option. A thin pressed polycrystalline pellet (~6 mg) was prepared for these experiments, and susceptibility data were initially recorded in arbitrary units. Absolute values of the real component,  $\chi'$ , were obtained by comparison with DC susceptibility data collected with the MPMS-3 in the overlapping temperature range (2–4 K), where dissipative processes are negligible. The imaginary component,  $\chi''$ , is reported in arbitrary units.

Heat capacity measurements on  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were carried out using the relaxation method in a Quantum Design PPMS equipped with a  $^3\text{He}$  cryostat, covering temperatures down to 0.4 K under constant magnetic fields from 0 to 7 T. Additional measurements extended to 0.05 K under fields up to 1 T using a Quantum Design PPMS DynaCool with a DR module. The samples consisted of thin pressed polycrystalline pellets (~1 mg for  $^3\text{He}$  and ~0.2 mg for DR). In both setups, Apiezon N grease (~0.1 mg) was applied to ensure good thermal contact between the sample and the calorimeter platform. Its contribution to the total heat capacity was subtracted using a phenomenological correction.

Direct quasi-adiabatic MCE measurements on  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were performed for complete demagnetization processes using the DR of the DynaCool. For these experiments, a pressed polycrystalline pellet of ~5 mg was mounted on a calorimeter platform coated with ~0.2 mg of Apiezon N grease to improve thermal coupling. In addition, the MCE of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  was also evaluated indirectly by applying standard thermodynamic relations to the measured magnetization and heat capacity data.

## III. RESULTS AND DISCUSSION

### A. Electron paramagnetic resonance

The zero-field splitting parameters for  $\text{Gd}^{3+}$  in  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were determined from EPR measurements by modeling the spectra with the spin Hamiltonian

$$\mathcal{H} = b_2^0 \left( \frac{s_z}{\hbar} \right)^2 + \frac{b_2^2}{3} \left( \frac{s_x^2 - s_y^2}{\hbar^2} \right) - g_J \mu_B \vec{B} \cdot \left( \frac{\vec{s}}{\hbar} \right), \quad (1)$$

where  $\vec{s}$  is the spin operator with quantum number  $s = 7/2$ . The parameters  $b_2^0$  and  $b_2^2$  represent the first-order zero-field splitting terms associated with axial and in-plane crystal-field anisotropy, respectively. Here,  $g_J$  is the Landé factor;  $\mu_B$  is the Bohr magneton; and  $\hbar$  is the reduced Planck constant. The three terms in Eq. (1) correspond to axial anisotropy, in-plane anisotropy, and the Zeeman interaction.

To minimize magnetic interactions that could otherwise hinder the determination of zero-field splitting parameters, EPR measurements were performed on diluted, isomorphous host matrices. This approach was first implemented by Misra and Mikolajczak,<sup>38</sup> who determined the anisotropy parameters of  $\text{Gd}^{3+}$  in  $[\text{Gd@R}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  single crystals for various trivalent host ions R. Particularly relevant are the results for 1% diluted  $[\text{Gd@Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  and  $[\text{Gd@Sm}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  since the ionic radius of  $\text{Gd}^{3+}$  lies between those of  $\text{Y}^{3+}$  and  $\text{Sm}^{3+}$ . The paramagnetic  $\text{Sm}^{3+}$  ion is an appropriate host because it undergoes rapid spin

flips; viz., it has a very short spin-lattice relaxation time, rendering its interaction with  $\text{Gd}^{3+}$  negligible on the EPR timescale.<sup>38,39</sup>

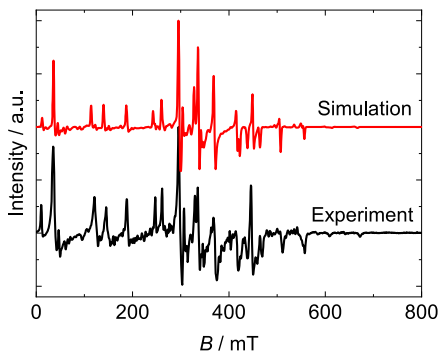
The same study by Misra and Mikolajczak<sup>38</sup> revealed that  $b_2^0$  and  $b_2^2$  vary linearly with the host ionic radius and exhibit a temperature dependence. Since the present work focuses on the low-temperature properties of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ , it is essential to determine these parameters at cryogenic temperatures. Among the hosts considered, only  $[\text{Gd}@\text{Sm}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  was previously investigated at liquid-helium temperatures, yielding  $b_2^0/k_B = -0.095(1)$  K and  $b_2^2/3k_B = 0.017$  K.<sup>38</sup> To complement these data, we conducted continuous-wave EPR experiments on a 1% diluted polycrystalline sample of  $[\text{Gd}@\text{Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at liquid-helium temperatures (Fig. 1). The experimental spectrum is accurately reproduced, assuming  $g_J = 2.0$ ,  $b_2^0/k_B = -0.072(2)$  K, and  $b_2^2/3k_B = 0.015(2)$  K.

Finally, the zero-field splitting parameters for  $\text{Gd}^{3+}$  in  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  were estimated by linear interpolation between the values obtained for the  $\text{Y}^{3+}$  and  $\text{Sm}^{3+}$  hosts, yielding  $b_2^0/k_B = -0.087(3)$  K and  $b_2^2/3k_B = 0.016(2)$  K (Fig. 2). The ionic radii were taken from Ref. 40 for coordination number 6. These results confirm that the anisotropy is predominantly axial. Consequently, for  $B = 0$ , the 4 twofold-degenerate energy levels of  $\text{Gd}^{3+}$  in  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  can be approximated by  $s_z = \pm 7/2, \pm 5/2, \pm 3/2, \pm 1/2$ , ordered from lowest to highest energy. The corresponding level spacings are comparable with those reported for other  $\text{Gd}^{3+}$  salts.<sup>17,39,41</sup>

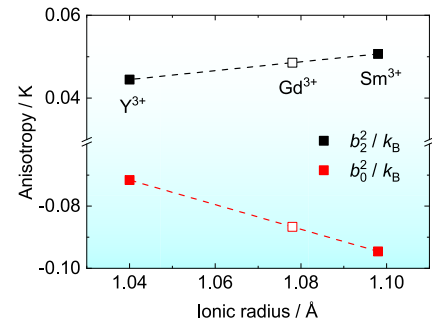
## B. Magnetization and magnetic susceptibility

Figure 3 shows the isothermal molar magnetization,  $M$ , of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at selected temperatures. The experimental curves closely follow Brillouin-type behavior throughout the investigated temperature range. At 2 K and under high magnetic fields, the magnetization saturates at  $7.0 N_A \mu_B$ , consistent with non-interacting  $\text{Gd}^{3+}$  ions characterized by  $s = 7/2$  and  $g_J = 2.0$ .

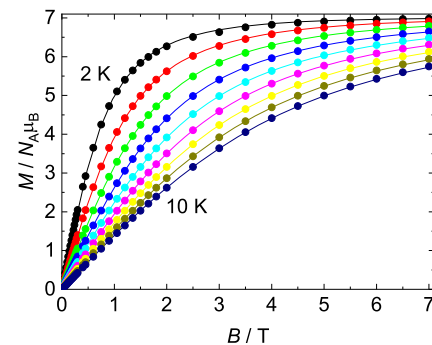
Figure 4 shows the real,  $\chi'$ , and imaginary,  $\chi''$ , components of the magnetic susceptibility of polycrystalline  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  for temperatures below 1 K. The data strongly suggest the onset of antiferromagnetic ordering. A pronounced maximum in  $\chi'$  occurs



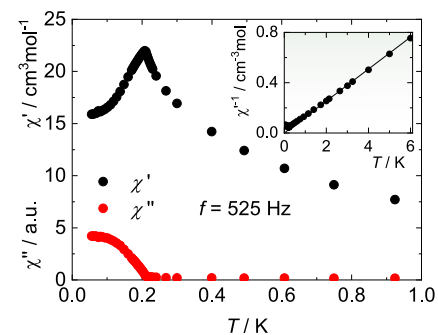
**FIG. 1.** Continuous-wave EPR spectra of  $\text{Gd}^{3+}$  on a 1% diluted polycrystalline sample of  $[\text{Gd}@\text{Y}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at  $T = 5$  K. Black line = experimental data; red line = simulation of a  $s = 7/2$  spin system with  $g_J = 2.0$  and crystal-field anisotropy parameters  $b_2^0/k_B = -0.072$  K and  $b_2^2/3k_B = 0.015$  K.



**FIG. 2.** Zero-field splitting parameters  $b_2^0/k_B$  and  $b_2^2/k_B$  for  $\text{Gd}^{3+}$  at liquid-helium temperatures as a function of the host ionic radius. The filled symbols represent values obtained from EPR measurements; the open symbols correspond to interpolated estimates.



**FIG. 3.** Isothermal magnetization  $M$  of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at selected temperatures. The filled symbols represent experimental data; the solid lines correspond to Brillouin-function fits.



**FIG. 4.** Real ( $\chi'$ ) and imaginary ( $\chi''$ ) components of the magnetic susceptibility of polycrystalline  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  below 1 K. Inset: Inverse of the real component of the magnetic susceptibility,  $\chi'^{-1}$ . The filled symbols represent experimental data; the solid line corresponds to the Curie-Weiss fit.

at the Néel temperature  $T_N = 0.21$  K, reaching  $22.0 \text{ cm}^3 \text{ mol}^{-1}$ . Below  $T_N$ ,  $\chi'$  decreases gradually, while  $\chi''$  becomes non-zero, indicating the emergence of dissipative processes. The inverse susceptibility  $\chi'^{-1}$  exhibits a linear temperature dependence down to 2 K, below which slight deviations from linearity appear, culmi-

nating in an upward anomaly at  $T_N = 0.21$  K, characteristic of an antiferromagnetic phase transition (inset of Fig. 4). The fit to the Curie–Weiss law  $\chi'^{-1} = (T - \theta_W)/C$  yields the Curie constant of  $C = 7.88(1) \text{ cm}^3 \text{ K mol}^{-1}$ , in excellent agreement with the expected value for non-interacting  $\text{Gd}^{3+}$  ions and the Weiss temperature  $\theta_W = -0.02(1)$  K. This nearly vanishing Weiss temperature is fully consistent with previous reports.<sup>34,35</sup>

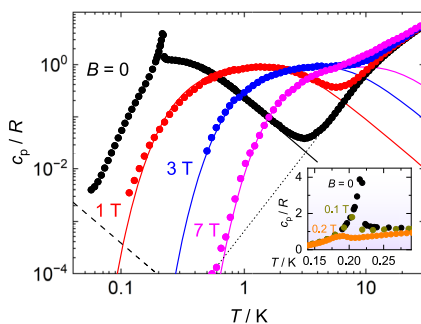
### C. Heat capacity

Figure 5 presents the heat capacity,  $c_p$ , of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ . At zero applied magnetic field, a pronounced  $\lambda$ -type anomaly appears at  $T_N = 0.21$  K, coinciding with the Néel temperature identified from magnetic susceptibility measurements. This anomaly shifts to lower temperatures under small applied fields (see the inset of Fig. 5), consistent with antiferromagnetic ordering. Below  $T_N$ ,  $c_p$  decreases exponentially, as expected for an antiferromagnetic ground state with a crystal-field anisotropy-induced energy gap.<sup>42</sup> At the lowest temperatures, a slight upturn in  $c_p$  is observed, most likely arising from hyperfine contributions associated with the  $^{155}\text{Gd}$  and  $^{157}\text{Gd}$  isotopes (combined natural abundance  $\approx 30\%$ ), both of which possess nuclear spin  $I = 3/2$ . Notably, assuming an isotropic hyperfine interaction of the form  $\mathcal{H} = A\mathbf{I} \cdot \mathbf{s}/\hbar^2$ , a coupling constant  $A = 0.8$  mK satisfactorily accounts for the anomaly (Fig. 5, dashed line). This value of  $A$  is consistent with hyperfine parameters reported for  $\text{Gd}^{3+}$  in various host matrices.<sup>43</sup>

A broad Schottky-like anomaly is observed underneath the  $\lambda$ -type peak, likely arising from a combination of crystal-field anisotropy and magnetic interactions. To clarify its origin, we analyzed the high-temperature tail of this anomaly. For magnetic ions with spin  $s$  subjected to axial and in-plane crystal-field anisotropy parameters  $b_0^2$  and  $b_2^2$ , the high-temperature expansion of the heat capacity is given by

$$\frac{c_{\text{cf}}T^2}{R} = \frac{s(s+1)(2s+3)(2s-1)\left[(b_0^2)^2 + \frac{1}{3}(b_2^2)^2\right]}{45k_B^2}, \quad (2)$$

as derived in Ref. 44. For  $\text{Gd}^{3+}$  ions with  $s = 7/2$  and zero-field splitting parameters  $b_0^2/k_B = -0.087$  K and  $b_2^2/3k_B = 0.016$  K,



**FIG. 5.** Temperature dependence of the heat capacity  $c_p$  of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  for selected magnetic fields. Inset: Low-temperature  $c_p$  under small applied magnetic fields. The filled symbols represent experimental data; the solid lines correspond to calculated values; the dotted line indicates the lattice heat capacity; and the dashed line represents the hyperfine contribution.

as determined for  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ , the calculated value is  $c_{\text{cf}}T^2/R = 0.17 \text{ K}^2$ . The dipolar contribution to the Schottky-like tail can also be estimated. Following the van Vleck formalism,<sup>45</sup> the high-temperature expansion of the dipolar term is

$$\frac{c_{\text{dip}}T^2}{R} = \frac{QT^2}{6}, \quad (3)$$

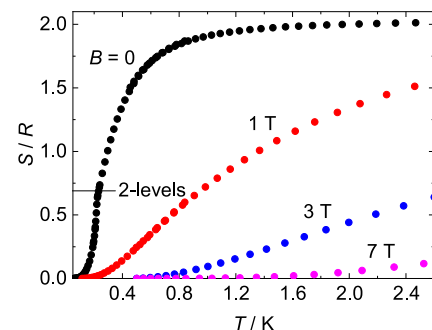
where  $\tau = N_s g_J^2 \mu_B^2 s(s+1)/k_B$  is a characteristic temperature and  $Q = N_s^{-2} \sum_m 2r_{nm}^{-6}$  is a geometrical factor. Here,  $N_s$  denotes the number of spins per unit volume. From the crystal structure of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ , we estimate  $N_s = 3.23 \times 10^{21} \text{ Gd}^{3+} \text{ ions/cm}^3$  and  $Q = 18.2$ , yielding  $\tau = 0.12$  K and  $c_{\text{dip}}T^2/R = 0.05 \text{ K}^2$ . Combining crystal-field anisotropy and dipolar contributions gives a total  $c_{\text{cf}}T^2/R + c_{\text{dip}}T^2/R = 0.22 \text{ K}^2$ , in excellent agreement with experiment (Fig. 5, black solid line). These results indicate negligible exchange interactions, supporting that antiferromagnetic ordering originates from dipolar coupling. This behavior closely resembles that observed in other well-known classical salts, such as  $[\text{GdCl}_3] \cdot 6\text{H}_2\text{O}$  and  $[\text{Gd}_2(\text{SO}_4)_3] \cdot 8\text{H}_2\text{O}$ .<sup>17</sup>

External magnetic fields of  $B \geq 1$  T are sufficient to suppress both crystal-field anisotropy and dipolar interactions, allowing the heat capacity to be accurately described by simple paramagnetic Schottky contributions (Fig. 5, colored solid lines). At the highest temperatures, the dominant contribution arises from lattice vibrations, which follow a Debye law that simplifies to  $c_{\text{latt}}/T^3R = 6.3 \times 10^{-4} \text{ K}^{-3}$  below 6 K (Fig. 5, dotted line).

The absolute entropy for different magnetic fields was derived from the heat capacity data using  $S = \int [c_p/T]dT$  (Fig. 6). At zero applied field, the entropy saturates at  $S = R \ln(2s+1) = 2.08R$  for  $s = 7/2$  ions at 2 K, corresponding to  $38.3 \text{ J kg}^{-1} \text{ K}^{-1}$  for  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ . Notably, at the antiferromagnetic transition temperature  $T_N = 0.21$  K, the entropy is approximately  $S \approx R \ln(2) = 0.69R$ , indicating that only the lowest doublet ( $s_z = \pm 7/2$ ) remains populated at the onset of magnetic ordering.

### D. Magnetocaloric effect

The MCE of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  was evaluated using both direct measurements and indirect methods, based on thermodynamic relations.



**FIG. 6.** Entropy  $S$  of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  at selected magnetic fields. The horizontal line marks the entropy expected for a two-level system.

## 1. Direct measurements

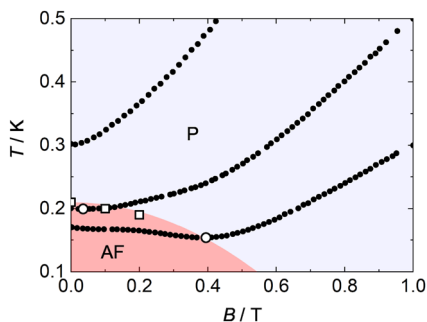
Direct MCE measurements are presented in Fig. 7 for demagnetization processes starting at  $B = 1$  T and bath temperatures of 0.3, 0.5 and 1 K. The plotted temperature traces are not corrected for heat exchange with the thermal bath; however, such heat leakage is negligible under our experimental conditions. At 0.1 K, the sample heat capacity is  $c_{\text{sample}} \approx 10 \mu\text{J K}^{-1}$ , whereas the thermal conductance of the wires connecting the calorimeter platform to the bath is  $G \approx 2 \text{ nW K}^{-1}$ , yielding a thermal time constant  $\tau \approx c_{\text{sample}}/G = 5000$  s. Since the field-change events in the direct MCE measurements last roughly 30 s, i.e., much shorter than  $\tau$ , the sample-platform assembly remains effectively thermally isolated during the sweep. As a result, the measured temperature traces provide an accurate representation of the adiabatic response of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$ .

At the highest magnetic fields and temperatures, the sample cools linearly, as expected for a paramagnet. A plateau is eventually reached as crystal-field anisotropy and dipolar interactions begin to dominate over the Zeeman effect. In addition, anomalies in the form of minima emerge when the material undergoes antiferromagnetic ordering, most prominently during demagnetization from 0.3 K. A minimum temperature of  $T \approx 0.15$  K is experimentally reached at  $B = 0.4$  T at the transition, below which an inverted MCE occurs. As expected, the MCE vanishes once  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  becomes magnetically ordered.

The quasi-adiabatic temperature traces, together with the heat-capacity data, enable construction of the  $B$ – $T$  phase diagram (Fig. 7). Both methods yield fully consistent results for the transition line separating the antiferromagnetic and paramagnetic phases. This boundary is satisfactorily described by the quadratic dependence  $T_N(B) = T_N(0) - \alpha B^2$ , as expected for an antiferromagnet sufficiently far from the critical-field region. Although this quadratic approximation is not expected to remain valid very close to the critical field, our data suggest a critical field of roughly  $B_c \lesssim 1$  T for this material.

## 2. Indirect evaluation

The isothermal magnetic entropy change,  $\Delta S_m$ , was calculated from the entropy curves (Fig. 6) for any magnetic field variation  $\Delta B = B - 0$ . In addition,  $\Delta S_m$  was independently estimated



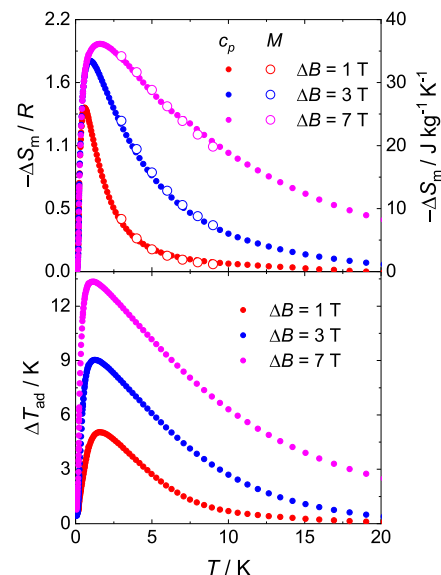
**FIG. 7.** Direct MCE measurements and  $B$ – $T$  phase diagram of  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  in the  $B$ – $T$  plane, showing the boundary between the antiferromagnetic (AF) and paramagnetic (P) phases. Data points were obtained from  $c_p$  measurements (squares) and quasi-adiabatic demagnetization processes (circles) starting at  $B = 1$  T and bath temperatures of 0.3, 0.5, and 1 K.

from the magnetization data (Fig. 3), using the Maxwell relation  $\Delta S_m = \int [\partial M / \partial T] dB$ , yielding nearly identical results (Fig. 8, top panel). The adiabatic temperature change,  $\Delta T_{\text{ad}}$ , associated with full demagnetization, was also evaluated from the entropy data (Fig. 8, bottom panel).

For the largest magnetic field change of  $\Delta B = 7$  T, the maximum isothermal magnetic entropy change reaches  $-\Delta S_m = 36.0 \text{ J kg}^{-1} \text{ K}^{-1}$  at 1.5 K, while the corresponding adiabatic temperature change is as high as  $\Delta T_{\text{ad}} = 13.3$  K at  $T = 1.1$  K. Even for smaller magnetic field changes, the MCE remains substantial. For example, for  $\Delta B = 1$  T, an entropy change of  $-\Delta S_m = 26.1 \text{ J kg}^{-1} \text{ K}^{-1}$  is observed at 0.6 K, corresponding to 68% of the total available magnetic entropy. The associated adiabatic temperature change reaches  $\Delta T_{\text{ad}} = 5.0$  K at  $T = 1.6$  K for the same magnetic field change.

These results clearly outperform many  $\text{Gd}^{3+}$ -based compounds in the sub-Kelvin range. In most cases, competing materials undergo magnetic phase transitions at relatively high temperatures (typically  $\gtrsim 0.5$  K), which drastically reduces the available magnetic entropy and causes the MCE to vanish. Representative examples include  $\text{GdLiF}_4$ ,<sup>11</sup>  $\text{Gd}(\text{HCOO})_3$ ,<sup>12</sup>  $\text{GdPO}_4$ ,<sup>13</sup>  $\text{GdF}_3$ ,<sup>14</sup>  $\text{GdVO}_4$ ,<sup>15</sup> and  $\text{Gd}(\text{OH})\text{F}_2$ ,<sup>16</sup> as well as  $\text{Gd}_3\text{Ga}_5\text{O}_{12}$  (GGG), whose MCE, despite its very low ordering temperature, drops sharply between 1 and 0.8 K due to the onset of short-range correlations.<sup>46</sup>

In contrast,  $[\text{Gd}(\text{NO}_3)_3] \cdot 6\text{H}_2\text{O}$  remains one of the most competitive refrigerants for very low temperatures. Notably, it exhibits the highest reported adiabatic temperature change,  $\Delta T_{\text{ad}}$ , together with the lowest temperature of its corresponding maximum,  $T_{\Delta T}^{\text{max}}$ , for small field changes, such as  $\Delta B = 1$  T, among state-of-the-art sub-Kelvin  $\text{Gd}^{3+}$ -based compounds (Table I). This exceptional performance stems from its extremely low magnetic ordering temperature, combined with a high magnetic density and remarkable lattice rigidity, with the latter reflected in its unusually small lattice heat



**FIG. 8.** Isothermal magnetic entropy change,  $\Delta S_m$  (top), and adiabatic temperature change,  $\Delta T_{\text{ad}}$  (bottom), for selected magnetic field changes, as obtained from heat capacity data (filled symbols) and magnetization data (open symbols).

**TABLE I.** Comparison of Gd<sup>3+</sup>-based magnetocaloric refrigerants for very low temperatures. Reported values include Néel or Curie temperature ( $T_N$  or  $T_C$ ); magnetic entropy change ( $-\Delta S_m$ ) for  $\Delta B = 1$  T; temperature at which  $-\Delta S_m$  is maximum ( $T_{\Delta S}^{\max}$ ); adiabatic temperature change ( $\Delta T_{ad}$ ) for  $\Delta B = 1$  T; temperature at which  $\Delta T_{ad}$  is maximum ( $T_{\Delta T}^{\max}$ ); relative cooling power ( $RCP = |\Delta S_m| \times \delta T_{FWHM}$ , where  $\delta T_{FWHM}$  is the full width at half maximum) for  $\Delta B = 1$  T; and lattice heat capacity parameter ( $c_{latt}/T^3R$ ); literature reference. The units are indicated in parentheses. An ellipsis denotes an unknown value.

Compound	$T_N$ or $T_C$ (K)	$-\Delta S_m$ (J kg <sup>-1</sup> K <sup>-1</sup> )	$T_{\Delta S}^{\max}$ (K)	$\Delta T_{ad}$ (K)	$T_{\Delta T}^{\max}$ (K)	$RCP$ (J kg <sup>-1</sup> )	$c_{latt}/T^3R$ (K <sup>-3</sup> )	References
[GdCl <sub>3</sub> ] · 6H <sub>2</sub> O	0.19	...	...	...	...	...	...	17
[Gd <sub>2</sub> (SO <sub>4</sub> ) <sub>3</sub> ] · 8H <sub>2</sub> O	0.18	...	...	...	...	...	...	17
{Gd <sub>2</sub> }	0.18	27.0	0.5	3.5	1.9	50	$1.0 \times 10^{-3}$	18
{GdW <sub>10</sub> }	0.036	2.3	0.8	...	...	5	$2.0 \times 10^{-3}$	19
{GdW <sub>30</sub> }	<0.01	1.5	0.3	...	...	2	$1.1 \times 10^{-2}$	19
{GdZn}	<0.3	12.3	0.7	3.9	1.8	29	$5.1 \times 10^{-3}$	20
{Gd <sub>7</sub> }	<0.3	11.7	0.9	2.4	2.3	28	$2.0 \times 10^{-2}$	21
Ba <sub>2</sub> GdSbO <sub>6</sub>	<0.4	...	...	...	...	...	$4.8 \times 10^{-6}$	22
Sr <sub>2</sub> GdSbO <sub>6</sub>	<0.4	...	...	...	...	...	$2.2 \times 10^{-6}$	22
KBaGd(BO <sub>3</sub> ) <sub>2</sub>	0.24	14.3	0.5	...	...	20	...	23
{Gd <sub>12</sub> Na <sub>6</sub> }	<0.4	29.3	0.5	4.0	1.8	56	$3.8 \times 10^{-2}$	24
Gd <sub>9,33</sub> [SiO <sub>4</sub> ] <sub>6</sub> O <sub>2</sub>	<0.05	12.7	0.8	2.8	3.0	45	$4.9 \times 10^{-5}$	25
[Gd(NO <sub>3</sub> ) <sub>3</sub> ] · 6H <sub>2</sub> O	0.21	26.1	0.6	5.0	1.6	46	$6.3 \times 10^{-4}$	This work

capacity,  $c_{latt}/T^3R$ . Importantly, achieving large MCE values under small magnetic fields is highly desirable for practical applications, as it simplifies the design and fabrication of ADR's. Lower fields reduce the need for bulky superconducting magnets and complex cryogenic infrastructure, enabling more compact and cost-effective cooling systems.

#### IV. CONCLUSIONS

We have investigated the magnetothermal properties of the classical gadolinium salt [Gd(NO<sub>3</sub>)<sub>3</sub>] · 6H<sub>2</sub>O down to temperatures approaching absolute zero. This compound undergoes an antiferromagnetic phase transition at  $T_N = 0.21$  K, driven by weak dipolar interactions combined with dominant axial crystal-field anisotropy. These characteristics result in a very low operational temperature for [Gd(NO<sub>3</sub>)<sub>3</sub>] · 6H<sub>2</sub>O, which, together with its relatively high magnetic density and lattice stiffness, produces a remarkable magnetocaloric effect at very low temperatures.

#### ACKNOWLEDGMENTS

We thank Jesús I. Martínez for his assistance with the EPR experiments and acknowledge the Servicio General de Apoyo a la Investigación of Universidad de Zaragoza for technical support. This work was funded by EU (MSCA-DN MolCal, 101119865), MICIU/AEI/10.13039/501100011033/, and ERDF/EU (PID2024-159457OB-C21, CEX2023-001286-S).

#### AUTHOR DECLARATIONS

##### Conflict of Interest

The authors have no conflicts to disclose.

#### Author Contributions

**David Gracia:** Data curation (lead); Investigation (equal); Methodology (equal); Writing – original draft (lead); Writing – review & editing (equal). **Marc Ubach I Cervera:** Data curation (supporting); Investigation (equal); Methodology (equal); Writing – review & editing (equal). **Emmanouil K. Charkiolakis:** Data curation (supporting); Investigation (equal); Methodology (equal); Writing – review & editing (equal). **Inés García-Rubio:** Investigation (equal); Methodology (equal); Writing – review & editing (equal). **Constantinos J. Milios:** Investigation (equal); Methodology (equal); Writing – review & editing (equal). **Marco Evangelisti:** Conceptualization (lead); Data curation (supporting); Funding acquisition (lead); Investigation (equal); Methodology (equal); Supervision (lead); Writing – original draft (supporting); Writing – review & editing (equal).

#### DATA AVAILABILITY

All data presented in this article can be retrieved at <https://doi.org/10.20350/digitalCSIC/17747>.

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