

# 1 Analysis of thermal resistance evolution of ash deposits during co-firing of 2 coal with biomass and coal mine waste residues

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## 6 **Abstract**

7 Co-firing biomass or waste fuels with coal in conventional thermal plants is a promising way to reduce  
8 environmental impact of human activities with an acceptable economic investment. One of the main  
9 issues to be addressed is the worsening in ash fouling and the reduction of heat transfer rate. In the  
10 present paper, the deposits thermal resistance during direct combustion of different blends of coal  
11 and various native fuels is investigated by using a deposition probe, kept at 550 °C in order to emulate  
12 the conditions of superheaters of conventional power units. Two energy crops (*Cynara cardunculus*  
13 *L.* and *Populus spp.*), a forest residue (*Pinus pinaster*) and a waste coal (coal mine waste residues)  
14 were successfully tested in a semi-industrial scale pilot plant.

15 A thermal model of the probe is presented to estimate heat transfer rate and thermal resistance  
16 of ash deposits. After the validation with experimental data, a sensitivity analysis allows to identify  
17 the deposit surface emissivity and the flue gas temperature as the most influential parameters. The  
18 heat uptake in air flow decreases with time for all the experimental tests in spite of the increase  
19 in flue gas and walls temperatures. Except for poplar blends, under similar operation conditions, a  
20 rise in the substitution percentage means faster decreasing rates in heat transfer and higher thermal  
21 resistance due to the ash deposits, especially for cynara and coal mine waste residues.

The present work demonstrates the usefulness of thermal models to estimate the thermal resis-  
tance of ash deposits without the need of sophisticated instrumentation. Dedicated thermal models,  
similar to the developed one, could serve to design smart cleaning sequences to improve efficiency in  
power generation processes.

22 *Keywords:* Thermal resistance, Biomass co-firing, Coal mine waste residues, Superheater fouling,  
23 Deposition probe

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## 24 **1. Introduction**

25 Promoted by diverse international energy policies, biomass and other low-cost fuels, as coal mine  
26 waste residues, emerge as promising native resources, which can be co-fired with coal in existing  
27 power plants to reduce external energy dependency and environmental impacts.

28 Biomass, considered a renewable and CO<sub>2</sub>-neutral resource, continues to attract great attention  
29 because of the priority to reduce greenhouse and pollutant emissions (1; 2; 3). In 2009, the IEA  
30 Bioenergy Implementing Agreement identified globally some 150 power plants using coal along with  
31 biomass, mainly located in northern Europe and in the United States, and it is expected an important  
32 increase in the next decade (4).

33 Coal mine waste residue (CMR) is a much less conventional fuel coming from low-energy-value  
34 discards of the coal mining industry. Usually, coal mine waste residues pile accumulated near the  
35 original mines as a potential source of environmental pollution. There exists around 30 coal mine  
36 waste residues burning power plants in the United States, all of them based on Circulating Fluidized  
37 Bed technology (5). However, as the 90% of thermal power stations in the world are based on  
38 pulverized fuel burners, research on co-firing of CMR under such technology is very desirable.

39 Ash deposition on heat transfer surfaces during combustion brings about significant losses of  
40 efficiency in large solid-fired boilers (6; 7), long-term corrosion and even boiler shut-down (1; 8; 9).  
41 These problems become more critical for biomass and coal mine waste residues, as the former usually  
42 have high concentrations of alkali metals, sulfur and chlorine (10), and the later might be constituted  
43 by a 50% of ash matter, including iron, manganese or sulfur.

44 A lot of research has been done aiming at the modelling of deposits growth from different ap-  
45 proaches: definition of slagging indices (11; 12; 13), direct simulation by Montecarlo method (14), or  
46 CFD models (15; 16; 17; 18; 19; 20; 21). This kind of models results of great interest to understand  
47 the relative importance of the processes involved in ash deposition, to have an insight of the slagging  
48 potential of new fuels and to optimize the design of boilers and heat transfer exchangers. Neverthe-  
49 less, such models involve many empirical parameters that introduce important uncertainties which  
50 limit the accuracy of predictions in actual power boilers.

51 Ash deposition strongly depends on the nature of the coal mineral matter, but also on particle  
52 size and shape (15; 22) and working temperatures (23; 24; 25). Those parameters are crucial for  
53 growth rate, sintering processes and microstructure of deposits (24; 26). Therefore, they determine  
54 the thermal properties of the formed deposits, namely thermal conductivity and emissivity (6; 26; 27;  
55 28; 29; 30), which are essential in heat transfer processes. However, experimental results on deposit

## Nomenclature

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### Abbreviations

SAC	South African Coal
CYN	<i>Cynara Cardunculus</i>
PWO	Pine Wood Chips
POP	<i>Poplar Populus ssp.</i>
CMR	Coal Mine (Waste) Residues
w.b.	wet basis
d.b.	dry basis

SCADA Supervisory Control and Data Acquisition

HHV High Heating Value

### Geometrical parameters

$D$	diameter (m)
$A$	area (m <sup>2</sup> )
$r$	radius (m)
$x$	length of a section (m)

### Radiative model

$\epsilon$	emissivity
$\alpha$	absorptivity
$R_k$	resistance by emission of k (m <sup>-2</sup> )
$R_{kl}$	resistance between k and l (m <sup>-2</sup> )
$R_{kk}$	equivalent resistance for k (m <sup>-2</sup> )
$J$	node radiosity (W/m <sup>2</sup> )

### Thermal model

$T$	temperature (K)
$c_p$	specific heat capacity (J/kg-K)
$h$	convection coefficient (W/m <sup>2</sup> -K)
$\dot{m}$	cooling air mass flow (kg/s)
$R'_t$	thermal resistance per unit length (m-K/W)
$\dot{Q}$	heat transfer rate (W)

### Subscripts

$ch$	combustion chamber
$dep$	deposit
0	inner surface of inner duct
1	outer surface of inner duct
2	inner surface of outer duct
3	inner surface of inner duct
$j$	control volume j of deposition probe
$cw$	$H_2O/CO_2$ mixture
$s$	deposit surface
$w$	water wall
$g$	flue gases
$air$	cooling air
$a$	air flux in the annulus
$i$	internal air flux
$k, l, m$	referred to $s, w, g$

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56 thermal properties are quite scarce, very dependent on fuel blends and usually require specific and  
 57 complex instrumentation (24; 31; 32; 33; 34).

58 In spite of the great interest of these research works, the complexity of the required measurement

59 equipment and the involved mathematical methods could jeopardize its practical usefulness for on-  
60 line monitoring or control systems under actual conditions. With this goal in mind, it is necessary  
61 to develop simplified models based on usually available plant data (35; 36).

62 The present paper is focused on co-firing of different fuel blends in a semi-industrial scale pilot  
63 plant provided with an air-cooled deposition probe. The objectives of the work are threefold: (i) to  
64 present experimental results about successful co-firing of coal mine waste residues in a pulverized fuel  
65 burner for the first time in the literature; (ii) to estimate the deposits thermal resistance through the  
66 development of a thermal model, as a quantitative parameter to be used in eventual soot-blowing  
67 strategies (iii) to compare the thermal resistance evolution for different blends of biomass and coal  
68 mine waste residues.

69 The main novelties of the work, besides the use of CMR as fuel, are the improvement of the  
70 radiation model with respect to previous papers (35; 36), considering two sink surfaces and a gaseous  
71 source, and the simplified modelling approach with few data available in actual power boilers.

72 The experimental facility and the tests program is presented in Section 2. The thermal model to  
73 estimate fouling thermal resistances is detailed and validated in Section 3. The main results of the  
74 work are gathered in Section 4: experimental data acquired during co-firing tests, a sensitivity analysis  
75 to identify the main influential parameters on predicted thermal resistances and the comparison of  
76 results for different fuel blends.

## 77 **2. Experimental methodology**

### 78 *2.1. Combustion pilot plant*

79 The experimental facility consists of a 500 kW<sub>th</sub> swirl burner for pulverized fuel, placed downward  
80 on top of a cylindrical chamber 3 m long and 1 m of internal diameter (Figure 1). The combustion  
81 chamber comprises six water-cooled rings, being the three in the upper part coated with refractory  
82 concrete to promote flame stability. The swirl burner includes an ignitor of natural gas of 35 kW<sub>th</sub>  
83 and two concentric entries of primary air-fuel and secondary air streams. Swirl is imposed by a  
84 tangential scroll to the primary air while the secondary air crosses an externally controlled system  
85 of radial vanes, located on the bottom of a wind box. An air-cooled cross-flow heat exchanger of  
86 47 tubes is placed at the middle of the combustion chamber in order to investigate corrosion and  
87 degradation.

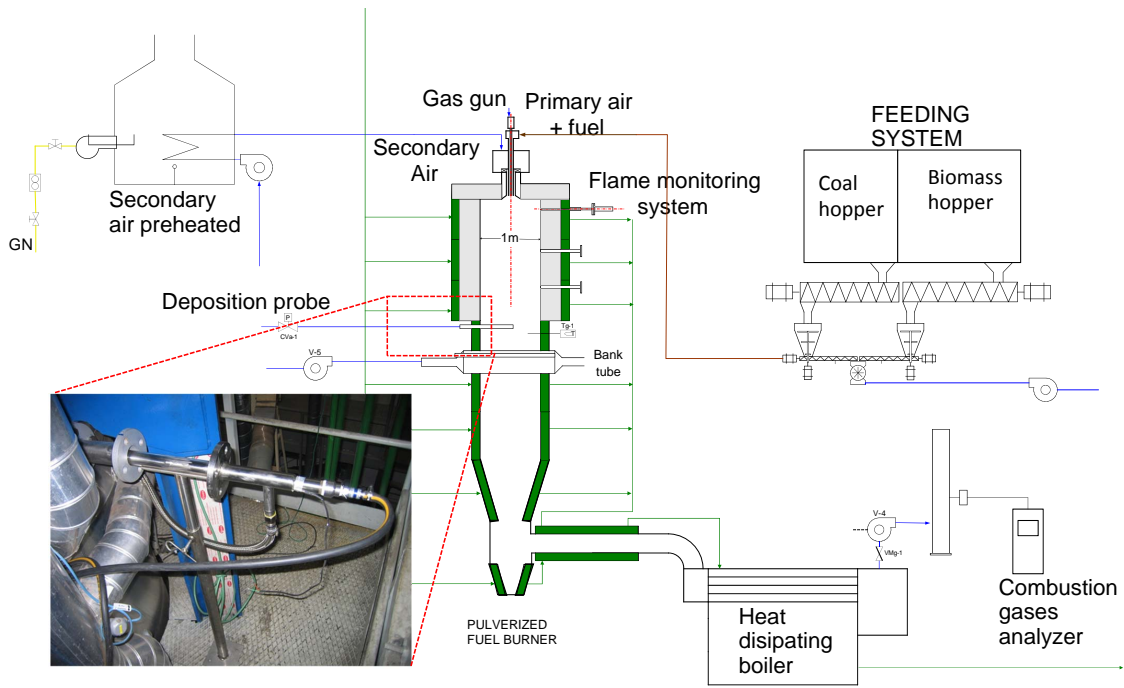


Figure 1: Arrangement of the combustion test facility and deposition probe location.

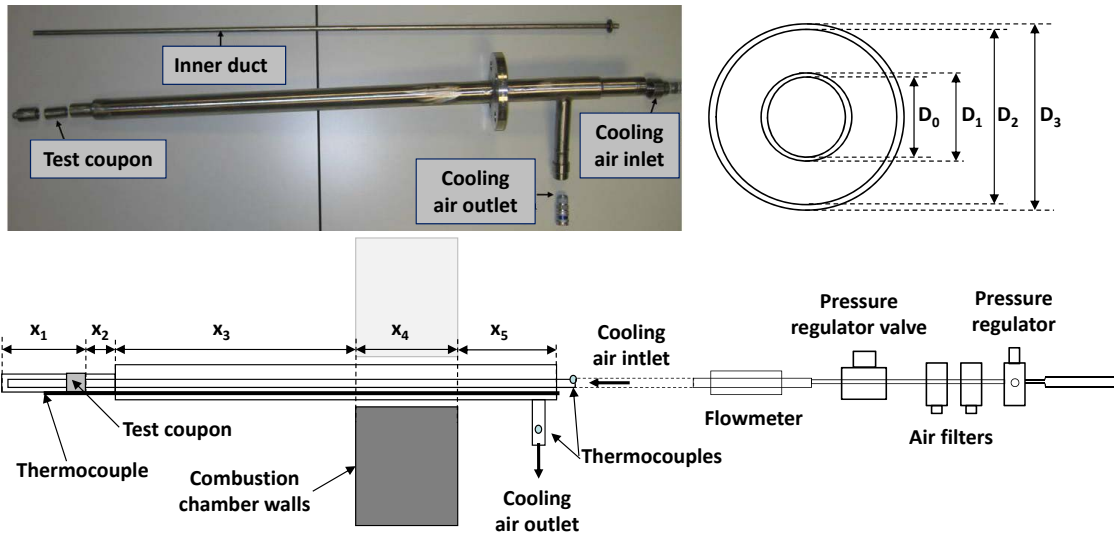


Figure 2: Layout of the deposition probe.

Table 1: Characterization of fuels. The oxygen concentration has been calculated by difference.

		SAC	POP	CYN	PWO	CMR
Moisture (% w.b.)		3,6	8,2	10,9	8,57	16,81
Proximate analysis (% d.b.)	ash	13,4	3,2	8,9	1,7	55,5
	volatile matter	26,0	82,6	77,0	79,9	28,9
	fixed carbon	60,6	14,2	14,1	18,5	15,6
Ultimate analysis (% d.b.)	C	69,6	45,7	46,3	49,5	23,1
	H	4,0	5,8	4,9	4,9	1,1
	N	2,1	0,2	1,1	0,5	0,6
	S	0,5	0,0	0,1	0,1	3,2
	O	10,5	45,0	38,7	43,4	16,5
HHV (kJ/kg d.b)		27800	17190	19320	19590	7382
Max. particle size ( $\mu\text{m}$ )		100	500	500	500	100
Median or $d_{50}$ ( $\mu\text{m}$ )		44,6	201,0	204,6	205,7	24,4

88 Thermocouples measure water temperatures at inlet and outlet of each water ring, air tempera-  
89 ture at inlet and outlet of tube bank, temperature of 12 points into the refractory walls, and flue gas  
90 temperature just below the refractory rings inside the furnace. Different flow meters register the flow  
91 rate of the cooling water and the air flow of primary, secondary and tube bank cooling streams. Con-  
92 centration of main species present in flue gases ( $CO$ ,  $CO_2$ ,  $O_2$ ,  $SO_2$ ,  $NO$ ) is continuously measured  
93 with a complete set of standard analyzers. An advanced SCADA system (Supervisory Control and  
94 Data Acquisition) provides the on-line control, visualization and recording of operation parameters  
95 and emissions. Further details of the experimental facility can be found in (37; 38; 39).

96 Finally, a visualization system based in a CCD camera (charged coupled device) is used to monitor  
97 continuously the flame and to acquire videos when it is needed. The CCD camera inside a protective  
98 probe is installed at the first refractory ring of the combustion chamber in order to register the root  
99 of the flame. Details of the equipment and analysis procedure can be found in Ref. (40). The flame

100 videos will be useful in the present work to identify anomalous combustion states and to interpret  
101 the experimental observations.

## 102 2.2. Deposition probe

103 A deposition probe inserted in the combustion chamber was used to investigate ash deposits formation  
104 during the combustion of different fuel blends (37; 41). The surface probe is kept at a constant  
105 temperature of  $550\pm 5$  °C to reproduce the typical operating temperatures of superheaters of thermal  
106 power units. It is inserted in a spyhole located at 1.7 m from the burner throat, just above the  
107 cross-flow heat exchanger.

108 The probe is cooled by pressurized air which flows inside two stainless-steel concentric pipes.  
109 Air enters into the inner duct at ambient temperature coming from a compressor and returns by  
110 the external annular pipe. Figure 2 gathers the geometrical parameters of the probe, including the  
111 nomenclature used in the following sections. The external diameter ( $D_3$ ) is 40 mm and the total  
112 length inside the combustion chamber 515 mm.

113 The deposition probe is instrumented with an air-flow meter for the inlet of cooling air and three  
114 thermocouples for the measurement of the outer surface temperature near the test coupon and the  
115 inlet and the outlet cooling air temperatures. The surface temperature is adjusted by a control loop  
116 programmed in a PLC (Programmable Logic Controller) by adjusting the cooling air flow rate with  
117 an automatic control valve (42).

## 118 2.3. Fuel blends

119 Experimental tests were performed with different blends of bituminous South African coal (SAC)  
120 and several native solid fuels: three biomasses (*Cynara cardunculus L.*-CYN, *Populus spp.*-POP and  
121 *Pinus pinaster*-PWO) and coal mine waste residues (CMR) of very low heating value (HHV). Pre-  
122 processing of samples and characterization analyses agree international normative and details can be  
123 found in previous works (41). The main characteristics of the tested fuels are summarized in Table 1.

124 With respect to biomasses, PWO and CYN have similar heating values, slightly higher than POP.  
125 Moisture and specially ashes are higher for CYN, while volatile matter, which favors ignition, is lower  
126 than that of POP and PWO. Some previous works studied the ash composition with SEM/EDS  
127 (Energy Dispersive X-ray Spectroscopy) and ICP-OES (Inductive Coupled Plasma-Optical Emission  
128 Spectroscopy) techniques (41).

129 Regarding CMR, it has to be noted its very low heating value, the high ash content and the low  
130 content on carbon and hydrogen. Given the intrinsic difficulties related to coal mine waste residues

Table 2: Operation parameters during experimental tests during co-firing of SAC and CYN, PWO, POP or CMR. (\*) Measurement of flue gas by a thermocouple before correction.

Test Code	1	2	3	4	5
% substitution	0%	5% CYN	10% CYN	15% CYN	10% PWO
Coal mass flow rate (kg/h)	68.4	65.0	61.6	58.2	61.6
Biomass mass flow rate (kg/h)	0	6.2	12.3	18.5	10.2
Primary / Secondary air	0.30	0.29	0.32	0.32	0.34
Excess of air (%)	19	25	20	19	13
Mean flue gas temperature* (°C)	940	970	920	935	947
Refractory wall temperature (°C)	445	465	413	481	475

Test Code	6	7	8	9	10
% substitution	10% CYN	10% POP	15% POP	10% CMR	20% CMR
Coal mass flow rate (kg/h)	61.6	61.6	58.17	61.8	54.9
Secondary fuel mass flow (kg/h)	11.2	11.3	16.9	27.2	54.3
Primary / Secondary air	0.35	0.34	0.36	0.33	0.41
Excess of air (%)	11	11	11	34	40
Mean flue gas temperature* (°C)	961	962	985	1011	1059
Refractory wall temperature (°C)	587	585	707	455	642

131 combustion, no previous works were found by the authors in the literature and new research must  
 132 be done.

133 *2.4. Test series*

134 Experimental tests were performed in several series, whose details are gathered in Table 2, includ-  
 135 ing percentages of fuels in energy basis, mean mass flows and mean temperature of flue gases and  
 136 refractory walls.

137 It has to be noticed that the thermal inertia of a semi-industrial scale combustion facility involves  
 138 a very slow transient period, in which the time evolution of thermal variables, such as temperatures,  
 139 depends on many factors, including ambient temperature (variable) or fuel properties (heterogeneous



140 blends). The use of this kind of facilities is a challenge to be assumed if representative results of  
141 actual boilers are wanted.

142 According to the data of Tables 1-2, the percentage of moisture is higher for blends (tests 2-8)  
143 than for 100%SAC (test 1). Specifically, the increase with regard to coal combustion ranges from  
144 15% to 50% in biomass co-firing tests. As for ash content, it decreases with regard to test 1 for  
145 biomass co-firing from a 3.4% in test 2, to a 17% in test 8. The most relevant changes occur when  
146 coal mine waste residues are introduced: moisture undergoes an increase of 100% and 170% and ash  
147 content of 90% and 136% for tests 9 and 10, respectively.

148 In the table, flue gas temperature is measured inside the combustion chamber, near the deposition  
149 probe, by means of a thermocouple (see location in Figure 1). Before to be used in the thermal model,  
150 the measurement is corrected of convection and radiation effects, according to the method of Cox  
151 and Chitty reported in Ref. (43). With respect to the refractory wall, the referenced temperature is  
152 the mean value inside the first refractory ring, near the throat.

### 153 **3. Thermal model**

#### 154 *3.1. Initial considerations*

155 The main parts of the deposition probe ( $x_1$ - $x_3$  in Figure 2) were discretized in eight control volumes in  
156 order to obtain an appropriate compromise between computation time and accuracy of the solution.  
157 The section  $x_3$  includes volumes 1-4 , section  $x_2$  volumes 5-7 and the section  $x_1$  constitutes the eighth  
158 volume. Additionally, a simplified model was developed for sections  $x_4 - x_5$  to estimate the actual  
159 temperatures of cooling air arriving and leaving the combustion chamber.

160 Heat transfer coefficients by convection inside the probe were calculated according to the Gnielin-  
161 ski correlation, including corrections for entry effects (44) and Stephan correction for the annular  
162 duct (45). The convection coefficient over the outer surface of the probe due to the combustion gases  
163 was estimated according to the Churchill and Bernstein correlation (44).

164 Emissivity and absorptivity of flue gases were estimated from the Hottel's model (44; 46), con-  
165 sidering the approach of gray gas for each component of a mixture of water, carbon dioxide and  
166 non-participating gases. The partial pressure for each gas was calculated from the mass balance un-  
167 der complete combustion conditions. In order to carry out the presence of soot particles, a corrective  
168 factor is applied (47):

$$\epsilon = 1 - (1 - \epsilon_{cw}) \exp(-K C_s D_{ch} T_g) \quad (1)$$

169 where  $K$  is a dimensional constant ( $1.5 \cdot 10^{-3} \text{ m}^2/\text{g K}$ ),  $C_s$  is the particle concentration ( $\text{g}/\text{m}^3$ ),  $D_{ch}$   
 170 is the inner diameter of the combustion chamber (m) and  $\epsilon_{cw}$  is the emissivity before correction.

171 Values for the properties used in the thermal model are gathered in Table 3. Emissivity of the  
 172 different radiative surfaces has been considered near to unity (29), while typical values of thermal  
 173 conductivity for the stainless-steel ducts (44) and of the particle concentration factor (47) have been  
 174 considered. Given the uncertainty in those values, a sensitivity analysis is performed in Section 4 in  
 175 order to evaluate the influence of these estimated properties and the order of magnitude of deviations  
 176 in subsequent calculations.

Table 3: Values of some properties used in the thermal model.

Thermal property	Symbol	Value
Ducts conductivity (W/m-K)	$\kappa_{tube}$	20
Thermocouple emissivity	$\epsilon_{th}$	0.8
Emissivity of surfaces 1/2	$\epsilon_{1/2}$	0.9
Emissivity of outer surface	$\epsilon_s$	0.9
Emissivity of water walls	$\epsilon_w$	1
Particle concentration ( $\text{g}/\text{m}^3$ )	$C_s$	0.6

### 177 3.2. Radiative exchange model

178 Conventional models usually simulate the radiative exchange between a single surface and the  
 179 flame (35). However, given the proximity of water cooling walls to the deposition probe, a bet-  
 180 ter approach is here considered with two sink surfaces and a gaseous source, according to the delta  
 181 radiation network of Figure 3 (48). The magnitudes referred to probe, wall and gases are denoted  
 182 with the subscripts  $s$ ,  $w$  and  $g$ , respectively. According to the actual geometry, the resistances are:

$$R_k = \frac{1 - \epsilon_k}{\epsilon_k A_k} \quad k = w, s \quad (2)$$

$$R_{kg} = \frac{1}{A_k \epsilon_{gk}} \quad k = w, s \quad (3)$$

$$R_{sw} = \frac{1}{A_s F_{sw} (1 - \epsilon_{gsw})} \quad (4)$$

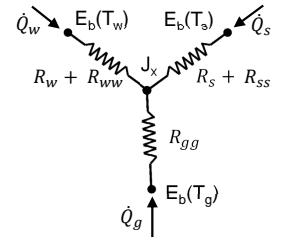
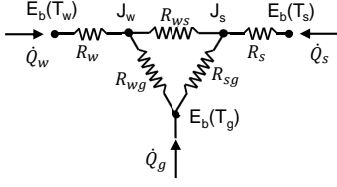


Figure 3: Delta-wye transformation for a model of two surfaces and a gaseous source.

183 where the view factors  $F_{wg}$  and  $F_{sg}$  are considered near to the unity and  $F_{sw} = 0.9$  was calculated  
 184 from the actual geometry. The heat fluxes are:

$$\dot{Q}_{sw} = \frac{J_s - J_x}{R_{sw}}, \quad \dot{Q}_{gk} = \frac{\sigma T_g^4 - J_k}{R_{kg}} \quad k = w, s$$

185 Following the delta-wye transformation, each leg of the wye consists of the surface resistance in  
 186 series with the resistance found from the transformation:

$$R_{kk} = \frac{R_{kl}R_{km}}{R_{kl} + R_{lm} + R_{km}} \quad k, l, m = w, s, g \quad (5)$$

187 being  $\delta_{kl} = \delta_{lm} = \delta_{km} = 0$ . The corresponding heat fluxes, which will be used in the following section,  
 188 are given by the following relations:

$$\dot{Q}_k = \frac{\sigma T_k^4 - J_x}{R_k + R_{kk}} = \frac{\sigma T_k^4 - J_k}{R_k} \quad k = s, w \quad (6)$$

$$\dot{Q}_g = \frac{\sigma T_g^4 - J_x}{R_{gg}} \quad (7)$$

189 where radiosities ( $J_k$ ) are obtained from the energy balance at the central node.

### 190 3.3. Energy balances

191 The model input data, registered during the experimental tests, are combustion and cooling air flow  
 192 rates, fuel flow rates, flue gas temperature ( $T_g$ ) and temperature of inlet and outlet of cooling air.  
 193 The main outputs are the heat absorbed by the cooling air, deposit surface temperature ( $T_d$ ), probe  
 194 surfaces temperatures ( $T_{0-3}$ ), temperature profile of cooling air across the probe and deposit thermal  
 195 resistance.

196 Mass and energy balances are applied to each control volume considering quasi-steady regimen.  
 197 Given the very small thickness of tube walls, longitudinal heat transfer by conduction through the  
 198 ducts is considered negligible.

199 The energy balance in the deposit surface for control volume  $j$ -th is:

$$\begin{aligned}\dot{Q}_{1,j} &= -\dot{Q}_{s,j} + h_{g,j} A_{dep,j} (T_g - T_{d,j}) \\ &= \frac{x_j (T_{d,j} - T_{3,j})}{R'_{t,dep}}\end{aligned}\quad (8)$$

200 where  $\dot{Q}_{s,j}$  is the absorbed heat flux by radiation from gases and wall given by Eq. (6),  $h_{g,j}$  is the  
201 estimated coefficient of heat transfer by convection over the deposit,  $T_{d,j}$  is the temperature in the  
202 external surface of the deposit given by  $A_{dep,j}$  and the thermal resistance per unit length due to ash  
203 deposition is denoted by  $R'_{t,dep}$ .

204 For the surfaces 3 and 2 (Figure 2), corresponding to the outer and inner sides of the outer tube  
205 of the probe, the energy balances are:

$$\begin{aligned}\dot{Q}_{1,j} &= \frac{2\pi \kappa_{tube} x_j (T_{3,j} - T_{2,j})}{\ln(r_{3,j}/r_{2,j})} \\ &= A_{1,j} \sigma \epsilon_{t,j} (T_{2,j}^4 - T_{1,j}^4) + h_{a,j} A_{2,j} (T_{2,j} - \bar{T}_{a,j})\end{aligned}\quad (9)$$

206 where  $T_{2,j}$  and  $T_{3,j}$  denote the temperature of volume  $j$  in the surfaces 2 and 3,  $\bar{T}_{a,j}$  is the mean bulk  
207 temperature of the cooling air inside the annulus and  $\epsilon_{t,j}$  is the equivalent emissivity from surface 2  
208 to surface 1, which are coaxial cylinders:

$$\epsilon_{t,j} = \left( \frac{1}{\epsilon_1} + \frac{1 - \epsilon_2}{\epsilon_2} \frac{A_{1,j}}{A_{2,j}} \right)^{-1}\quad (10)$$

209 Being air a non-participating medium, the energy balance for the air in the annular duct of the  
210 volume  $j$ -th:

$$\begin{aligned}h_{a,j} A_{2,j} (T_{2,j} - \bar{T}_{a,j}) &= h_{a,j} A_{1,j} (\bar{T}_{a,j} - T_{1,j}) + \\ &+ \dot{m}_{air} c p_{a,j}^{air} (T_{a,j-1}^{air} - T_{a,j}^{air})\end{aligned}\quad (11)$$

211 where  $c p_{a,j}^{air}$  is the specific heat capacity at temperature  $\bar{T}_{a,j}$ , and  $T_{a,j-1}^{air}$  and  $T_{a,j}^{air}$  are the air temper-  
212 atures at exit and entry of volume  $j$ -th, respectively, inside the annulus .

213 The energy balances in surfaces 1 and 0 of inner tube are:

$$\begin{aligned}\dot{Q}_{2,j} &= \frac{2\pi \kappa_{tube} x_j (T_{1,j} - T_{0,j})}{\ln(r_{1,j}/r_{0,j})} \\ &= A_{1,j} \sigma \epsilon_{t,j} (T_{2,j}^4 - T_{1,j}^4) + h_{a,j} A_{1,j} (\bar{T}_{a,j} - T_{1,j}) \\ &= h_{i,j} A_{0,j} (T_{0,j} - \bar{T}_{i,j}) \\ &= \dot{m}_{air} c p_{i,j}^{air} (T_{i,j}^{air} - T_{i,j-1}^{air})\end{aligned}\quad (12)$$

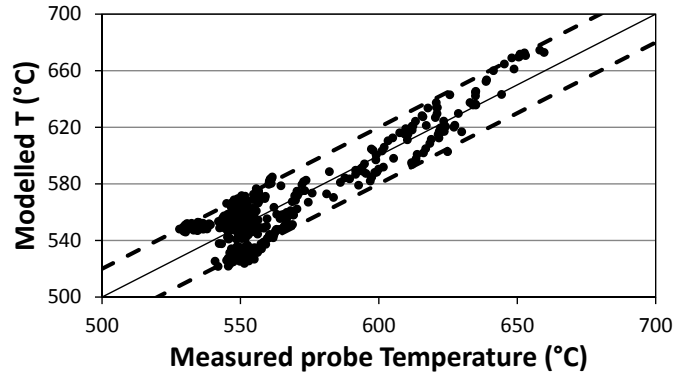


Figure 4: Predicted temperature vs. measured temperature of probe surface at the point indicated in Figure 2 during the tests 1-10. The full line represents zero error, while dashed lines indicates deviations of  $\pm 20^\circ\text{C}$ .

214 where  $cp_{i,j}^{air}$  is the specific heat capacity at temperature  $\bar{T}_{i,j}$ ,  $T_{1,j}$  and  $T_{0,j}$  are surface temperatures of  
 215 inner duct and  $T_{i,j}^{air}$  and  $T_{i,j-1}^{air}$  are the air temperatures at exit and entry of volume  $j$ -th, respectively,  
 216 inside the inner tube.

217 Finally, the heat uptake is given by:

$$\begin{aligned}
 \dot{Q} &= - \sum_j \dot{Q}_{s,j} = \dot{m}_{air} \sum_j cp_{i,j}^{air} (T_{i,j}^{air} - T_{i,j-1}^{air}) \\
 &+ \dot{m}_{air} \sum_j cp_{a,j}^{air} (T_{a,j-1}^{air} - T_{a,j}^{air})
 \end{aligned} \tag{13}$$

### 218 3.4. Validation of thermal model

219 Before the application of the thermal model to compare the thermal resistances, a validation has  
 220 been carried out with the available experimental data. The probe surface temperature was measured  
 221 with a thermocouple during combustion tests (see the position in Figure 2) and compared with the  
 222 output of the model.

223 Validation data have been selected following two criteria. On the one hand, stable regimen is  
 224 required as it is a premise for the validity of balance equations considered in the thermal model.  
 225 Accordingly, the transient period at the beginning of the tests has been discarded. On the other  
 226 hand, high temperature in the refractory wall is desirable, as the radiative exchange model considers  
 227 thermal equilibrium between flame and refractory wall.

228 Under such conditions, maximum deviations of around  $20^\circ\text{C}$  are obtained when the measurement  
 229 is compared to the calculated temperature with the model at the same point. Figure 4 represents  
 230 the predicted value of the probe surface temperature vs. the measured value for all the tests with  
 231 an error range of  $\pm 20^\circ\text{C}$ . It has to be noticed that predictions are in that range even during some

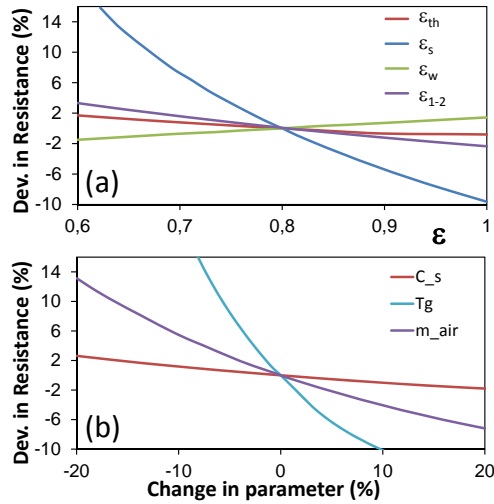


Figure 5: Deviation in thermal resistance of ash deposits under changes in certain parameters.

232 periods for which surface temperature is far from the set point (550 °C).

233 The small observed deviations could be due both to the inherent thermocouple errors, to some  
 234 influential variables in the thermal model, as fouling on chamber walls, ambient temperature or  
 235 cooling water temperature, which cannot be controlled, or to some assumptions in the thermal  
 236 model, such as negligible longitudinal heat transfer in the outer pipe.

## 237 4. Results and discussion

238 This section gathers the main results of the work, with a practical focus. Firstly, a sensitivity  
 239 analysis is performed to identify the more influential parameters which might be known or measured  
 240 to reach accurate enough predictions of thermal resistance. Secondly, heat transfer and thermal  
 241 resistance are compared for the different co-firing tests. Finally, a realistic discussion about the  
 242 usefulness and the possibility of thickness prediction is carried out.

### 243 4.1. Influential parameters

244 A sensitivity analysis was performed to quantify the dependency of final predictions on variations in  
 245 certain magnitudes: unknown properties used in the thermal model and operational parameters.

246 From such analysis, it has been demonstrated that thermal conductivity of pipes, cooling air  
 247 pressure and total combustion air mass flow produce variations in thermal resistance of ash deposits  
 248 less than 1% under changes of a 30% in the parameter value.

249 The effect of changing emissivities of different surfaces from 0.6 to 1 is shown in Figure 5a.  
 250 Deviations below 3% are obtained for thermocouple surface emissivity ( $\epsilon_{th}$ ), wall surface emissivity

251  $(\epsilon_w)$  and emissivities of tube ducts ( $\epsilon_1$  and  $\epsilon_2$ ).

252 On the contrary, emissivity of ash deposit surface ( $\epsilon_s$ ) is a very influential parameter with devi-  
253 ations of 15% on thermal resistance. Therefore, experimental measurements should be performed to  
254 achieve accurate predictions. In the present work, it is an unknown parameter which has been esti-  
255 mated from the literature. As the sintering process has little contribution in the present tests (41),  
256 a typical value of 0.9 was considered for  $\epsilon_s$  (29).

257 The influence of cooling air mass flow is shown in Figure 5b. Typical fluctuations during stable  
258 operation are below 5%, resulting in variations of 4% in thermal resistance of ash deposit. In principle,  
259 the registration of  $\dot{m}_{air}$  would be avoided, considering a mean value for the simulations. Nevertheless,  
260 under actual conditions with continuous load changes, the registration of this parameter is required.

261 As for flue gas temperature, the sensibility analysis demonstrates that is the most important  
262 parameter. Measurement errors of 10% produce deviations above 15% in thermal resistance of ash  
263 deposits. Therefore, an accurate equipment should be desirable to measure flue gas temperature  
264 inside the combustion chamber.

265 Finally, variations of a 20% on particle concentration ( $C_s$ ) produce deviations below 3% on thermal  
266 resistance. The measure of this parameter is quite difficult in actual facilities, but the error is  
267 acceptable, given the uncertainties in more influential parameters as  $\epsilon_s$  or  $T_g$ .

#### 268 4.2. Heat transfer and thermal resistance

269 Nowadays, thermal power plants usually work at variable partial loads, following the instantaneous  
270 electrical demand. Therefore, the sole heat transfer study is not enough to decide when a cleaning  
271 sequence must be activated. On the contrary, thermal resistance is the key parameter to this end  
272 because it provides a quantitative measure of actual fouling and its effect on heat uptake rate.

273 This section gathers the comparative analysis for the time evolution of heat transfer and thermal  
274 resistance, for different fuel blend composition. Flue gas temperature along each experimental tests  
275 is also shown in Figure 6 with the same colour code to facilitate the correct interpretation of results.

276 Subsequent figures represent the instantaneous rate of heat transfer rate related to the initial  
277 value ( $Q(t)/Q(0)$ ) and the thermal resistance of ash deposits ( $R'_{t,dep}$  in  $mK/W$ ). The general trend  
278 in all cases is a decrease of heat uptake ratio, coherent with an increase of thermal resistance under  
279 increasing flue gas temperatures. However instantaneous increases in heat transfer, associated to fast  
280 decrease of thermal resistance, are also observed in many cases. This phenomenon could be caused  
281 by spontaneous ash sheddings, as occurs in actual heat exchangers (35; 36).

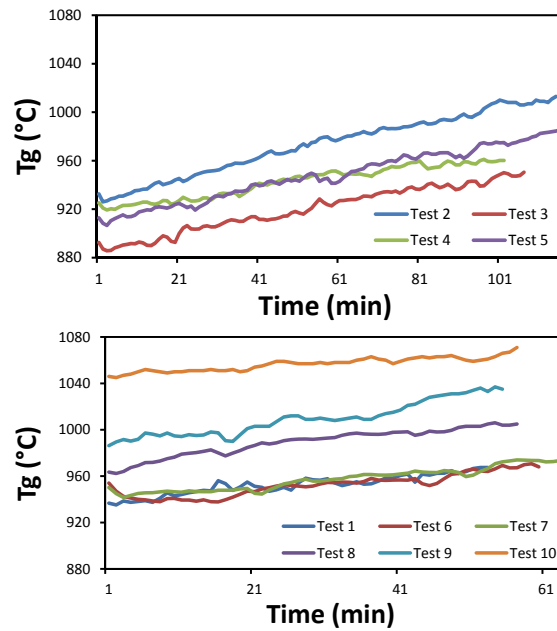


Figure 6: Flue gas temperature registered during experimental tests.

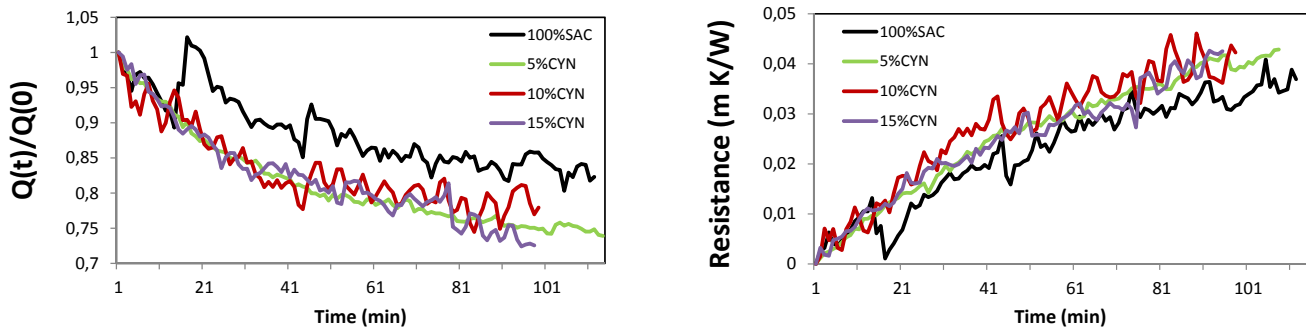


Figure 7: Time evolution of heat uptake ratio (left) and deposit thermal resistance (right) for tests 1-4.

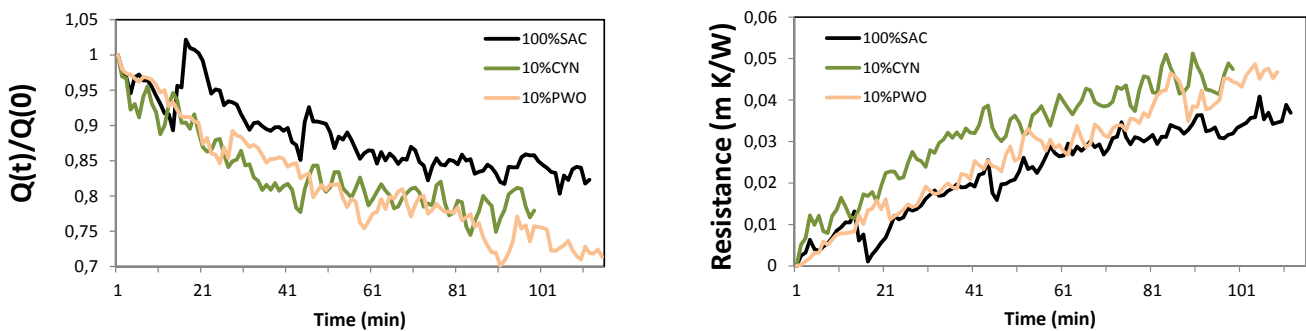


Figure 8: Time evolution of heat uptake ratio (left) and deposit thermal resistance (right) for tests 1, 3 and 5.

282 Figure 7 compares such variables for tests 1-4, performed under different percentages of CYN. As  
 283 it could be expected, the fouling rate and the decrease of heat transfer rate are slower for 100% SAC  
 284 than during co-firing with CYN. Furthermore, spontaneous sheddings seem to be more frequent for



285 100% SAC. In spite of the lower ash content of CYN, the presence of alkaline elements, as calcium  
286 or potassium, together with other elements as sulfur and chlorine, favors fouling growth (37; 41).

287 With regard to CYN-SAC blends, some differences in the dynamics would be noticed. Time series  
288 of 5% CYN (test 2) follow very monotonic trend, while many spontaneous sheddings would be iden-  
289 tified for 10% CYN (test 3) and 15% CYN (test 4). Such different dynamics could be explained from  
290 higher temperatures in the first case, which could influence the structure of the deposit, producing  
291 higher sintering level and reducing spontaneous shedding of ash deposits. In addition, temperatures  
292 would also change the emissivity of the flame as the percentage of CYN increase, due to the higher  
293 volatile content (39). Such changes are influential on radiative heat exchange, but they were not  
294 considered in the present modelling approach.

295 Thermal resistance is slightly lower for 10% CYN than for 15% CYN as it would be expected, but  
296 it is also lower than for 5% CYN. This result could be explained from higher temperatures during  
297 test 2 both, for combustion gases and for refractory walls, and the subsequent absence of casual  
298 sheddings because of a more important sintering of the outer deposit layer.

299 Figure 8 compares the heat transfer ratio and the deposit thermal resistance of tests 1, 3 and  
300 5 (100% SAC, 10% CYN and 10% PWO, respectively). As previously, decrease in heat uptake ratio  
301 is lower for 100% SAC, while it is quite similar for the two biomass blends. Thermal resistance  
302 is slightly lower for PWO than that for CYN, although they are very similar at the end of the  
303 experiment. Despite the small difference in gases temperature, this was a non-expectable result as,  
304 a priori, cynara, with much higher ash content, would produce a fouling rate significantly faster.

305 In order to explain this result, the flame radiation captured by the CCD camera is here used  
306 to compare the combustion performance during both tests, given the usefulness of flame imaging to  
307 detect instabilities and inefficiencies during combustion shown in previous works (39; 49). Specifically,  
308 Figure 9 represents the mean gray level of a flame video constituted by 5200 images, where the burner



Figure 9: Mean radiation level during co-firing at a gases temperature of 970 °C and nominal operational conditions. Left: 10% CYN with [CO]=82 mg/m<sup>3</sup>N. Right: 10% PWO with [CO]=460 mg/m<sup>3</sup>N.

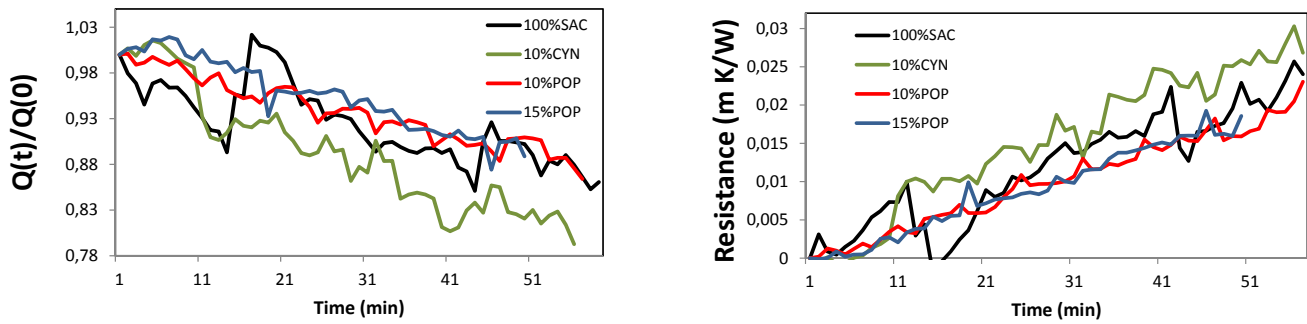


Figure 10: Time evolution of heat transfer ratio (left) and deposit thermal resistance (right) for tests 5-8.

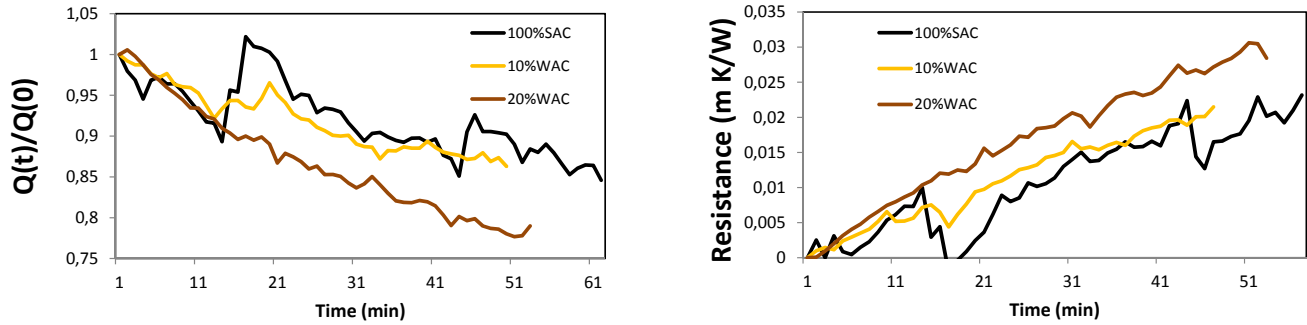


Figure 11: Time evolution of heat transfer ratio (left) and deposit thermal resistance (right) for tests 1 and 9-10.

309 exit is centered on the bottom side. A lower level of radiation during test 5 and higher emissions of  
 310 carbon monoxide than those of test 3 were registered (460 vs. 82 mg/m<sup>3</sup>N), indicating an inefficient  
 311 PWO combustion. The probable generation of unburned solids could decrease flame radiation and  
 312 increase the amount of fouling deposits.

313 Figure 10 compares results for blends of POP and CYN with 100%SAC. First of all, little dif-  
 314 ferences are observed between the two blends of POP (tests 7-8), even in spite of the important  
 315 difference of refractory wall temperatures (Figure 6).

316 On the contrary, a very different dynamics is observed for tests 1 and 6 (100%SAC and 10%CYN,  
 317 respectively). Both heat uptake ratio and thermal resistance exhibit a very monotonic trend for  
 318 poplar blends, while a more irregular evolution is observed for 100%SAC and 10%CYN, probably  
 319 due to alternating periods of fouling and ash sheddings.

320 Additionally, a lower fouling level is obtained for poplar blends as it was expected from its very  
 321 low ash content shown in Table 1. Both phenomena could be interrelated. The important reduction  
 322 in ash content (12% and 15% for tests 7 and 8, respectively) would produce a thinner layer of ash  
 323 deposit, resulting in less probable shedding events.

324 Finally, Figure 11 compares the time evolution of heat transfer and thermal resistance for SAC



Figure 12: SEM image of a fouling layer during SAC combustion (left) and the corresponding black-white picture (right) for porosity estimation.

325 (test 1) and CMR (tests 9-10). As occurs with test 2, a very regular decrease of heat uptake is  
326 observed during co-firing of CMR (tests 9-10). The absence of spontaneous sheddings could be  
327 due to both, very high temperatures during the test, which could produce a more intense sintering,  
328 and the very high ash content of CMR (55% d.b.). Thermal resistance is significantly greater for  
329 20% CMR, where mass flow of CMR is a 50% of the total fuel flow rate.

330 All in all, it would be expected to obtain very much higher fouling levels for coal mine waste  
331 residues than for biomass fuels. Two possible phenomena could explain the experimental result of  
332 CMR: a lower porosity of the deposit or a continuous loss of ash due to the great concentration of  
333 particles impacting with the probe surface. Further experimental research should be done to clarify  
334 the cause of the observed behaviour.

#### 335 *4.3. Discussion about thermal conductivity estimation*

336 In principle, besides thermal resistance, the prediction of deposits thickness would be desirable. The  
337 essential parameter to this end is the thermal conductivity, given the almost linear relation between  
338 them. In turn, according to previous works (26; 31; 50; 51), the microstructure, specially the porosity,  
339 is determining to properly estimate thermal conductivity. Specifically, Baxter established a linear  
340 relation between thermal conductivity and porosity (50), while various authors reported an important  
341 influence of sintering degree as deposit growth takes place (26; 31).

342 This section performs a realistic evaluation of thickness prediction under semi-industrial scale  
343 conditions. The results about porosity of ash deposits obtained from images acquired with scanning  
344 electron microscope (SEM) are presented. The test coupon was embedded in epoxy, and the fouling  
345 layer was cross sectioned and polished before the imaging with SEM.

346 Thresholding method was applied to SEM images in order to convert gray images into black and  
347 white pictures. Threshold was adjusted for each image as illumination was different from one to

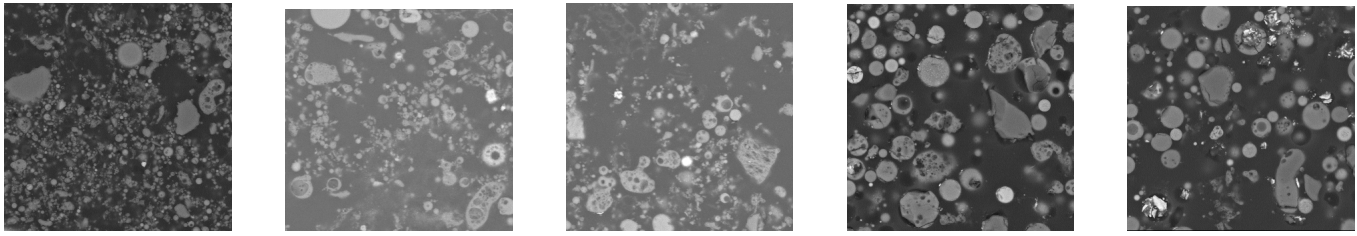


Figure 13: Examples of SEM images of ash deposits used for porosity estimation for different fuel blends. From left to right: Tests 1, 3, 4, 9 and 10.

348 another. An example of the final result is shown in Figure 12, where dark background corresponds to  
 349 epoxy and bright regions are ash fouling particles. The porosity was determined from the percentage  
 350 of black pixels in the fouling layer.

351 A strong decrease of porosity was observed from inner to outer layer of the deposit as can be seen  
 352 in Figure 12. Specifically, for the deposit collected during 100% SAC combustion, porosity diminishes  
 353 from 82% to 58%. This result agrees with previous observations (26) and could be due to a certain  
 354 degree of sintering in the outer layer as it is subjected to higher temperatures.

355 Mean porosity has been estimated for those tests with samples of enough quality (Figure 13).  
 356 The mean porosity is in all cases within the usual ranges as it is shown in Table 4. Porosity is around  
 357 10% lower for 100% SAC (test 1) than for blends of CYN and CMR. Little differences were obtained  
 358 in porosity for CYN blends, while a certain increase from 74% to 80% is obtained for CMR.

Table 4: Mean porosity estimated from SEM images.

Test	Fuel blend	Mean porosity (%)
1	100% SAC	62
3	10% CYN	74
4	15% CYN	72
9	10% CMR	74
10	20% CMR	80

359 According to previous works (31; 34), changes of the observed order in porosity could double the  
 360 value of thermal conductivity. For this reason, the prediction of thickness is almost impossible during  
 361 operation of actual boilers and dedicated and sophisticated instruments should be installed. However,  
 362 for the design of cleaning sequences in superheaters, the thickness value itself is not essential and the  
 363 prediction of fouling thermal resistance would be enough in most cases (35; 36).

## 364 5. Summary and conclusions

365 The present work has presented the results about ash deposition during successful co-firing of South  
366 African coal with three biomasses and with coal mine waste residues. An instrumented deposition  
367 probe, installed in a semi-industrial scale facility, emulated the conditions of actual superheaters in  
368 power stations.

369 A thermal model of the deposition probe was developed for estimation of deposit thermal resis-  
370 tance by considering two sink surfaces and a gaseous mass source in the radiative exchange model.  
371 The validation was performed by comparing the predicted and the measured temperature of the probe  
372 surface. Maximum deviations of 20 °C were obtained, being considered an acceptable figure for the  
373 present approach, given the order of magnitude of typical errors in thermocouples under convective  
374 and radiative effects.

375 The most influential parameters on thermal resistance were identified from a sensitivity analysis:  
376 the emissivity of deposit surface and the flue gas temperature. Therefore, the measure of emissivity  
377 under the specific conditions of final application and the registration of the flue gas temperature with  
378 high accuracy during the tests are mandatory to achieve an accurate prediction of fouling thermal  
379 resistance.

380 The comparison of time evolution of heat transfer ratio and thermal resistance for different fuel  
381 blends indicated that the introduction of cynara and pine increases the fouling rates, even for low  
382 substitution percentages. On the contrary, the introduction of poplar, with a very low ash content,  
383 produces lower or very similar levels of fouling rate to that obtained for coal combustion (41). With  
384 regard to coal mine waste residues, given its very high ash content, an important worsening with  
385 regard to deposit thermal resistance would be expected, but the calculated value was similar to that  
386 obtained for cynara and further research must be done to clarify such experimental result.

387 Finally, a discussion about the estimation of thermal conductivity estimation was performed from  
388 experimental data extracted from SEM images. On the one hand, fuel blends gave rise to higher  
389 porosity, related to lower thermal conductivity, especially for coal mine waste residues. On the other  
390 hand, the analysis on microstructure confirmed that porosity, and therefore thermal conductivity,  
391 varies from inner to outer layers (26). Thus, under real conditions, it is not possible to predict  
392 the deposit thickness with enough accuracy and dedicated and customized instruments should be  
393 designed and installed for its measurement in every particular facility if thickness is needed.

394 In summary, besides the interest of the comparative study of experimental results during co-firing

395 of the different fuel blends, the paper has demonstrated the usefulness of thermal models to estimate  
396 the thermal resistance of ash deposits without the need of sophisticated instrumentation. Dedicated  
397 thermal models, similar to the developed one, could be integrated in the control of combustion  
398 facilities in order to design smart cleaning sequences.

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