

1 **HIGH-PRESSURE SPEED OF SOUND IN PURE CO₂ AND IN CO₂ WITH SO₂ AS AN IMPURITY USING**
2 **METHANOL AS A DOPING AGENT**

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9 **ABSTRACT**

10 Reliable speed of sound, c , values in CO₂-rich mixtures and pure CO₂ are required for carbon
11 capture and storage (CCS) technology but are difficult to determine, particularly at relatively high
12 frequencies. We tested the suitability of methanol as doping agent to obtain accurate c values in
13 CCS systems at 5 MHz. We measured c in seven CO₂-rich, CO₂+methanol mixtures between 263.15
14 and 323.15 K and up to 196.30 MPa, and we extrapolated the values to obtain c in pure CO₂.
15 Additionally, we measured c from 263.15 to 373.19 K and up to 190.10 MPa in two CO₂-rich,
16 CO₂+SO₂ mixtures with the same SO₂ composition, which is of interest for CCS, with one mixture
17 doped with methanol. We compared our results for pure CO₂ with the literature and the Span and
18 Wagner equation of state (EoS). We validated the PC-SAFT EoS and the modeling with the REFPROP
19 software for the mixtures by comparing the predicted values with our experimental data under
20 the studied conditions. We conclude that methanol is a suitable doping agent to measure c in pure
21 CO₂ and CO₂-rich mixtures. For the CO₂+SO₂ mixtures, the effect of methanol on the experimental
22 values is small and negligible for modeling.

23 **Keywords**

24 CCS, speed of sound, CO₂, methanol, dopant, SO₂

25 **1. Introduction**

26 The concentration of CO₂ in the atmosphere increased 2.1 ppm/year during the last ten years,
27 exceeding 400 ppm in March 2015 (Mauna Loa Observatory). This value is 15% higher than the
28 recommended upper limit of 350 ppm to avoid dangerous climate effects (Hansen et al., 2008;
29 Allen et al., 2009). Despite political commitments (KP 1998; UNFCCC 2006, 2008, 2010, 2012, 2014,
30 2015, 2016), fossil fuels are expected to account for 75% of global energy demand by 2035. Global
31 energy demand is expected to grow, mainly in developing countries, and estimations predict that
32 energy-related CO₂ emissions will increase by 20% in the same period. Such increases will lead to a
33 long-term scenario with an average temperature increase of 3.6°C, far above the 2°C target
34 internationally agreed upon in 2009 and ratified in 2015 (UNFCCC 2010, 2016).

35 Carbon capture and storage (CCS) technology is a realistic, effective and promising option to
36 significantly reduce large-scale CO₂ emissions. CCS plays an important role in the mitigation of
37 climate change, in combination with increased energy efficiency, fuel switching and the
38 development of renewable energy sources. In the absence of CCS technology, the additional
39 investment needed to meet the 2°C target would increase by at least USD 2 trillion by 2050 (IEA,
40 2012).

41 The most economical and operational means of transporting anthropogenic CO₂ from capture and
42 conditioning facilities to geological storage sites is typically through pipelines as a dense-phase fluid
43 (either liquid or supercritical). Pipeline design must be optimized to ensure cost-effectiveness and
44 safety. The speed of sound, c , is a useful property to study several aspects of transport, such as

45 detection and monitoring of (undesired) gas bubbles in the dense phase and depressurization and
46 leak checking, because c determines how fast the pressure will drop (Aursand et al., 2013; Leighton
47 et al., 2012; Lund et al., 2011; Medwin, 1977; Stoianov et al., 2007; Zhang, 1996).

48 Because of the conditions inside geologic reservoirs, the fluid is usually in the supercritical phase
49 during storage. In this step, c can be used to monitor the formation of bubbles in leakages (Bergès
50 et al., 2015; Leighton and White, 2012), estimate the seismic properties of hydrocarbon reservoirs,
51 optimize enhanced oil recovery (EOR) processes, and monitor CO₂ plumes in saline aquifers and
52 depleted reservoirs (Lebedev et al., 2014; Siggins et al., 2010).

53 Anthropogenic CO₂ is not pure CO₂ but contains impurities that can modify its properties and thus
54 influence its behavior in the different steps of CCS technology. N₂, H₂, O₂, Ar, SO₂, NO_x, CO and
55 water are the main impurities (Løvseth et al., 2013; Porter et al., 2015), and methanol can be
56 present because of its use as a hydrate inhibitor and as a residue from pipeline drying. Recent
57 publications suggest that the presence of certain impurities, such as SO₂, favors some aspects of the
58 CCS process and propose the co-capture of CO₂/SO₂, which additionally avoids SO₂ emissions to the
59 atmosphere (Elshahomi et al., 2015; Koenen et al., 2015; Wang et al., 2015, 2011; Wolf et al., 2015;
60 Ziabakhsh-Ganji and Kooi, 2014a, 2014b). We are conducting a wide range of research on the
61 determination of values for the thermodynamic properties of CO₂-rich mixtures containing SO₂ and
62 other impurities. We are studying the influence of these impurities on CCS parameters for transport
63 and storage to determine the feasibility of CO₂/SO₂ co-capture (Gimeno et al., 2015).

64 Experimental thermodynamic data for the systems and conditions of interest for CCS technology
65 are scarce. For pipeline management and safety, the thermodynamic properties of fluids are often
66 obtained from thermodynamic models, usually equations of state, EoSs (Eiber et al., 1993; Picard

67 and Bishnoi, 1988; Mahgerefteh et al., 2012a, 2012b). For industrial applications, cubic EoSs are
68 preferred due to their simplicity, but deviations from real behavior are often important, particularly
69 when the fluid contains polar components. Multiparametric approaches, such as GERG EoS (Kunz et
70 al., 2007; Kunz and Wagner, 2012), with good accuracy for mixtures containing compounds
71 included in the database, are difficult to expand to other mixtures, and consume more computer
72 time. PC-SAFT EoSs (Gross and Sadowski, 2001, 2002), which is based on perturbation theory,
73 presents intermediate accuracy and complexity. The shortage of experimental thermodynamic data
74 under conditions relevant to CCS technology complicates EoS validation, and there is no reference
75 model to predict the behavior of the transported and stored fluid (Li et al., 2011).

76 With respect to pure CO₂, many thermodynamic properties have been accurately determined under
77 wide ranges of temperature and pressure; however, c data under CCS conditions are not abundant.
78 The reference EoS for CO₂, SW EoS (Span and Wagner, 1996), collected data from four sources
79 (Herget, 1940; Lemming, 1989; Novikov and Trelin, 1962; Pitaevskaya and Bilevich, 1973), and only
80 those from Pitaevskaya and Bilevich include some temperatures of interest for CCS. More recently,
81 Al-Siyabi (2013) and Lin (2013) reported data under CCS conditions using ultrasonic pulse-echo
82 techniques. Several works have focused on the study of the critical region and/or the use of c to
83 determine the critical point of pure CO₂ (Herget, 1940; Kordikowski et al., 1996; Oag et al., 2004;
84 Parbrook and Richardson, 1952; Tielsch and Tanneberger, 1954; Trelin and Sheludyakov, 1966;
85 Zevnik, et al., 2006).

86 Experimental determination of c in pure, dense CO₂ presents serious difficulties due to its high
87 sound absorption, α , associated with its long vibrational relaxation time, τ , which results in poor or
88 no signal detection at relatively high frequencies. τ can be reduced by decreasing the working
89 frequency, but this requires a large volume of fluid (not advisable with high-pressures techniques),

90 and echoes and diffraction effects can hinder the interpretation of the results (Lin, 2013; Lin and
91 Trusler, 2014). An alternative is the use of a *catalyst* or *dopant*. Knudsen and Fricke (1940)
92 investigated the influence of small amounts of certain impurities (H₂, H₂O, H₂S, CH₃OH, C₃H₇OH and
93 C₆H₅CH₃) on the acoustic behavior of highly absorptive gases (CO₂, N₂O, COS and CS₂) at
94 atmospheric pressure and 23°C. They determined that the impurities accelerate the reaction rate of
95 the transition of these gases from vibrating to non-vibrating molecules, decreasing the time of
96 survival of the activated molecules and decreasing both α and τ . In this way, Lin and Trusler (2014)
97 derived c in pure CO₂ based on measurements in mixtures of CO₂ containing small amounts of
98 propane as the dopant at 2 MHz, temperatures between 248 and 373 K and pressures up to 200
99 MPa. Extrapolation of these measurements to a zero concentration of the dopant enabled the
100 determination of c in pure CO₂.

101 We utilize a double-path, double-echo, ultrasonic pulse facility that functions at 5 MHz. At this
102 frequency, we obtain no signal or a very poor signal in either pure CO₂ or in several CO₂-rich
103 mixtures of interest for CCS technology, such as CO₂+SO₂ with $x_{\text{CO}_2} > 0.9$. In addition, we cannot
104 use propane as a dopant at this frequency (we obtained only a tiny signal for CO₂+C₃H₈ with
105 $x_{\text{CO}_2} \cong 0.8$), and thus we must select another doping compound that is adequate for the features of
106 our measurement device. We selected methanol, an impurity studied by Knudsen and Fricke
107 (1940). Methanol is chemically compatible with the installation, has well-known properties as a
108 modifier in supercritical extraction, is used in industrial processes as Rectisol, and is added as a
109 desiccant and/or hydrate inhibitor (Boot-Handford et al., 2014; Dykhno, L. et al., 2011; Esteban et
110 al., 2000; Feng et al., 2014; Kemper et al., 2014; Kerestecioglu and Haberle, 2010; McIntyre et al.,
111 2004; Perry and Eliason, 2004; Peterhead CCS Project, 2015; Weiss and Schriefl, 2010).

112 The aims of this work were as follows: i) to test the suitability of methanol as doping agent to
113 obtain reliable values of c at 5 MHz in the working ranges of our installation, not only in doped
114 “pure” dense CO₂ but also in acoustically opaque CO₂-rich mixtures of interest for CCS; ii) to
115 quantify the effect of methanol on c in pure CO₂ and in a CO₂+SO₂ mixture of interest for CCS; iii) to
116 validate the PC-SAFT EoS and the modeling implemented in the REFPROP 9 software for c in CO₂-
117 rich mixtures with methanol and/or SO₂, thus contributing to the development and improvement of
118 the models needed for the design of processes in CCS technology.

119 For this purpose, we determined c in seven CO₂+CH₃OH mixtures with compositions $0.80 < x_{\text{CO}_2} <$
120 0.99 at $T = 263.15, 298.15$ and 323.15 K and up to approximately 200 MPa. By extrapolation of c in
121 the five CO₂-richest mixtures to infinite dilution, we obtained reliable values of c in pure CO₂ and
122 compared these results with the literature (Al-Siyabi, 2013; Lin, 2013; Lin and Trusler, 2014;
123 Pitaevskaya and Bilevich, 1973). We estimated the effect of methanol by comparing our results for
124 the mixtures of CO₂+methanol with those calculated using the reference EoS for pure CO₂ (Span
125 and Wagner, 1996). In addition, we compared the results for binary mixtures with those calculated
126 using the PC-SAFT EoS (Gross and Sadowski, 2001, 2002) and the modeling procedure implemented
127 in the REFPROP 9 software (Lemmon et al. 2010). Finally, we applied the doping to a mixture of
128 CO₂+SO₂ with $x_{\text{SO}_2} = 0.1031$. We measured c in both undoped and doped mixtures of this
129 composition at eight temperatures between 263.15 and 373.19 K and at pressures up to
130 approximately 190 MPa, and we compared the results with each other and with those predicted by
131 the specified models.

132 **2. Materials and methods**

133 *2.1. Chemicals*

134 Carbon dioxide (mole fraction > 0.99998) and sulfur dioxide (mole fraction 0.9990), from Air
135 Liquide, were used as received. Methanol (biotech. grade, mole fraction 0.9993), from Sigma
136 Aldrich, was degassed immediately before use.

137 *2.2. Apparatus and procedure*

138 Speed of sound measurements were performed using an installation that employs a pulsed
139 ultrasonic system, which allows measurements in liquids and in compressed gases in dense or
140 supercritical phase with viscosities up to around 100 mPa s (Ball and Trusler, 2001; Dávila and
141 Trusler, 2009; Lin and Trusler, 2014). The main component is a dual-path ultrasonic cell located
142 within a pressure vessel inside a thermostatic bath. Both ends of the cell are stainless-steel
143 reflectors, and a piezoceramic transducer of lead zirconate titanate ($\text{PbZrO}_3/\text{PbTiO}_3$) is hold
144 between them, at constant and unequal distances of each one, by means of fused quartz spacers.
145 The transducer is operated at its resonance frequency of 5 MHz. Excited by a single five-cycle tone
146 burst (5 MHz, 10 V peak-to-peak amplitude), the transducer emits ultrasonic pulses that propagate
147 into the fluid to either side. The pulses are reflected by the reflectors at the ends of the cell, and
148 the two returning echoes are detected when they reach the transducer again. The speed of sound
149 in the fluid is determined using $c = 2\Delta L/\Delta t$, where ΔL is the difference between the two path
150 lengths (unequal transducer-reflector distances), determined by previous calibration, and Δt is the
151 difference between the two detection times. The apparatus works from 253.15 K to 473.15 K, and
152 the temperature is measured using a previously calibrated platinum resistor with a standard
153 uncertainty, u_T , of 0.015 K. The pressure is measured with a pressure transducer Paroscientific
154 Model 430K with a standard uncertainty, u_P , of 0.05 MPa, and the maximum achievable pressure is
155 200 MPa. A more detailed description of the apparatus, its calibration, measurement procedure,
156 and calculation of the accuracy for pure compounds has been published elsewhere (Velasco et al.,

2011). The procedures for preparing mixtures, performing measurements, and calculating measurement uncertainty are described in Rivas et al. (2016). The standard uncertainty of the experimental c , u_c , was calculated using the propagation uncertainty law

$$u_c^2 = [(\partial c/\partial T)_P u_T]^2 + [(\partial c/\partial P)_T u_P]^2 + [(\partial c/\partial x) u_x]^2 + (u_c^*)^2 \quad (1)$$

where u_x and u_c^* are the standard uncertainty of the mole fraction and the standard repeatability uncertainty, respectively, which depend on the studied system (Rivas et al., 2016). For the mixtures in this work, $u_c = 5.9 \times 10^{-4} c$ for $\text{CO}_2+\text{CH}_3\text{OH}$ (Rivas et al., 2016), $u_c = 6.2 \times 10^{-4} c$ for CO_2+SO_2 and $u_c = 8.1 \times 10^{-4} c$ for $\text{CO}_2+\text{SO}_2+\text{CH}_3\text{OH}$. These values lie within the range of standard uncertainties ($3 \times 10^{-4} c$ to $10 \times 10^{-4} c$) obtained by other authors using similar apparatus for liquids and for compressed gases (Ball and Trusler, 2001; Dávila and Trusler, 2009; Lin and Trusler, 2014).

3. Modeling

In this work, we compared our experimental data with those obtained from the PC-SAFT EoS and the REFPROP 9 software.

3.1. PC-SAFT EoS (Gross and Sadowski, 2001, 2002).

The PC-SAFT EoS describes the dimensionless Helmholtz energy, \tilde{a} , as the sum of different contributions: ideal-gas (*id*), hard-chain (*hc*), dispersive attraction (*dis*), association (*assoc*), and multipolar interactions (*DD*, dipole-dipole, *QQ*, quadrupole-quadrupole, and *QD*, quadrupole-dipole):

$$\tilde{a} = \tilde{a}^{id} + \tilde{a}^{hc} + \tilde{a}^{dis} + \tilde{a}^{assoc} + (\tilde{a}^{DD} + \tilde{a}^{QQ} + \tilde{a}^{QD}). \quad (2)$$

In this model, three geometric parameters (m , σ , ε) are needed to describe each non-associated and non-polar pure compound. In the mixtures, for each pair of compounds, i and j , classical mixing rules with an adjustable binary interaction parameter, k_{ij} , are used to calculate σ_{ij} and ε_{ij} :

$$\sigma_{ij} = \frac{1}{2}(\sigma_i + \sigma_j); \quad (3)$$

$$\varepsilon_{ij} = \sqrt{\varepsilon_i \varepsilon_j}(1 - k_{ij}). \quad (4)$$

178 Two additional parameters ($\kappa^{A_i B_i}$, $\varepsilon^{A_i B_i}$) and an association scheme are required if the molecule is
 179 self-associated or undergoes induced association. The latter can be considered in systems
 180 containing a self-associated compound and another non-associated compound that possess either
 181 proton donor or proton acceptor sites. Then, the cross-association parameters, $\kappa^{A_i B_j}$ and $\varepsilon^{A_i B_j}$, can
 182 be calculated from the Kleiner and Sadowski (2007) approach:

$$\kappa^{A_i B_j} = \kappa^{assoc.comp} \quad \varepsilon^{A_i B_j} = \frac{\varepsilon^{assoc.comp}}{2} \quad (5)$$

183 In this work, multipolar interactions were not considered, and the calculations were performed
 184 using VLXE software (Laursen, 2012).

185 3.2 REFPROP 9 software (Lemmon et al. 2010).

186 The software REFPROP (Reference Fluid Thermodynamic and Transport Properties Database) is a
 187 program developed by the National Institute of Standards and Technology (NIST) that calculates the
 188 thermodynamic and transport properties of fluids of interest and their mixtures. It uses the most
 189 accurate pure fluid and mixture models currently available. For the systems studied in this work, we
 190 applied the REFPROP 9 version in its “Calculate properties using default equations” option. It uses
 191 pure component reference EoSs by different authors, combined with different mixture models. The
 192 pure fluid equations are from Span and Wagner (1996) for CO₂, from de Reuck and Craven (1993)
 193 for methanol, and from Lemmon and Span (2006) for SO₂. According to Dr. E.W. Lemmon (2016,
 194 personal communication), the mixture models use the same functional form as that in the GERG-

195 2008 EoS (Kunz and Wagner, 2012); apart from their implementation in REFPROP 9, they are
196 unpublished as far as we know. The mixing parameters are available in the REFPROP 9 program.

197 4. Results

198 4.1. Speed of sound in the CO₂+CH₃OH system

199 $P - c - T - x_{\text{CO}_2}$ measurements for seven CO₂-rich, CO₂+CH₃OH mixtures $\{x_{\text{CO}_2} = 0.8005, 0.9025,$
200 $0.9503, 0.9700, 0.9794, 0.9845, 0.9898\}$ were performed at 5 MHz and at $T = 263.15, 298.15$ and
201 323.15 K, with the exception of $x_{\text{CO}_2} = 0.9700$ at 263.15 K, which we published previously (Rivas et
202 al., 2016). For mole fractions $x_{\text{CO}_2} > 0.99$, the results for c were not reproducible. The maximum
203 pressure for each isotherm and isopleth was delimited by the amount of transferred fluid and the
204 compressibility of the mixture, and the minimum pressure was the lowest at which a clear signal
205 was obtained. The range of pressures was 3.28–196.30 MPa.

206 The experimental results are listed in Tables 1–3, and their representations are shown in Figs. 1 and
207 S1-S6 (Supplementary Material). For the studied compositions, c in the fluid increased with
208 increasing pressure and decreasing temperature. We did not identify speed of sound data in the
209 literature for this system, except data published by ourselves (Rivas et al., 2016), which are in
210 agreement with this work.

211 The experimental values of c were correlated as a function of pressure using the polynomial (Lin
212 and Trusler, 2014)

$$(P - P^\#) = \sum_{i=1}^3 a_i (c - c^\#)^i, \quad (7)$$

213 where $P^\# = 70$ MPa and $c^\#$ is the speed of sound at $P = P^\#$.

214 The coefficients of equation 7 as well as the mean relative deviations $MRD_c(\%)$ between the fitted
215 and experimental values for each isotherm and isopleth are shown in Table 4. The overall mean
216 relative deviation was $\overline{MRD}_c = 0.012\%$, lower than the relative standard uncertainty of the
217 experimental data (0.059%). No clear trends with composition or temperature were observed, with
218 higher deviations at low pressures (Fig. 2).

219 4.2. Speed of sound in the CO_2+SO_2 and $CO_2+CH_3OH+SO_2$ systems

220 To test and quantify the effect of methanol as a doping agent in the CO_2+SO_2 system, we measured
221 eight $P - c - T$ isotherms for each of these systems: a binary mixture with composition
222 $x_{CO_2} = 0.8969$ and $x_{SO_2} = 0.1031$ and a ternary mixture (doped with 0.8% of methanol) with
223 composition $x_{CO_2} = 0.8889$, $x_{CH_3OH} = 0.0080$ and $x_{SO_2} = 0.1031$. The measurements were
224 performed at 263.15, 273.15, 293.15, 304.16, 313.15, 333.15, 353.15 and 373.19 K and from 7.99 to
225 150.00 MPa for the binary mixture and from 8.00 to 190.10 MPa for the ternary mixture. The
226 amount of CO_2 is sufficiently high to be of interest for CCS, and both mixtures provided reliable
227 values of c under the studied conditions. All experimental results are presented in Tables 5 and 6,
228 and values at select temperatures are presented in Figures 3 and 4. The value of c increased with
229 increasing pressure and decreasing temperature. No data were identified in the literature on c in
230 these mixtures.

231 The experimental results of c for each isotherm and isopleth were correlated to the polynomial (7).
232 Tables 7 and 8 present the values used for $P^\#$, the fitting coefficients, and the mean relative
233 deviations for the binary (undoped) and ternary (doped) mixtures, respectively. The overall mean
234 relative deviations of the fittings were 0.025% and 0.010%, respectively, lower than the
235 corresponding relative standard uncertainties of the experimental data (0.062% and 0.081%).

236 5. Discussion

237 5.1. Estimated speed of sound in dense, pure CO₂

238 Dense-phase pure CO₂ exhibits a very long vibrational relaxation time, $\tau_{\text{CO}_2-\text{CO}_2} \cong 1.71 \times 10^{-8}$ s, at
239 298 K and 69 atm (Bass and Lamb, 1958) and a high absorption coefficient at high frequencies. The
240 absorption coefficient of pure CO₂ at several pressures and temperatures can be calculated using
241 the equations collected by Lin and Trusler (2014). Under our working conditions, $\alpha \cong 100\text{-}1850$ m⁻¹,
242 far from the upper detection threshold of our device ($\alpha \cong 40$ m⁻¹); CO₂ is opaque in our facility.
243 However, we can use the catalytic effect of methanol in the deactivation of the vibrating CO₂
244 molecules (Knudsen et al., 1940): a vibrating CO₂ molecule will survive, on average, 86,000
245 collisions with other CO₂ molecules at room conditions but only 36 collisions with methanol
246 molecules. In this way, both α and τ decrease significantly.

247 In this work, we utilized the experimental values of c in the five CO₂-richest, CO₂+methanol
248 mixtures, $x_{\text{CO}_2} > 0.95$, and those for the mixture of composition $x_{\text{CO}_2} = 0.9700$ at 263.15 K
249 previously determined by us (Rivas et al., 2016) to estimate the values of c in pure CO₂ by
250 extrapolation to $x_{\text{CO}_2} = 1$. For this purpose, we used the coefficients from Table 4 to obtain c_{fit} data
251 at round values of P at each T . These interpolated values were correlated as a function of the CO₂
252 mole fraction (Lin and Trusler, 2014):

$$c_{fit}(x_{\text{CO}_2}) = c_0 + c_1(1 - x_{\text{CO}_2}) + c_2(1 - x_{\text{CO}_2})^2, \quad (8)$$

253 where $c_{fit}(x_{\text{CO}_2} = 1) = c_0$ is the speed of sound in pure CO₂. Table 9 presents the correlated
254 values of c_{fit} and, for each correlation, the coefficients of eq. (8), including the value obtained for c_0
255 and the standard relative uncertainty of c_0 , $u_r(c_0)$. This uncertainty was calculated by combining
256 the relative standard uncertainty of the experimental c , 0.059% (Rivas et al., 2016), with the

257 relative standard deviation of c_0 determined by eq. (8). The overall value, $\overline{u_r(c_0)} = 0.12\%$, is similar
258 to that obtained by Lin and Trusler (2014) using the same procedure but with a different dopant
259 (propane) and frequency (2 MHz) and lower than the tolerance margin (0.5-2%) presented by the
260 SW EoS in this region (Span and Wagner, 1996).

261 In the literature, experimental data on c in pure CO_2 under the same conditions as in this work are
262 scarce. Pitaevskaya and Bilevich (1973) determined c at temperatures $T=298\text{--}473$ K and pressures
263 $P = 50\text{--}450$ MPa and reported a minimum accuracy of the speed-density equations of 1%. Lin
264 (2013) measured c at $263\text{--}363$ K and pressures up to 325 MPa but did not obtain confident values
265 for the uncertainty. Both studies are in good agreement with our results, with overall mean relative
266 deviations $\overline{MRD}_c = 0.61\%$ and $\overline{MRD}_c = 0.44\%$, respectively, when the results at identical
267 temperatures are compared. Al-Siyabi (2013) reported values of c at $T=268\text{--}301$ K and $P=3.6\text{--}42$
268 MPa with an accuracy of ± 1 m/s; these results are consistent with ours but are not directly
269 comparable because they were measured at different temperatures. In addition, we compared our
270 results with those derived by Lin and Trusler (2014) at the same temperatures using propane as a
271 dopant at 2 MHz, obtaining $\overline{MRD}_c = 0.21\%$. Comparing our results with the values provided by SW
272 EoS, the difference is $\overline{MRD}_c = 0.43\%$. As shown in Fig. 5 and 6, there is good agreement between
273 the whole sets of data. Fig. 7 presents the relative deviations between the literature and this work
274 for c in pure CO_2 and those calculated by the SW EoS. The deviations are lower than the tolerance
275 margin of the Span and Wagner equation under these conditions (0.5–2%).

276 5.2. Quantification of the doping effect of methanol in dense, pure CO_2

277 Figure 8 presents the mean relative deviations of our experimental values of c in the CO_2 +methanol
278 mixtures from the values calculated in pure CO_2 using the SW equation, i.e., the error when the
279 mixtures are considered as pure CO_2 . For doping at up to 5 mole %, the relative deviations range

280 from -1.31% to +0.72%, with a \overline{MRD}_c of 0.52%. Doping with only 1 mole % of methanol, the sound
281 echoes are clear at 5 MHz in the studied ranges of pressure and temperature, with relative
282 deviations between -0.82% and +0.52% and $\overline{MRD}_c = 0.38\%$. These deviations are higher than the
283 experimental relative standard uncertainty of c (0.059%) but are almost always within the tolerance
284 margin of the SW equation. Only three of the entire set of experimental points are slightly outside
285 the tolerance margins, and all three are at low pressures (below 10 MPa), low temperature (263.15
286 K) and high concentrations of methanol.

287 Figure 9 shows the correlation of the speed of sound as a function of the composition (equation 8,
288 Table 9) at the three studied temperatures and at several pressures. At 263.15 K, every plot (at
289 each of the pressures of Table 9) presents a minimum between $x_{\text{CO}_2} = 0.960$ and 0.962 , inside the
290 studied high-dilution interval ($x_{\text{CO}_2} > 0.950$). At 298.15 K, the plots show either minima (at $P \leq 80$
291 MPa) or maxima (at $P \geq 100$ MPa), being all of them out of the high-dilution interval. Inside this
292 interval, c increases when the mole fraction of CO_2 increases for all the plots. At 323.15 K, every
293 plot presents a maximum inside the high-dilution interval, between $x_{\text{CO}_2} = 0.963$ and 0.972 . When
294 comparing each derived speed of sound in pure CO_2 , c_0 , with the minimum (at 263.15 K), the
295 maximum (at 323.15 K) or the most different value of c inside the interval (at 298.15 K), we found
296 that $\overline{MRD}_c = 0.86\%$, again within the tolerance margin of the SW equation.

297 5.3. Validation of the PC-SAFT EoS and the REFPROP 9 software for the $\text{CO}_2 + \text{CH}_3\text{OH}$ system

298 A detailed explanation of the application of the PC-SAFT EoS to $\text{CO}_2 + \text{methanol}$ is given in previous
299 works (Gil et al., 2012; Rivas et al., 2016) in which we studied vapor-liquid equilibrium, critical locus,
300 density and c over a wide range of temperature and pressure. In these papers, (i) the geometric
301 parameters of the pure compounds were obtained from their critical points; (ii) 2C and 2B
302 association schemes were used for CO_2 and methanol, respectively; (iii) volume translation was

303 included for the density modeling; and (iv) a temperature-dependent binary interaction parameter
304 was necessary. In this work, we maintained the same procedure, and the values of the parameters
305 used are listed in Table S1.

306 Table 10 reports the mean relative deviations between our experimental data and those calculated
307 using the two models (PC-SAFT and REFPROP 9). Figures 1 and S1-S6 present our experimental
308 results along with the calculated values for each composition and temperature. The relative
309 deviations between the experimental and calculated values are presented in Fig. S7-S9.

310 The PC-SAFT EoS relative deviations for each mole fraction and temperature become nearly
311 constant at pressures above approximately 50 MPa at 263.15 K and 90 MPa at 298.15 and 323.15 K;
312 in this region, the deviations increase with increasing CO₂ concentration. At low pressures, the
313 differences are higher at lower concentrations of CO₂ at 298.15 and 323.15 K. The relative
314 deviations obtained using this model range from -5.21% to +11.4%, with an overall value
315 of $\overline{MRD}_c = 2.83\%$.

316 The REFPROP 9 software overestimates c at all studied temperatures, pressures and compositions,
317 with higher deviations at lower working pressures and higher concentrations of methanol. The
318 relative deviations range from 0.3% to 26.3%, and the overall mean relative deviation is
319 $\overline{MRD}_c = 4.97\%$. However, the REFPROP 9 deviations decrease significantly with increasing CO₂, and
320 for the three CO₂-richest mixtures, \overline{MRD}_c is 1.23%.

321 *5.4. Effect of methanol on c in a mixture of CO₂+SO₂*

322 To assess the usefulness of doping in a CO₂-rich mixture of interest for CCS, we used the system
323 CO₂+SO₂. We prepared two mixtures, one without methanol, with composition $x_{\text{CO}_2} = 0.8969$ and
324 $x_{\text{SO}_2} = 0.1031$, and the other doped with 0.8 mole % methanol, $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and

325 $x_{\text{SO}_2} = 0.1031$. The amount of methanol was 0.8%, which is lower than the amount required for
326 detecting a signal in pure CO_2 in our facility (Section 4.1). We observed that SO_2 favors the
327 deactivation of the vibrating CO_2 molecules. The value of c at 5 MHz was measured in both mixtures
328 at eight temperatures between 263.15 and 373.19 K and an overall range of pressures from 7.99 to
329 190.10 MPa. We obtained good signals in both mixtures in these ranges, which permitted
330 comparison to quantify the effect of methanol on the experimental values of c .

331 To compare the results for both mixtures, we extrapolated the experimental values of c in the
332 binary mixture at each T up to 190.0 MPa using equation (7) and the coefficients from Table 7. The
333 relative deviations are between -0.96% and +0.29% (Fig. 10). These deviations are similar to those
334 for the $\text{CO}_2 + \text{CH}_3\text{OH}(1\%)$ mixture (section 5.2, Fig. 8). The overall mean relative deviation is only
335 0.17%, less than half that of the last mixture value (0.38%) and approximately twice the
336 experimental relative standard uncertainty of the measurements for the ternary mixture (0.081%).
337 The trend of the deviations with temperature is not clear, and larger differences are observed at
338 low pressures.

339 *5.5. Validation of the PC-SAFT EoS and the REFPROP 9 software for the $\text{CO}_2 + \text{SO}_2$ and* 340 *$\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ mixtures*

341 The $\text{CO}_2 + \text{SO}_2$ system (two non-associated compounds) was modeled with the PC-SAFT EoS using the
342 original parameters from Gross and Sadowski (2001) and the binary interaction parameter
343 published by Diamantonis et al. (2013) (Table S1).

344 Both models, PC-SAFT and REFPROP 9, adequately predict c in this mixture (Table 11), but the
345 trends with pressure are opposite (Figures 3 and S10). The overall mean relative deviation using PC-
346 SAFT is $\overline{MRD}_c = 2.19\%$, and the deviation increases with increasing pressure. However, REFPROP 9

347 results in higher deviations at lower pressures, with $\overline{MRD}_c = 1.39\%$. For both models, higher
348 deviations are observed at lower temperatures.

349 The $\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ mixture was modeled in two different ways:

350 (a) Considering the actual composition of the ternary mixture ($x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$,
351 $x_{\text{SO}_2} = 0.1031$). Modeling with PC-SAFT EoS, the pure compound parameters for CO_2 and
352 CH_3OH and its interaction binary parameter, $k_{ij}(\text{CO}_2\text{-CH}_3\text{OH})$, were as described in section
353 5.3 (mixture $\text{CO}_2 + \text{CH}_3\text{OH}$). The pure compound parameters for SO_2 and the $\text{CO}_2\text{-SO}_2$ binary
354 interaction parameter were taken from the literature, as described above (mixture
355 $\text{CO}_2 + \text{SO}_2$). It was assumed $k_{ij}(\text{SO}_2\text{-CH}_3\text{OH}) = 0$ due to the small amount of both compounds in
356 the mixture. The parameters are presented in Table S1. The deviations obtained for
357 modeling this mixture as a ternary mixture are presented in Table 11 and Figures S11 and
358 S12. By comparing our data with the PC-SAFT calculated values, we obtained an overall
359 $\overline{MRD}_c = 3.24\%$, and the observed deviations decrease with increasing temperature. From
360 REFPROP 9, the overall $\overline{MRD}_c = 1.28\%$, and the deviations are higher at low temperatures
361 and pressures.

362 (b) Considering the ternary mixture as a binary mixture in which the methanol mole fraction is
363 added to that of CO_2 ($x_{\text{CO}_2} = 0.8889 + 0.0080$; $x_{\text{SO}_2} = 0.1031$). Both models were applied using
364 the same procedure described above for the $\text{CO}_2 + \text{SO}_2$ mixture. The deviations obtained are
365 presented in Table 11 and Figures 4 and S13. The overall deviations obtained using PC-SAFT
366 and REFPROP 9 were $\overline{MRD}_c = 2.35\%$ and 1.26% , respectively. The trends with P and T are
367 similar to those observed in (a).

368 Regarding the variation of the relative deviations with pressure, for both methods of modeling, (a)
369 and (b), both models exhibited opposite trends (Fig. S12 and S13). Similar behavior was observed in
370 the CO₂+SO₂ mixture (Fig. S10).

371 PC-SAFT more accurately reproduces the experimental results of the ternary mixture if it is
372 modeled as binary rather than as ternary, whereas REFPROP 9 produces similar results for binary
373 and ternary modeling.

374 6. Conclusions

375 Due to the great difficulties in determining c in pure CO₂ and in many CO₂-rich mixtures of interest
376 for CCS, we evaluated the suitability of methanol as a doping agent at a frequency of 5 MHz. The
377 addition of methanol between 1% and 5% to pure CO₂ enabled the measurement of c at the cited
378 frequency in the studied ranges of pressure and temperature. This effect was studied by the
379 measurement of c in seven CO₂+methanol mixtures with $0.8005 < x_{\text{CO}_2} < 0.9898$ at temperatures
380 $T=263.15, 298.15$ and 323.15 K at a global pressure range of 3.28–196.30 MPa. The standard
381 uncertainty of the experimental results, $u_c = 5.9 \times 10^{-4}c$, is within the values reported in the
382 literature. By extrapolation of the experimental results to $x_{\text{CO}_2} = 1$, we obtained c in pure CO₂. The
383 derived results exhibited deviations between 0.21% and 0.61% from the literature data and of
384 0.43% from the Span and Wagner EoS for pure CO₂. The quantification of the doping effect was
385 estimated by calculating the error in c if the mixtures were considered pure CO₂. When doping with
386 1% methanol, we obtained reproducible measures and $\overline{MRD}_c = 0.38\%$ with respect to pure CO₂
387 (Span and Wagner EoS). These deviations are within the tolerance margin of the Span and Wagner
388 equation under the studied conditions (0.5–2%).

389 The experimental results of the mixtures were compared with those calculated using the PC-SAFT
390 EoS and the REFPROP 9 software, resulting in \overline{MRD}_c of 2.83% and 4.97%, respectively. The
391 differences with REFPROP 9 decrease significantly with increasing CO₂ and are 11.9% for
392 $x_{\text{CO}_2} = 0.8005$ and only 1.23%, on average, for the three CO₂-richest compositions.

393 The effect of methanol on the mixture of interest for CCS technology was studied by comparing the
394 c results for two CO₂+SO₂ (binary, undoped) and CO₂+CH₃OH+SO₂ (ternary, doped) mixtures with
395 the same SO₂ mole fraction ($x_{\text{SO}_2} = 0.1031$) containing 0.8% methanol. The working temperature
396 and pressure ranged from 263.15 to 373.19 K and from 7.99 to 190.10 MPa. The experimental
397 standard uncertainties were $u_c = 6.2 \times 10^{-4}c$ for the undoped mixture and $u_c = 8.1 \times 10^{-4}c$ for
398 the doped mixture.

399 When comparing the c results for both mixtures, we observed that the overall mean relative
400 deviation was $\overline{MRD}_c = 0.17\%$, approximately half that observed when 1% methanol was added to
401 pure CO₂ (0.38%) and approximately twice the experimental relative standard uncertainty of c in
402 the CO₂+CH₃OH+SO₂ mixtures (0.081%).

403 Both mixtures were modeled with PC-SAFT EoS and REFPROP 9 software, and the following overall
404 mean relative deviations were obtained: 2.19% and 1.39%, respectively, for the binary mixture and
405 3.24% and 1.28%, respectively, for the ternary (doped) mixture. When the ternary mixture was
406 modeled as if it was a binary mixture, the deviations were 2.35% with PC-SAFT and 1.26% with
407 REFPROP 9.

408 We verified the suitability of methanol as a doping agent to obtain reliable values of c at 5 MHz in
409 pure dense CO₂ and in a CO₂+SO₂ mixture of interest for CCS. Moreover, we have also quantified
410 the effect of methanol on c in these systems. The effect of methanol on the experimental values is

411 small, and the effect of methanol on modeling is negligible. These results will allow us to obtain
412 reliable values of c in CO₂-rich mixtures that would otherwise not be possible.

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416 **Appendix A. Supplementary material**

417 Supplementary material for this article can be found in the online version. Table S1 contains the
418 parameters used in the PC-SAFT modeling. Figures S1-S6 and S11 present the experimental and
419 modeled speeds of sound in the studied mixtures. Figures S7-S10, S12 and S13 show the relative
420 deviations between the experimental and modeled speeds of sound in the studied mixtures.

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636

Table 1. Experimental speed of sound, c , in the $\text{CO}_2+\text{CH}_3\text{OH}$ system at $T = 263.15$ K and at compositions x and pressures P .

P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})
$x_{\text{CO}_2} = 0.8005$							
6.00	715.0	35.20	931.9	64.83	1073.7	110.60	1235.7
9.77	752.1	39.99	958.0	70.01	1094.6	121.71	1269.0
14.79	795.6	44.89	983.3	75.05	1114.2	140.55	1321.7
20.11	836.3	50.00	1008.2	80.11	1133.2	158.97	1369.6
25.13	870.8	54.74	1030.1	90.13	1169.0	179.95	1419.9
29.95	901.1	60.08	1053.5	100.04	1202.2	196.30	1456.9
$x_{\text{CO}_2} = 0.9025$							
10.03	719.6	35.01	902.0	60.03	1026.1	89.88	1141.4
14.94	764.0	39.98	929.6	65.02	1047.3	99.98	1175.3
19.97	803.8	44.95	955.5	70.26	1068.7	109.60	1205.9
24.91	838.9	50.41	982.4	75.17	1087.8	120.18	1237.6
29.86	871.1	55.21	1004.7	80.08	1106.4		
$x_{\text{CO}_2} = 0.9503$							
3.80	633.5	24.92	829.4	54.91	995.6	110.06	1199.3
6.02	661.8	24.99	830.2	60.01	1018.3	119.96	1228.9
6.17	664.3	29.61	860.8	65.09	1039.8	140.00	1284.7
10.02	706.8	29.96	862.5	69.97	1059.9	159.90	1335.8
14.91	752.6	34.89	892.6	75.00	1079.5	179.99	1383.3
14.96	752.4	39.94	921.0	80.15	1098.9	194.49	1415.5
19.89	792.8	44.89	947.0	90.13	1134.4		
20.10	794.8	49.99	972.3	100.14	1168.0		
$x_{\text{CO}_2} = 0.9700^a$							
3.28	626.2	24.92	829.4	60.01	1018.3	110.06	1199.3
3.80	633.5	29.96	862.5	65.09	1039.8	119.96	1228.9

5.05	649.7	34.89	892.6	69.97	1059.9	140.00	1284.7
6.02	661.8	39.94	921.0	75.00	1079.5	159.90	1335.8
10.02	706.8	44.89	947.0	80.15	1098.9	179.99	1383.3
14.96	752.4	49.99	972.3	90.13	1134.4	194.49	1415.5
19.89	792.8	54.91	995.6	100.14	1168.0		
$x_{\text{CO}_2} = 0.9794$							
6.05	662.9	39.59	920.9	75.03	1081.7	160.48	1339.2
9.85	705.2	45.15	950.4	80.36	1101.8	160.48	1339.2
14.60	750.5	50.12	975.6	89.91	1135.9	180.44	1386.1
19.65	792.4	55.18	998.8	100.30	1170.8	195.38	1419.4
24.80	830.2	60.25	1021.4	110.19	1202.0		
29.76	863.1	65.97	1045.7	120.05	1231.5		
34.69	893.2	69.77	1061.1	139.56	1285.8		
$x_{\text{CO}_2} = 0.9845$							
6.11	665.1	34.84	896.6	65.10	1044.7	110.11	1204.2
9.96	708.0	39.54	923.3	70.08	1064.9	120.77	1236.1
14.64	752.9	44.38	949.0	74.99	1084.3	139.56	1288.3
	793.3	50.19	978.0	79.96	1103.0	159.16	1338.3
24.71	831.8	54.91	1000.2	89.90	1138.5	179.47	1386.5
29.67	865.0	60.05	1023.2	100.07	1172.6		
$x_{\text{CO}_2} = 0.9898$							
54.793	1003.4	75.44	1089.5	110.07	1207.6	179.81	1390.1
59.665	1025.2	80.43	1108.3	119.47	1235.7		
64.697	1046.6	90.23	1143.0	140.15	1293.1		
70.224	1069.3	101.20	1179.7	159.52	1342.3		

Standard uncertainties: $u_T = 0.015$ K, $u_p = 0.05$ MPa, $u_x = 2 \times 10^{-6}$, $u_c^* = 5.3 \times 10^{-4}c$, $u_c = 5.9 \times 10^{-4}c$.^a

^a Rivas et al. 2016.

Table 2. Experimental speed of sound, c , in the $\text{CO}_2+\text{CH}_3\text{OH}$ system at $T = 298.15$ K and at compositions x and pressures P .

P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})
$x_{\text{CO}_2} = 0.8005$							
15.26	580.0	44.89	827.1	75.07	983.0	140.09	1212.0
19.71	629.3	49.68	855.5	80.14	1004.7	159.87	1267.4
24.87	679.9	55.49	888.8	90.51	1046.5	180.76	1321.2
29.92	722.8	60.31	913.7	99.98	1082.0		
34.98	761.4	65.06	937.3	109.95	1117.2		
39.97	795.8	70.08	960.7	120.21	1151.3		
$x_{\text{CO}_2} = 0.9025$							
14.96	550.1	39.82	772.5	65.00	915.0	109.67	1095.0
19.89	606.5	44.89	805.5	70.21	939.5	120.24	1130.1
24.84	654.9	50.08	836.4	75.28	962.3	139.48	1189.0
29.89	698.4	55.06	864.3	90.39	1024.8		
34.85	737.1	60.11	890.7	99.92	1060.7		
$x_{\text{CO}_2} = 0.9503$							
15.04	534.4	50.12	831.3	75.27	957.5	120.16	1124.7
24.90	647.1	55.04	858.9	80.29	979.0	140.53	1186.9
34.90	731.4	59.70	883.6	90.09	1018.7	159.68	1240.0
39.97	767.8	65.14	910.6	99.88	1055.4	178.78	1288.7
44.93	800.1	70.32	935.3	109.68	1090.1		
$x_{\text{CO}_2} = 0.9700$							
20.04	597.6	44.84	802.7	74.99	959.8	110.38	1096.0
24.95	649.5	50.47	836.5	80.32	982.7	120.07	1127.8
29.89	694.4	54.96	861.8	81.42	987.4	140.10	1188.7
34.82	733.7	59.78	887.3	90.50	1023.8	160.14	1244.0
39.83	769.8	64.96	913.4	99.58	1057.9	170.64	1271.3

39.88	770.1	70.20	938.2	109.40	1092.6		
$x_{\text{CO}_2} = 0.9794$							
29.87	696.2	54.88	863.6	79.93	983.2	140.07	1190.5
34.92	736.5	60.22	891.9	90.55	1026.1	159.98	1245.5
39.97	772.8	65.26	917.0	100.14	1062.0		
44.94	805.4	70.33	940.9	109.99	1096.5		
50.18	837.1	75.17	962.8	120.19	1130.2		
$x_{\text{CO}_2} = 0.9845$							
44.80	806.6	70.39	943.1	119.43	1129.2	179.95	1297.2
50.19	839.2	80.03	985.5	139.95	1191.4		
59.91	892.2	100.60	1065.3	159.48	1245.3		
$x_{\text{CO}_2} = 0.9898$							
59.98	892.6	79.93	985.0	120.25	1131.6	160.32	1247.2
65.33	919.3	89.96	1025.5	130.39	1163.1	170.19	1272.8
70.30	942.7	100.24	1063.9	140.04	1191.4		
75.33	965.3	110.18	1098.7	149.87	1219.3		

Standard uncertainties: $u_T = 0.015$ K, $u_p = 0.05$ MPa, $u_x = 2 \times 10^{-6}$, $u_c^* = 5.3 \times 10^{-4}c$, $u_c = 5.9 \times 10^{-4}c$.^a

^a Rivas et al. 2016.

Table 3. Experimental speed of sound, c , in the $\text{CO}_2+\text{CH}_3\text{OH}$ system at $T = 323.15$ K and at compositions x and pressures P .

P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})
$x_{\text{CO}_2} = 0.8005$							
24.98	558.1	60.39	832.9	80.33	932.0	120.47	1087.8
30.07	612.5	65.08	858.2	90.06	973.9	140.70	1152.8
50.04	771.9	70.16	884.0	99.72	1012.7	159.50	1207.7
55.40	804.7	75.36	909.1	110.02	1051.2	180.28	1263.6
$x_{\text{CO}_2} = 0.9025$							
24.90	538.9	50.13	750.6	80.16	910.5	140.17	1130.4
29.95	593.0	54.95	780.5	90.12	953.7	160.42	1189.3
34.91	638.4	59.87	808.9	99.79	992.4		
39.98	679.6	65.02	836.9	110.29	1031.6		
45.08	716.9	74.85	885.9	120.09	1065.9		
$x_{\text{CO}_2} = 0.9503$							
29.99	589.1	50.01	747.2	69.99	860.3	99.49	989.2
34.91	634.9	55.08	778.9	75.12	885.2	110.19	1029.1
40.04	676.9	59.73	805.8	79.95	907.6	120.29	1064.4
45.00	713.4	64.87	833.9	89.27	948.2	140.61	1129.3
$x_{\text{CO}_2} = 0.9700$							
40.00	680.0	64.94	836.9	89.99	953.5	140.13	1129.4
44.88	715.2	70.03	863.0	100.09	993.8	159.98	1186.6
50.07	750.3	74.97	887.0	109.98	1030.5	171.27	1217.0
60.02	810.1	80.16	911.0	120.04	1065.4		
$x_{\text{CO}_2} = 0.9794$							
54.47	777.7	70.33	864.4	90.57	955.8	119.81	1064.4
60.08	810.4	75.03	887.4	100.13	993.8	139.42	1127.3
65.26	838.5	80.29	911.5	109.91	1030.0	159.41	1184.4

$x_{\text{CO}_2} = 0.9845$							
69.67	860.4	89.68	951.3	120.42	1065.6	150.01	1157.4
75.24	887.4	100.05	992.7	130.13	1097.3	159.54	1184.2
80.28	910.7	110.20	1030.2	140.84	1130.4		
$x_{\text{CO}_2} = 0.9898$							
95.03	971.9	109.51	1026.6	129.94	1095.6	150.71	1158.2
99.68	990.1	119.49	1061.4	139.88	1126.3		

Standard uncertainties: $u_T = 0.015$ K, $u_p = 0.05$ MPa, $u_x = 2 \times 10^{-6}$, $u_c^* = 5.3 \times 10^{-4}c$, $u_c = 5.9 \times 10^{-4}c$.^a

^a Rivas et al. 2016.

Table 4. Coefficients of equation 7 and the mean relative deviations for the CO₂+CH₃OH mixtures at compositions x and temperatures T .

x_{CO_2}	T (K)	$10 \times a_1$	$10^4 \times a_2$	$10^8 \times a_3$	MRD_c
		(MPa m ⁻¹ s)	(MPa m ⁻² s ²)	(MPa m ⁻³ s ³)	(%)
0.8005	263.15	2.51877	2.4355	6.345	0.007
	298.15	2.17429	2.2126	7.287	0.033
	323.15	2.00343	2.1208	6.700	0.042
0.9025	263.15	2.50605	2.5074	7.390	0.004
	298.15	2.16483	2.2431	8.072	0.031
	323.15	2.00504	2.1074	6.754	0.005
0.9503	263.15	2.50388	2.5430	7.332	0.019
	298.15	2.16489	2.2715	7.399	0.012
	323.15	2.00015	2.1274	7.100	0.004
0.9700	263.15 ^a	2.50355	2.5400	7.258	0.012
	298.15	2.16314	2.2930	7.535	0.008
	323.15	2.00467	2.1435	7.613	0.009
0.9794	263.15	2.50071	2.5495	7.483	0.009
	298.15	2.16464	2.2995	7.558	0.004
	323.15	2.00334	2.1419	8.354	0.010
0.9845	263.15	2.50066	2.556	7.533	0.008
	298.15	2.16900	2.3230	7.377	0.003
	323.15	2.00545	2.1602	7.498	0.001
0.9898	263.15	2.50598	2.5363	8.680	0.004
	298.15	2.16843	2.3351	7.289	0.006
	323.15	2.06645	1.8687	12.67	0.003

Overall mean relative deviation: $\overline{MRD}_c=0.012\%$.

$MRD_c(\%) = \frac{100}{N} \sum_i^N \left| \frac{c_i - c_{i,fit}}{c_i} \right|$; $\overline{MRD}_c(\%) = \frac{100}{N'} \sum_{i=1}^{N'} \left| \frac{c_i - c_{i,fit}}{c_i} \right|$. c_i : experimental datum; $c_{i,fit}$: value obtained for the property at the same state point from the correlating equation 7; N : number of points for each isopleth and isotherm; N' : total number of points.

^aRivas et al. 2016.

Table 5. Experimental speed of sound, c , in the CO_2+SO_2 mixture with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P .

P (MPa)	c (m s ⁻¹)	P (MPa)	c (m s ⁻¹)	P (MPa)	c (m s ⁻¹)	P (MPa)	c (m s ⁻¹)
$T = 263.15$ K							
7.99	763.3	30.00	915.7	55.00	1037.4	80.00	1132.9
9.99	780.2	35.00	943.1	60.00	1059.4	85.00	1149.9
14.99	820.2	40.00	968.8	65.00	1078.0	90.00	1166.5
20.00	855.5	45.00	992.8	70.00	1096.9	95.00	1182.4
25.00	886.2	50.00	1015.6	75.00	1115.2		
$T = 273.15$ K							
17.99	785.1	40.00	923.2	65.00	1038.9	90.00	1131.3
19.99	800.5	45.00	949.1	70.00	1058.8	95.00	1147.9
25.00	836.0	50.00	973.3	75.00	1078.0	99.99	1163.8
30.00	866.0	55.00	996.2	80.00	1096.4		
34.99	895.6	60.00	1018.1	85.00	1114.2		
$T = 293.15$ K							
31.03	778.4	55.00	917.5	80.00	1026.9	105.00	1116.1
34.99	805.5	60.01	941.6	85.00	1046.0	110.00	1132.3
39.98	837.6	65.00	964.4	90.00	1064.5	115.01	1148.0
44.99	866.2	70.00	986.2	95.00	1082.2		
49.99	893.3	75.00	1007.0	100.00	1099.4		
$T = 304.16$ K							
45.97	828.7	65.03	925.9	90.00	1029.8	115.01	1115.9
50.00	851.7	69.99	950.5	95.00	1048.3	119.99	1131.8
55.00	878.6	75.00	972.1	100.00	1066.1		
59.98	903.8	79.99	990.9	105.00	1083.3		
65.00	927.7	85.00	1010.7	110.00	1099.9		
$T = 313.15$ K							

62.01	882.4	79.99	962.9	100.00	1039.8	120.00	1107.1
64.99	897.1	84.99	983.3	105.00	1057.5	124.99	1122.5
69.99	920.5	90.00	1002.8	110.00	1074.5		
74.99	943.1	95.00	1021.7	115.00	1091.0		
$T = 333.15 \text{ K}$							
80.99	909.6	105.00	1003.7	120.00	1055.4	132.49	1095.1
85.00	926.8	110.00	1021.4	122.50	1063.6	135.00	1102.9
90.00	947.5	112.51	1030.1	125.00	1071.7		
94.99	967.5	115.00	1040.0	127.50	1079.6		
99.99	986.5	117.50	1047.1	130.00	1087.5		
$T = 353.15 \text{ K}$							
97.99	929.4	113.99	988.7	127.99	1036.3	138.00	1066.7
100.00	936.7	116.00	995.8	129.98	1041.4	140.00	1072.7
101.97	944.4	118.00	1002.7	132.00	1049.1	142.01	1078.9
103.99	952.1	120.00	1009.5	132.49	1049.4	144.00	1084.8
106.01	959.7	122.00	1016.3	133.97	1054.0	145.01	1087.2
108.00	967.1	124.00	1023.0	134.96	1057.3		
109.98	974.3	126.00	1028.4	136.01	1060.4		
111.99	981.6	127.48	1033.3	137.49	1065.0		
$T = 373.19 \text{ K}$							
112.49	940.4	125.00	984.6	135.00	1017.7	144.00	1044.3
115.00	949.7	127.51	993.1	135.99	1019.3	145.99	1050.4
117.50	958.5	129.99	1001.3	138.00	1027.1	148.00	1056.4
119.99	967.3	132.49	1009.6	140.00	1032.0	150.00	1062.3
122.50	976.1	133.98	1012.9	141.98	1038.1		

Standard uncertainties: $u_T = 0.015 \text{ K}$, $u_p = 0.05 \text{ MPa}$, $u_x = 1 \times 10^{-6}$, $u_c^* = 6.2 \times 10^{-4} c$, $u_c = 6.2 \times 10^{-4} c$.

Table 6. Experimental speed of sound, c , in the $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ mixture with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P .

P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})	P (MPa)	c (m s^{-1})
$T = 263.15$ K							
8.00	754.8	39.98	965.8	74.98	1113.2	140.00	1308.4
9.99	772.9	44.97	990.0	79.95	1131.1	149.97	1333.0
14.99	813.7	49.97	1013.0	89.98	1164.8	160.00	1357.0
19.95	849.5	54.96	1034.8	99.98	1196.7	170.03	1379.9
24.97	882.2	59.98	1055.8	110.00	1226.7	180.03	1402.2
29.97	912.0	65.00	1075.7	119.96	1255.1	190.00	1423.4
35.01	939.9	69.99	1094.9	129.97	1282.3		
$T = 273.15$ K							
17.97	777.7	49.96	970.7	84.98	1112.3	140.00	1278.1
20.01	794.0	54.97	993.9	89.98	1130.1	149.92	1303.1
24.95	829.6	59.98	1015.9	99.98	1162.5	160.00	1328.2
30.00	862.7	64.97	1036.8	109.95	1193.8	169.96	1351.6
34.97	892.4	70.01	1056.8	114.99	1208.5	179.99	1374.5
40.02	919.4	74.95	1076.2	119.97	1223.4	189.95	1396.0
45.00	946.6	79.98	1094.8	129.98	1251.0		
$T = 293.15$ K							
34.98	801.0	64.98	962.8	110.01	1131.8	169.97	1297.5
40.00	833.1	69.99	984.7	119.98	1162.8	180.01	1321.2
45.00	862.6	75.01	1005.7	129.96	1192.3	189.99	1344.0
49.97	889.8	79.97	1025.9	139.96	1220.3		
54.96	915.4	89.99	1063.8	149.99	1247.2		
59.98	939.7	100.00	1098.8	159.97	1272.8		
$T = 304.16$ K							
47.06	830.9	70.00	947.0	109.98	1099.2	159.99	1244.1

50.02	847.3	74.99	968.8	119.98	1131.2	169.98	1269.2
54.98	874.5	79.95	989.4	130.01	1161.6	179.99	1293.6
59.99	900.0	89.99	1028.9	139.99	1190.2	189.99	1316.8
65.00	924.0	100.01	1065.4	150.00	1217.6		
$T = 313.15 \text{ K}$							
54.92	843.3	79.99	961.6	129.97	1137.4	179.98	1271.7
60.01	869.2	89.95	1001.5	139.99	1166.8	189.98	1295.2
65.04	894.2	99.96	1039.0	149.93	1194.2		
69.98	917.9	109.95	1073.8	159.94	1221.2		
75.00	940.3	120.01	1106.7	169.95	1247.1		
$T = 333.15 \text{ K}$							
69.98	856.2	100.03	984.9	140.02	1117.6	180.01	1226.2
74.94	880.1	110.04	1021.0	149.98	1146.6	189.97	1250.5
79.99	903.0	119.96	1055.0	159.99	1174.4		
89.98	945.3	130.00	1087.3	169.96	1200.7		
$T = 353.15 \text{ K}$							
84.98	872.7	109.97	972.8	134.99	1057.4	170.00	1158.2
90.00	894.4	115.00	991.0	139.97	1072.6	179.93	1184.1
95.00	915.1	119.99	1008.1	144.96	1087.8	190.10	1209.3
100.00	935.1	124.97	1025.0	149.96	1102.5		
105.00	954.3	130.00	1041.3	160.01	1131.0		
$T = 373.19 \text{ K}$							
99.99	890.5	119.98	965.4	139.95	1031.6	169.95	1119.1
104.96	910.2	124.96	982.7	145.02	1047.2	179.93	1145.5
110.01	929.3	129.96	999.5	150.00	1062.2	189.94	1171.2
115.04	947.7	134.96	1015.9	159.93	1091.2		

Standard uncertainties: $u_T = 0.015 \text{ K}$, $u_p = 0.05 \text{ MPa}$, $u_x = 2 \times 10^{-6}$, $u_c^* = 8.1 \times 10^{-4} c$, $u_c = 8.1 \times 10^{-4} c$.

Table 7. Coefficients and $P^\#$ of equation 7 along with the mean relative deviations for the CO_2+SO_2 mixture with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T .

T (K)	$P^\#$ (MPa)	$10 \times a_1$ (MPa $\text{m}^{-1} \text{s}$)	$10^4 \times a_2$ (MPa $\text{m}^{-2} \text{s}^2$)	$10^8 \times a_3$ (MPa $\text{m}^{-3} \text{s}^3$)	MRD_c (%)
263.15	30.00	1.76485	2.2533	10.30	0.030
273.15	30.00	1.64259	2.0347	11.88	0.019
293.15	50.00	1.92170	2.3548	4.024	0.025
304.16	65.00	2.17783	2.5527	-1.847	0.027
313.15	80.00	2.42432	2.3997	6.009	0.020
333.15	100.00	2.70016	2.6889	-1.251	0.022
353.15	110.00	2.78887	2.7460	14.29	0.027
373.19	120.00	2.86153	3.7143	-51.84	0.030

Overall mean relative deviation $\overline{MRD}_c = 0.025\%$.

$MRD_c(\%) = \frac{100}{N} \sum_i^N \left| \frac{c_i - c_{i,fit}}{c_i} \right|$; $\overline{MRD}_c(\%) = \frac{100}{N'} \sum_{i=1}^{N'} \left| \frac{c_i - c_{i,fit}}{c_i} \right|$. c_i : experimental datum; $c_{i,fit}$: value obtained for the property at the same state point from the correlating equation 7; N : number of points for each isotherm; N' : total number of points.

Table 8. Coefficients and $P^\#$ of equation 7 along with the mean relative deviations for the $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ mixture with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T .

T (K)	$P^\#$ (MPa)	$10 \times a_1$ (MPa m ⁻¹ s)	$10^4 \times a_2$ (MPa m ⁻² s ²)	$10^8 \times a_3$ (MPa m ⁻³ s ³)	MRD_c (%)
263.15	50.00	2.22847	2.5432	8.303	0.009
273.15	50.00	2.10376	2.4528	7.911	0.017
293.15	80.00	2.54506	2.5949	8.365	0.006
304.16	90.00	2.65293	2.6121	8.018	0.008
313.15	95.00	2.68592	2.5895	8.536	0.015
333.15	100.00	2.65349	2.5408	7.572	0.007
353.15	120.00	2.92232	2.6115	8.911	0.005
373.19	125.00	2.93618	2.5359	9.762	0.006

Overall mean relative deviation $\overline{MRD}_c = 0.010\%$.

$MRD_c(\%) = \frac{100}{N} \sum_i^N \left| \frac{c_i - c_{i,fit}}{c_i} \right|$; $\overline{MRD}_c(\%) = \frac{100}{N'} \sum_{i=1}^{N'} \left| \frac{c_i - c_{i,fit}}{c_i} \right|$. c_i : experimental datum; $c_{i,fit}$: value obtained for the property at the same state point from the correlating equation 7; N : number of points for each isotherm; N' : total number of points.

Table 9. Speed of sound in the CO₂+CH₃OH mixtures calculated using equation (7), c_{fit} , and the coefficients of equation (8), c_i , at temperatures T and at pressures P . c_0 is the derived speed of sound in pure CO₂, and $u_r(c_0)$ is the standard relative uncertainty of c_0 . Italicized figures are extrapolated values.

T (K)	P (MPa)	c_{fit} (m s ⁻¹)					c_0 (m s ⁻¹)	c_1 (m s ⁻¹)	c_2 (m s ⁻¹)	$u_r(c_0)$ (%)
		$x_{CO_2} =$								
		0.9503	0.9700 ^a	0.9794	0.9845	0.9898				
263.15	8	684.93	684.73	685.50	687.00		691.61	-387	5087	0.24
	10	706.15	705.96	706.87	708.57		713.82	-440	5753	0.25
	15	753.13	752.97	754.14	756.18		762.63	-538	6985	0.26
	25	830.13	829.98	831.53	833.92		841.81	-654	8437	0.25
	35	893.30	893.16	894.95	897.51	902.28	910.43	-994	13118	0.08
	50	972.48	972.34	974.35	977.02	980.95	988.79	-927	12092	0.16
	60	1018.25	1018.11	1020.21	1022.90	1026.61	1034.38	-911	11826	0.13
	70	1059.93	1059.80	1061.95	1064.65	1068.24	1075.98	-902	11679	0.12
	75	1079.51	1079.38	1081.55	1084.25	1087.80	1095.53	-899	11626	0.12
	80	1098.35	1098.23	1100.41	1103.11	1106.63	1114.35	-896	11578	0.12
	100	1167.60	1167.50	1169.70	1172.37	1175.81	1183.43	-883	11383	0.11
	120	1229.13	1229.05	1231.23	1233.84	1237.20	1244.67	-864	11118	0.10
	125	1243.54	1243.47	1245.63	1248.24	1251.57	1258.99	-858	11038	0.10
	140	1284.81	1284.76	1286.88	1289.44	1292.67	1299.93	-838	10762	0.10
	150	1310.86	1310.83	1312.92	1315.45	1318.60	1325.73	-823	10550	0.10
	160	1335.88	1335.87	1337.91	1340.42	1343.48	1350.47	-805	10318	0.10
	175	1371.69	1371.70	1373.69	1376.15	1379.06	1385.82	-777	9935	0.10
180	1383.21	1383.23	1385.19	1387.64	1390.49	1397.18	-767	9799	0.09	
200	1427.43	1427.48	1429.35	1431.73	1434.35	1440.69	-724	9216	0.09	
298.15	25	648.39	650.03	652.10	652.94		657.66	-346	3214	0.19
	35	732.30	734.96	737.12	738.89	738.29	740.74	-183	219	0.27
	50	830.58	833.85	836.02	838.07	837.87	840.73	-236	619	0.21
	60	885.13	888.56	890.71	892.73	892.62	895.42	-234	512	0.19

70	933.76	937.26	939.38	941.32	941.24	943.92	-222	330	0.18	
75	956.32	959.83	961.93	963.83	963.75	966.35	-215	230	0.17	
80	977.88	981.39	983.48	985.32	985.24	987.77	-207	130	0.16	
100	1056.03	1059.48	1061.49	1063.13	1063.01	1065.23	-175	-238	0.15	
120	1124.27	1127.60	1129.55	1130.99	1130.83	1132.76	-146	-528	0.14	
125	1140.13	1143.42	1145.35	1146.75	1146.57	1148.45	-139	-587	0.13	
140	1185.28	1188.45	1190.34	1191.62	1191.40	1193.11	-122	-738	0.13	
150	1213.62	1216.71	1218.56	1219.77	1219.53	1221.14	-112	-817	0.13	
160	1240.73	1243.73	1245.55	1246.70	1246.43	1247.95	-103	-880	0.12	
175	1279.35	1282.22	1284.00	1285.06	1284.76	1286.17	-91	-948	0.12	
180	1291.73	1294.56	1296.32	1297.35	1297.05	1298.42	-88	-964	0.12	
200	1339.10	1341.75	1343.46	1344.39	1344.05	1345.31	-77	-1002	0.12	
<hr/>										
323.15	50	747.17	749.99	749.95	749.08	745.36	341	-6138	0.14	
	60	807.33	810.01	809.96	809.20	805.73	317	-5739	0.12	
	70	860.25	862.82	862.80	862.01	862.45	860.77	170	-3615	0.14
	75	884.61	887.12	887.12	886.30	886.13	884.01	308	-4557	0.11
	80	907.80	910.26	910.26	909.41	908.84	906.41	285	-5180	0.08
	100	991.20	993.39	993.39	992.45	991.30	988.44	350	-5935	0.10
	120	1063.37	1065.26	1065.15	1064.20	1063.07	1060.24	343	-5649	0.09
	125	1080.07	1081.88	1081.72	1080.79	1079.66	1076.85	340	-5547	0.09
	140	1127.49	1129.05	1128.75	1127.89	1126.72	1123.96	333	-5287	0.09
	150	1157.16	1158.55	1158.14	1157.34	1156.09	1153.32	334	-5181	0.09
	160	1185.49	1186.70	1186.16	1185.45	1184.06	1181.25	341	-5147	0.09
	175	1225.77	1226.71	1225.95	1225.40	1223.68	1220.75	361	-5235	0.10
	180	1238.66	1239.51	1238.68	1238.19	1236.32	1233.34	370	-5301	0.10
	200	1287.91	1288.39	1287.23	1287.00	1284.45	1281.15	420	-5745	0.13

Overall standard relative uncertainty of c_0 , $\overline{u_r(c_0)}=0.12\%$.

Standard uncertainty of c : $u_c = 5.9 \times 10^{-4} c$. $\overline{u_r(c_0)} = \frac{1}{N} \sum_i^N u_r(c_0)_i$; N : number of pressures in Table 9.

^aAt 263.15 K, experimental data from Rivas et al. 2016. ^bRivas et al. 2016.

Table 10. Comparison between the experimental $P - c - T - x_{\text{CO}_2}$ data for the $\text{CO}_2 + \text{CH}_3\text{OH}$ mixtures studied in this work and those calculated using the PC-SAFT EoS and the REFPROP 9 software, at temperatures T .

x_{CO_2}	MRD_c (%)		MRD_c (%)		MRD_c (%)	
	$T = 263.15 \text{ K}$		$T = 298.15 \text{ K}$		$T = 323.15 \text{ K}$	
	PC-SAFT	REFPROP 9	PC-SAFT	REFPROP 9	PC-SAFT	REFPROP 9
0.8005	2.12	11.7	2.09	12.9	2.16	11.0
0.9025	2.56	7.12	1.60	7.65	1.57	6.49
0.9503	2.82	4.95	2.05	4.23	1.55	3.16
0.9700	3.08	3.62	2.61	2.29	2.56	1.40
0.9794	3.98	2.15	3.22	1.34	2.95	0.86
0.9845	4.32	1.55	3.66	0.85	3.09	0.74
0.9898	5.01	0.80	3.86	0.64	3.15	0.65

Overall mean relative deviations $\overline{MRD}_c = 2.83\%$ for PC-SAFT and 4.97% for GERG

$MRD_c(\%) = \frac{100}{N} \sum_{i=1}^N \left| \frac{c_{i,\text{model}} - c_{i,\text{exp}}}{c_{i,\text{exp}}} \right|$; $\overline{MRD}_c(\%) = \frac{100}{N'} \sum_{i=1}^{N'} \left| \frac{c_{i,\text{model}} - c_{i,\text{exp}}}{c_{i,\text{exp}}} \right|$. $c_{i,\text{exp}}$: experimental values; $c_{i,\text{model}}$: values calculated using the PC-SAFT EoS or the REFPROP 9 software; N : number of points for each isotherm and isopleth; N' : total number of points.

Table 11. Comparison between the experimental $P - c - T$ data for the $\text{CO}_2 + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8969, x_{\text{SO}_2} = 0.1031$) and $\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8889, x_{\text{CH}_3\text{OH}} = 0.0080, x_{\text{SO}_2} = 0.1031$) mixtures studied in this work and those calculated using the PC-SAFT EoS and the REFPROP 9 software at temperatures T . The ternary mixture was modeled as a ternary (a) and binary mixture of composition $x_{\text{CO}_2} = 0.8969, x_{\text{SO}_2} = 0.1031$ (b).

	MRD_c (%)		MRD_c (%)		MRD_c (%)	
	$\text{CO}_2 + \text{SO}_2$		$\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ (a)		$\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ (b)	
T (K)	PC-SAFT	REFPROP 9	PC-SAFT	REFPROP 9	PC-SAFT	REFPROP 9
263.15	2.52	3.19	4.32	2.16	2.83	1.86
273.15	2.32	2.51	4.04	1.66	2.66	1.44
293.15	2.14	1.43	3.49	1.14	2.36	1.02
304.16	2.23	0.92	3.20	0.89	2.29	0.84
313.15	2.28	0.53	3.00	0.75	2.27	0.79
333.15	2.20	0.53	2.55	0.70	2.12	0.96
353.15	2.04	0.87	2.16	0.96	1.94	1.25
373.19	1.88	1.12	1.77	1.23	1.76	1.51
\overline{MRD}_c (%)	2.19	1.39	3.24	1.28	2.35	1.26

$$MRD_c(\%) = \frac{100}{N} \sum_{i=1}^N \left| \frac{c_{i,\text{model}} - c_{i,\text{exp}}}{c_{i,\text{exp}}} \right|; \overline{MRD}_c(\%) = \frac{100}{N'} \sum_{i=1}^{N'} \left| \frac{c_{i,\text{model}} - c_{i,\text{exp}}}{c_{i,\text{exp}}} \right|. c_{i,\text{exp}}: \text{experimental values}; c_{i,\text{model}}:$$

values calculated using the PC-SAFT EoS or the REFPROP 9 software; N : number of points for each mixture and isotherm; N' : total number of points for each mixture.

Figure 1. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9503$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

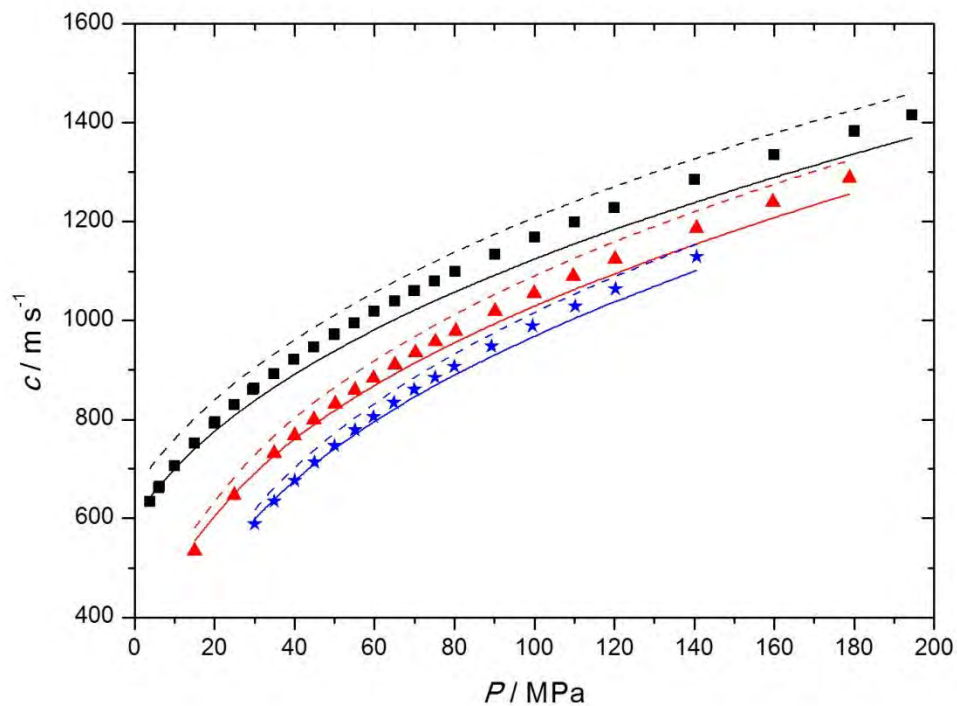


Figure 2. Relative deviations of the experimental speed of sound, c , from the values obtained from equation (7), c_{fit} , for all experimental points of the studied $\text{CO}_2+\text{CH}_3\text{OH}$ mixtures. \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. The deviations of the data used in the section 5.1 range between -0.05% and $+0.08\%$ (dotted lines).

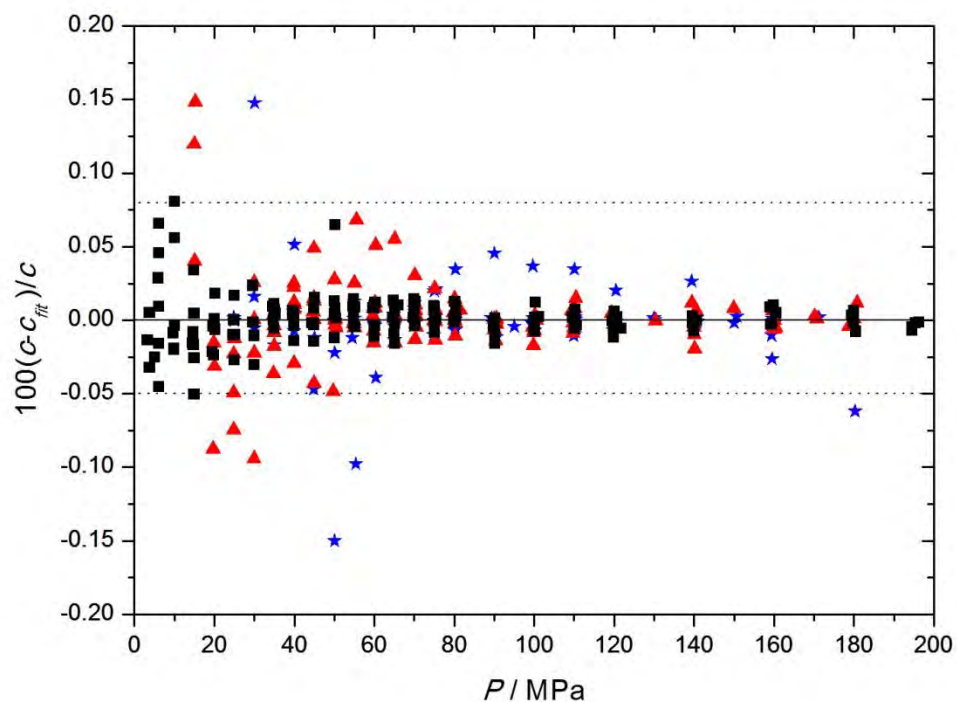


Figure 3. Speed of sound, c , in CO_2+SO_2 with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 293.15$ K; \blacktriangledown , $T = 333.15$ K; \blackstar , $T = 373.19$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

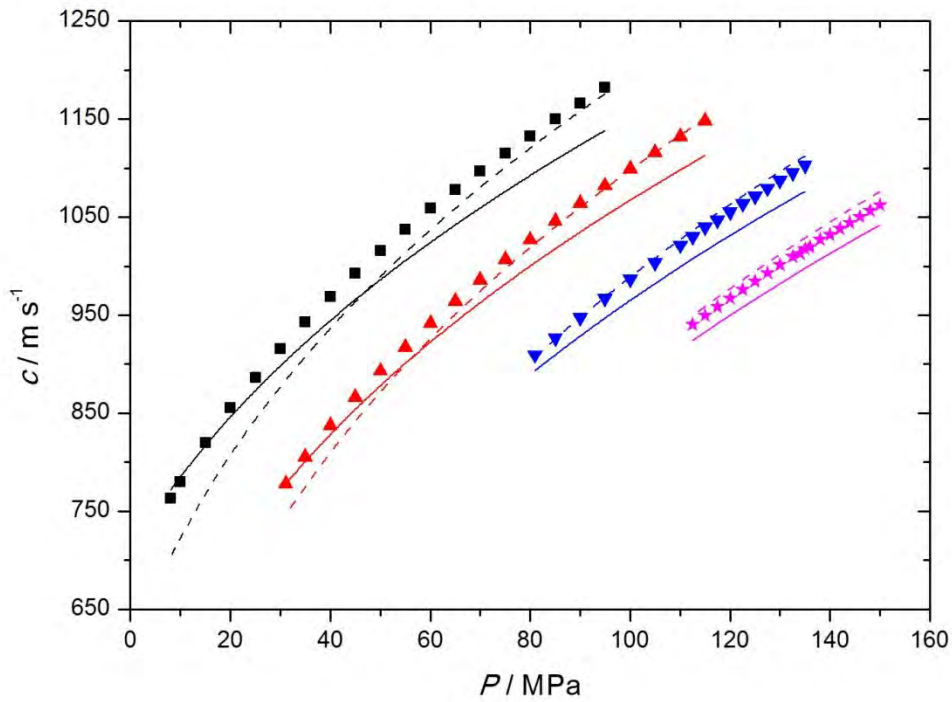


Figure 4. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 293.15$ K; \blacktriangledown , $T = 333.15$ K; \blackstar , $T = 373.19$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software; system modeled as a binary mixture with $x_{\text{CO}_2} = 0.8989$, $x_{\text{SO}_2} = 0.1031$.

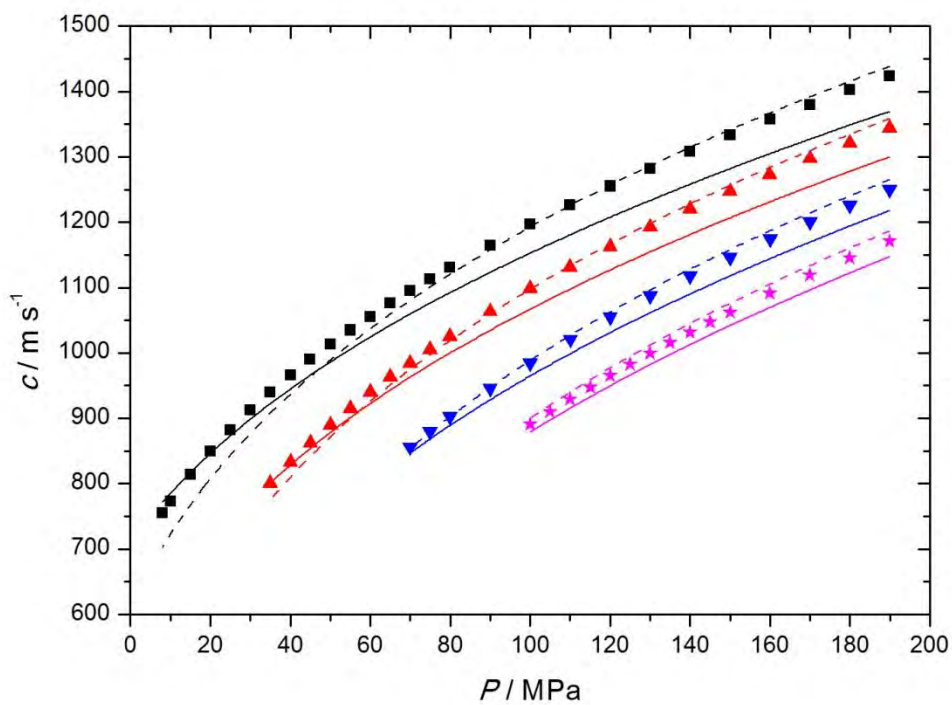


Figure 5. Speed of sound, c , in pure CO₂ versus pressure, P , at temperatures T . ■, $T = 263.15$ K; ▲, $T = 298.15$ K; ★, $T = 323.15$ K.

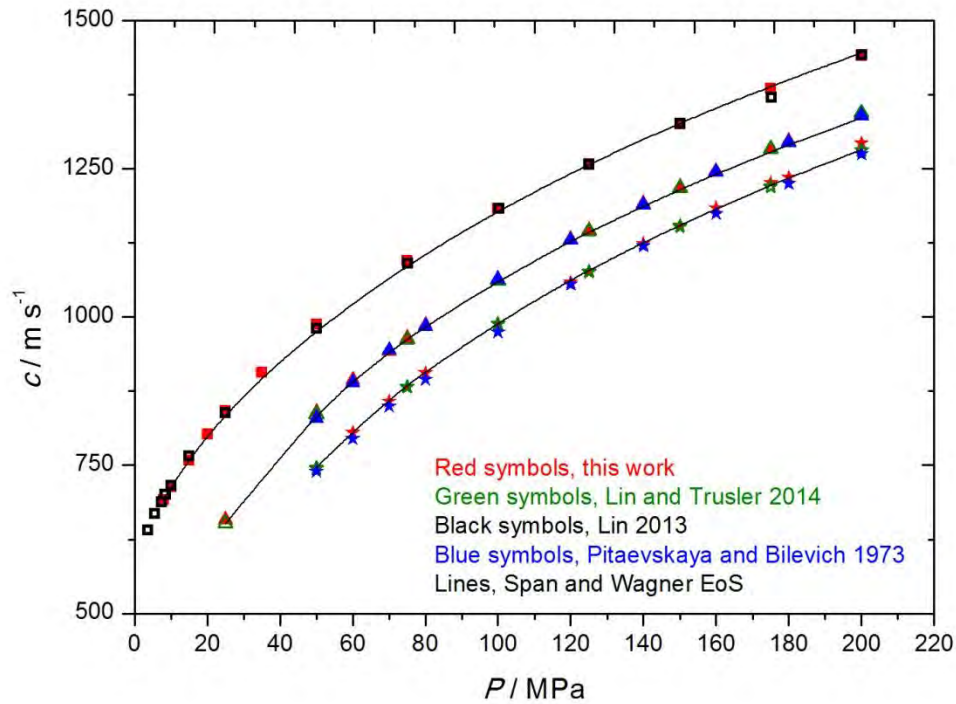


Figure 6. Speed of sound, c , in pure CO₂ versus temperature, T , at pressures P . ■, $P = 8$ MPa; □, $P = 15$ MPa; ●, $P = 25$ MPa; ▲, $P = 50$ MPa; △, $P = 75$ MPa; ▼, $P = 100$ MPa; ▽, $P = 125$ MPa; ◆, $P = 150$ MPa; ◇, $P = 175$ MPa; ★, $P = 200$ MPa.

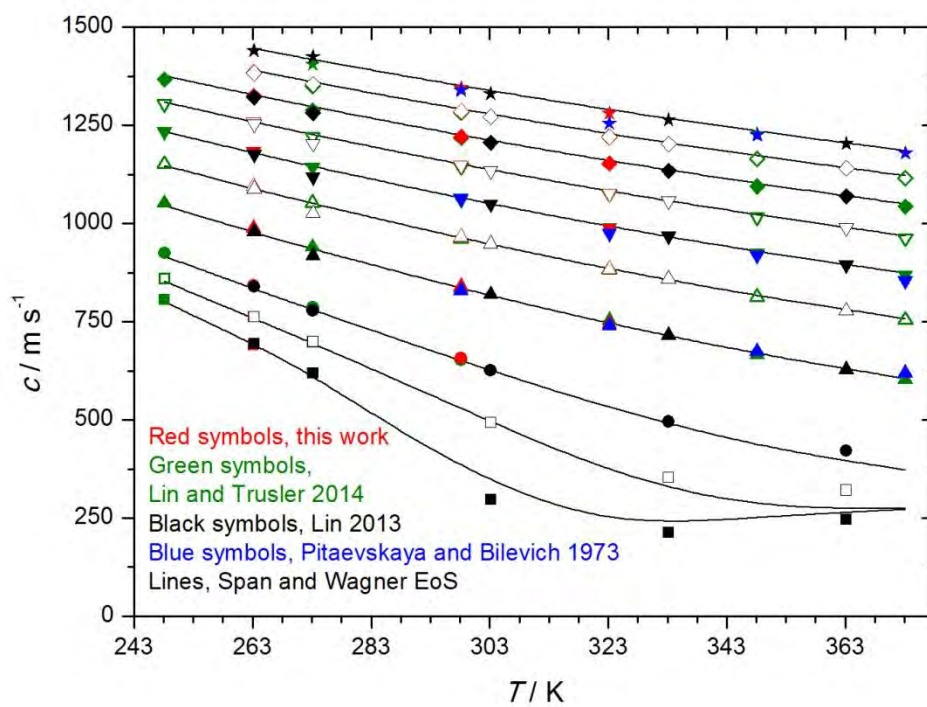


Figure 7. Relative deviations of the speed of sound in pure CO₂ obtained in this work and those in the literature, c , from the values obtained using the Span and Wagner EoS, c_{EoS} . ■, $T = 263.15$ K; ▲, $T = 298.15$ K; ★, $T = 323.15$ K.

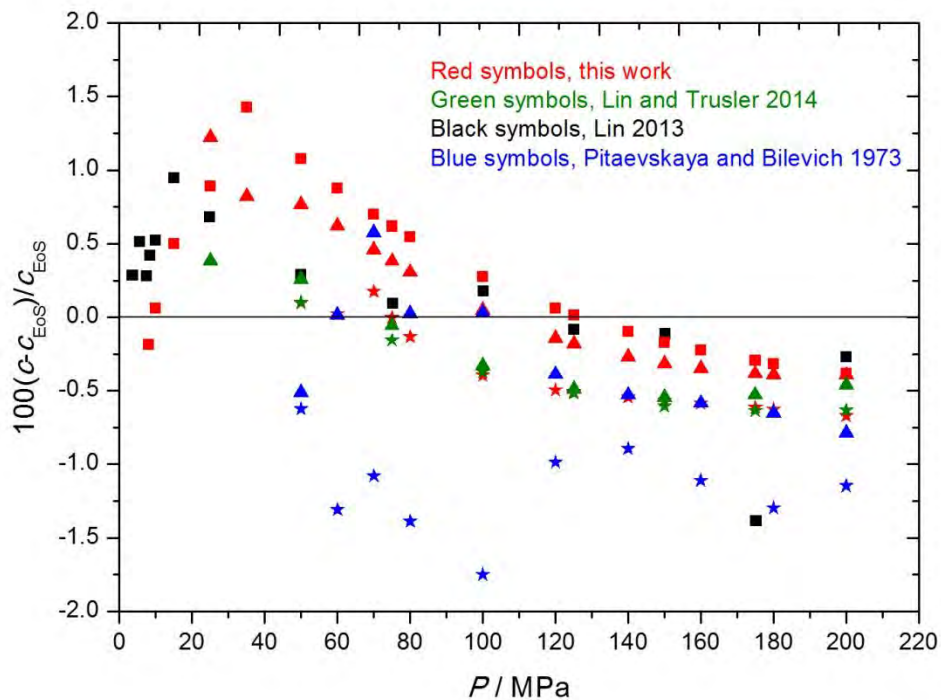


Figure 8. Relative deviations of the experimental speed of sound in CO₂+CH₃OH mixtures in this work, c , from the speed of sound in pure CO₂ calculated by the Span and Wagner EoS, c_{EoS} . ★, $x_{\text{CO}_2} = 0.9503$; ◆, $x_{\text{CO}_2} = 0.9700$; ▲, $x_{\text{CO}_2} = 0.9794$; ●, $x_{\text{CO}_2} = 0.9845$; ■, $x_{\text{CO}_2} = 0.9898$. Deviations when doping with 1% of methanol lie between the dotted lines.

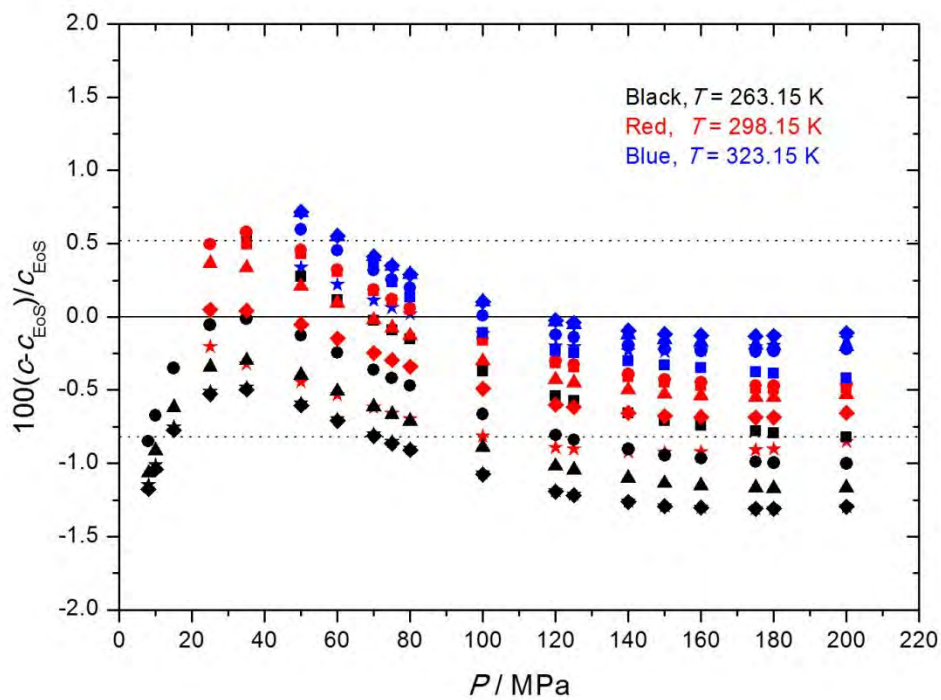


Figure 9. Correlation of the speed of sound calculated with equation (7), c_{fit} , as a function of the CO₂ mole fraction, x_{CO_2} , for the CO₂+CH₃OH mixtures at the three studied temperatures and at several pressures (equation 8, Table 9). ■, $P = 50$ MPa; ▲, $P = 100$ MPa; ◆, $P = 150$ MPa; ★, $P = 200$ MPa. Black, $T = 263.15$ K; red, $T = 298.15$ K; blue, $T = 323.15$ K.

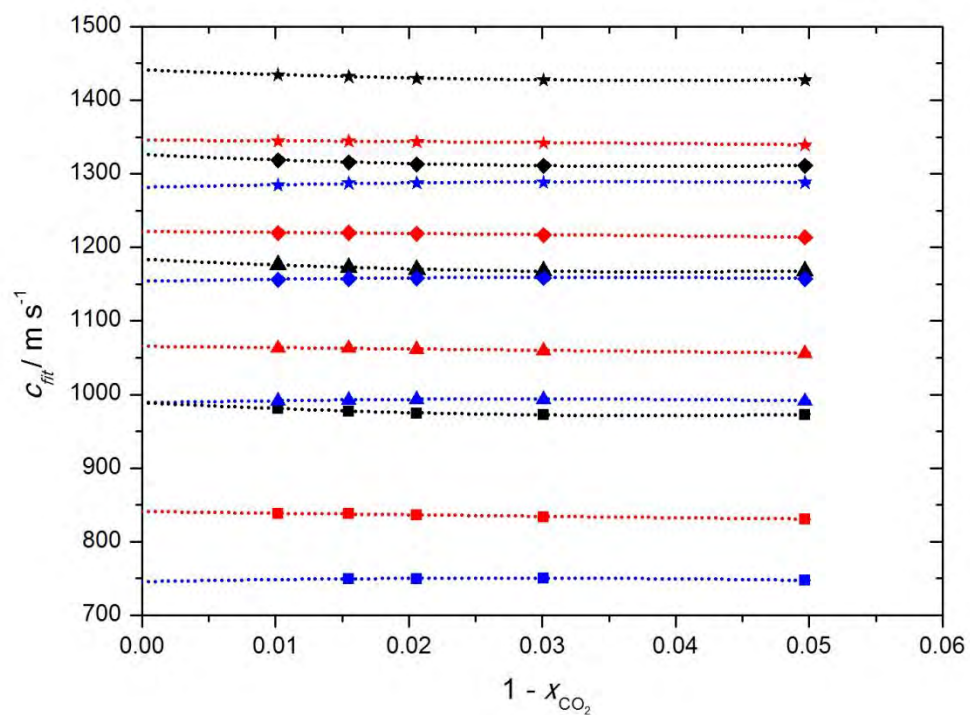


Figure 10. Relative deviations between the $P - c - T$ data in this work for the binary (c_{bin}) $\text{CO}_2 + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8969, x_{\text{SO}_2} = 0.1031$) and the ternary (c_{ter}) $\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8889, x_{\text{CH}_3\text{OH}} = 0.0080, x_{\text{SO}_2} = 0.1031$) mixtures at temperatures T and pressures P . ■, $T = 263.15$ K; ●, $T = 273.15$ K; ▲, $T = 293.15$ K; ◆, $T = 304.16$ K; ▶, $T = 313.15$ K; ▼, $T = 333.15$ K; ◀, $T = 353.15$ K; ★, $T = 373.19$ K. Solid symbols, correlated data; empty symbols, extrapolated data (equation 7, Tables 7 and 8).

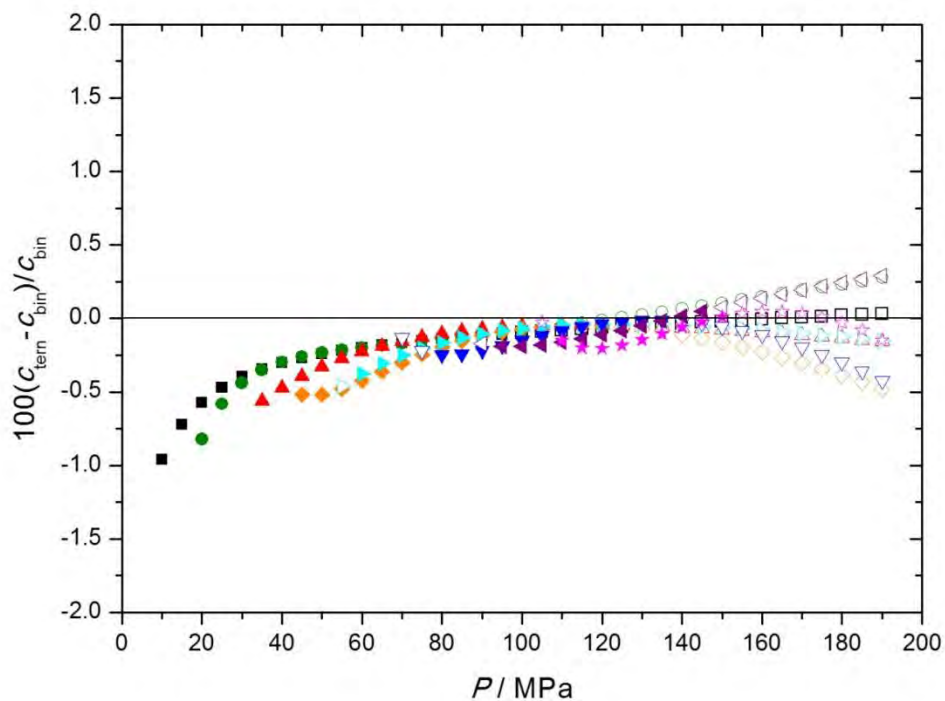


Figure 1. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9503$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

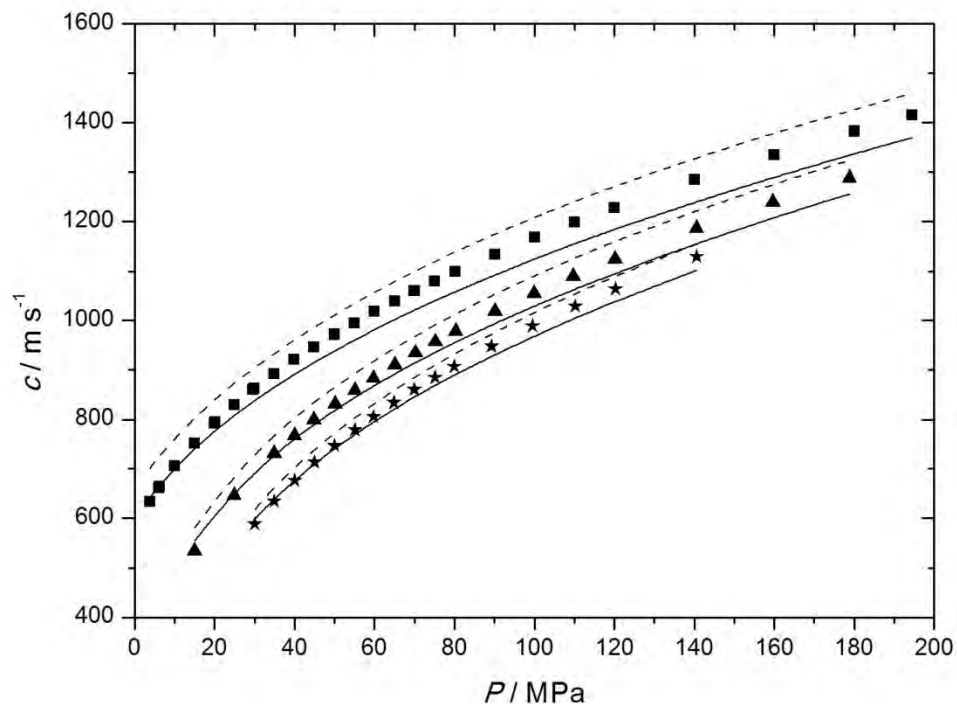


Figure 2. Relative deviations of the experimental speed of sound, c , from the values obtained from equation (7), c_{fit} , for all experimental points of the studied $\text{CO}_2+\text{CH}_3\text{OH}$ mixtures. \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. The deviations of the data used in the section 5.1 range between -0.05% and $+0.08\%$ (dotted lines).

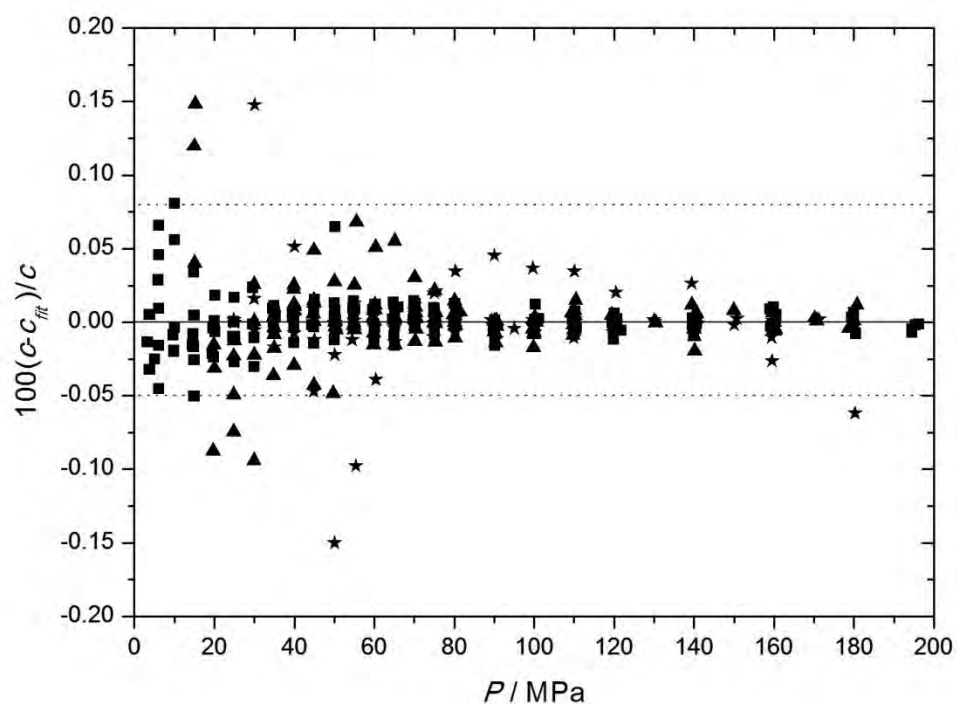


Figure 3. Speed of sound, c , in CO_2+SO_2 with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 293.15$ K; \blacktriangledown , $T = 333.15$ K; \star , $T = 373.19$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

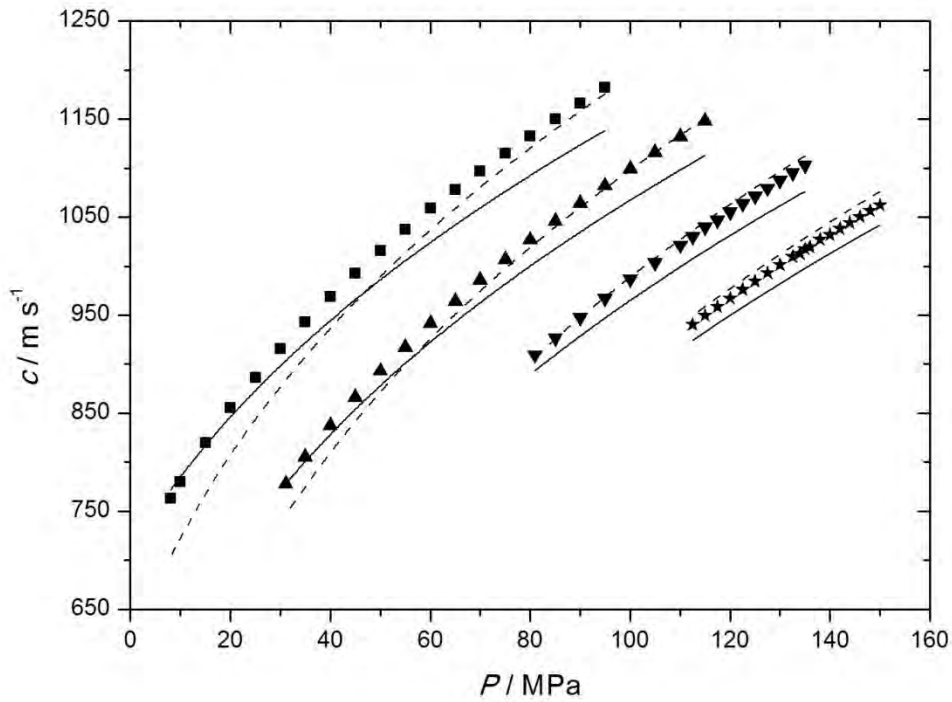


Figure 4. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 293.15$ K; \blacktriangledown , $T = 333.15$ K; \star , $T = 373.19$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software; system modeled as a binary mixture with $x_{\text{CO}_2} = 0.8989$, $x_{\text{SO}_2} = 0.1031$.

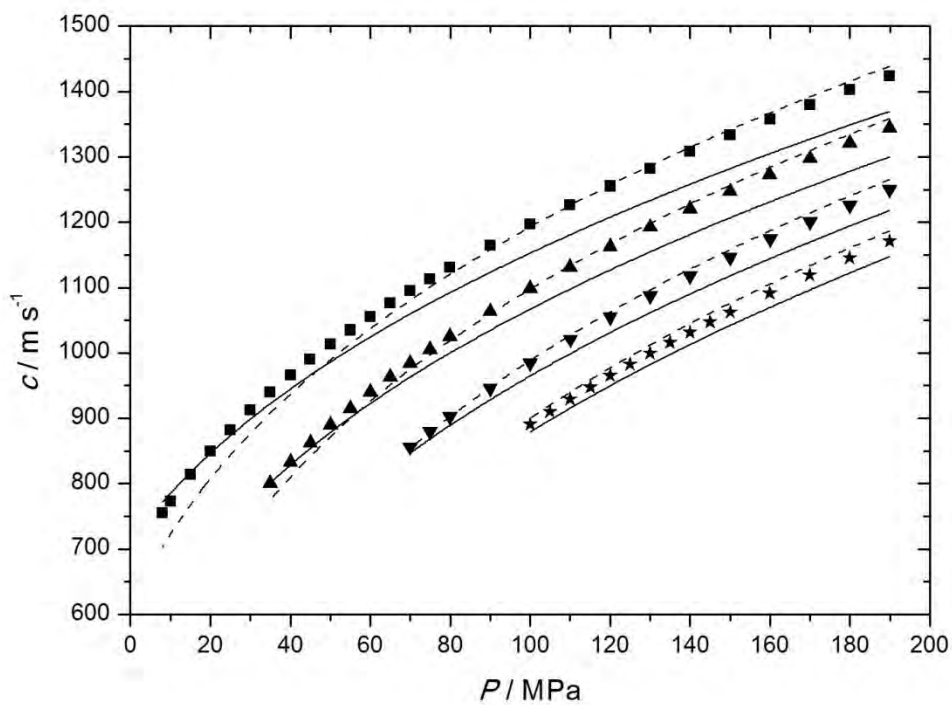


Figure 5. Speed of sound, c , in pure CO₂ versus pressure, P , at temperatures T . \square , $T = 263.15$ K; \triangle , $T = 298.15$ K; \circ , $T = 323.15$ K.

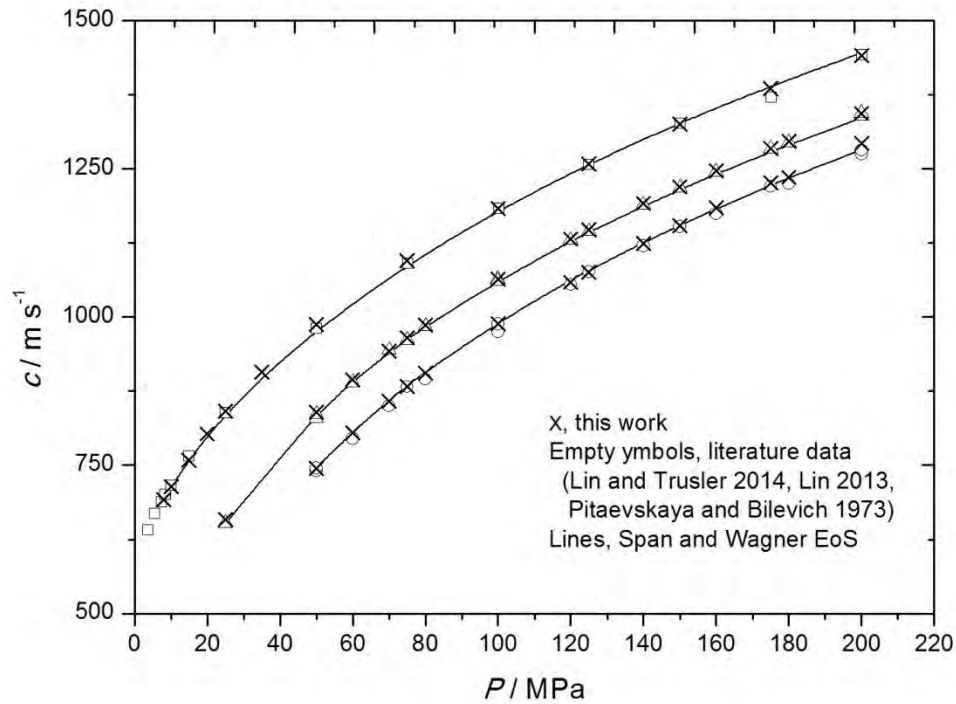


Figure 6. Speed of sound, c , in pure CO₂ versus temperature, T , at pressures P . \square , $P = 8$ MPa; \circ , $P = 15$ MPa; \triangle , $P = 25$ MPa; ∇ , $P = 50$ MPa; \diamond , $P = 75$ MPa; \triangleleft , $P = 100$ MPa; \triangleright , $P = 125$ MPa; \oplus , $P = 150$ MPa; \star , $P = 175$ MPa; \boxtimes , $P = 200$ MPa.

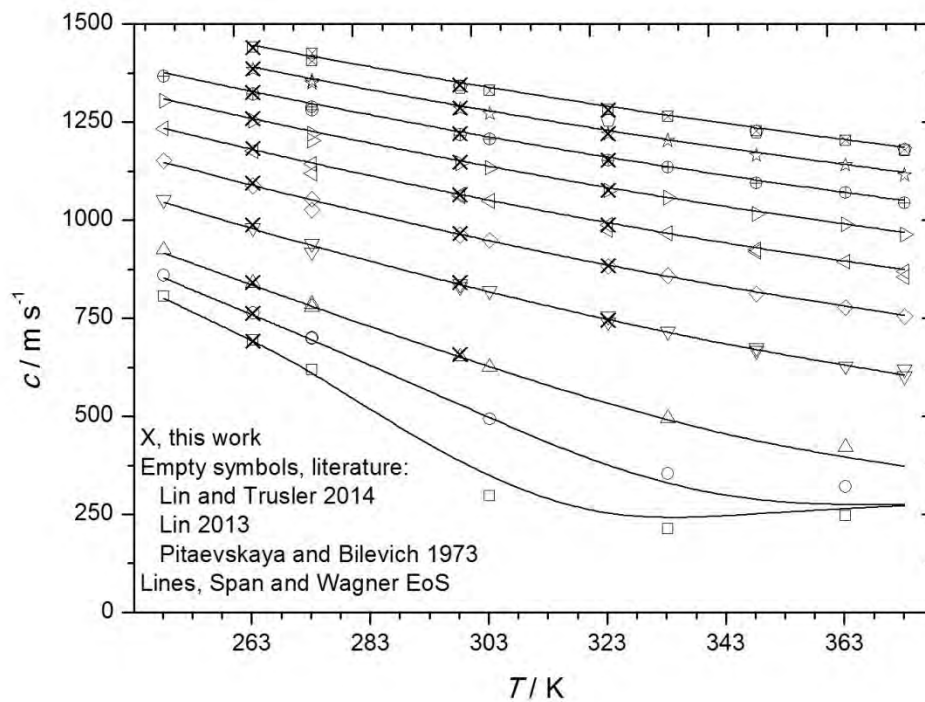


Figure 7. Relative deviations of the speed of sound in pure CO₂ obtained in this work and those in the literature, c , from the values obtained using the Span and Wagner EoS, c_{EoS} . \square , $T = 263.15$ K; \triangle , $T = 298.15$ K; \circ , $T = 323.15$ K.

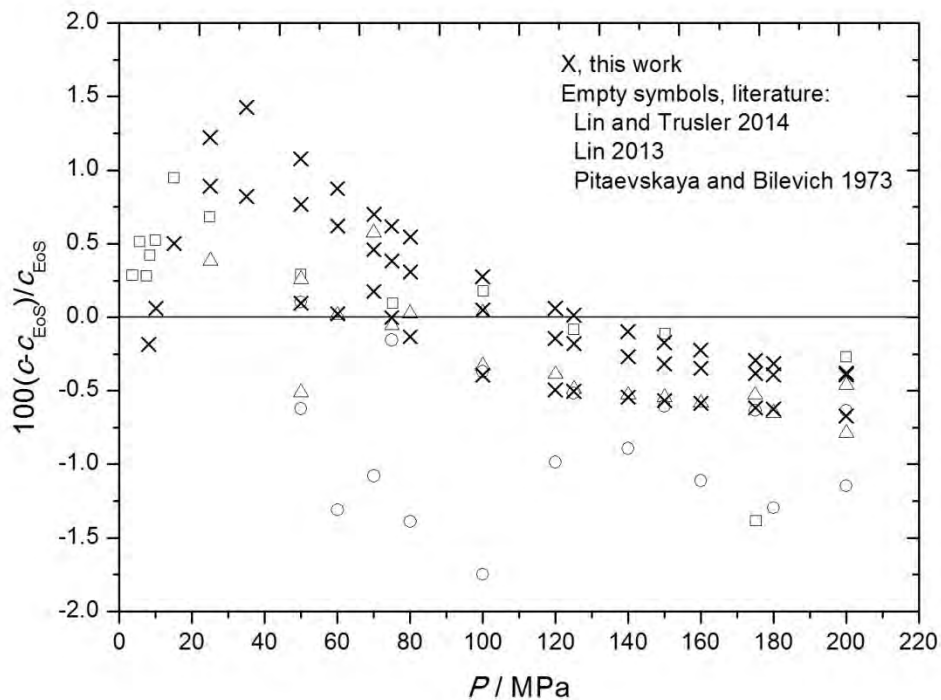


Figure 8. Relative deviations of the experimental speed of sound in CO₂+CH₃OH mixtures in this work, c , from the speed of sound in pure CO₂ calculated by the Span and Wagner EoS, c_{EoS} . \star , $x_{\text{CO}_2} = 0.9503$; \blacklozenge , $x_{\text{CO}_2} = 0.9700$; \blacktriangle , $x_{\text{CO}_2} = 0.9794$; \bullet , $x_{\text{CO}_2} = 0.9845$; \blacksquare , $x_{\text{CO}_2} = 0.9898$. Deviations when doping with 1% of methanol lie between the dotted lines.

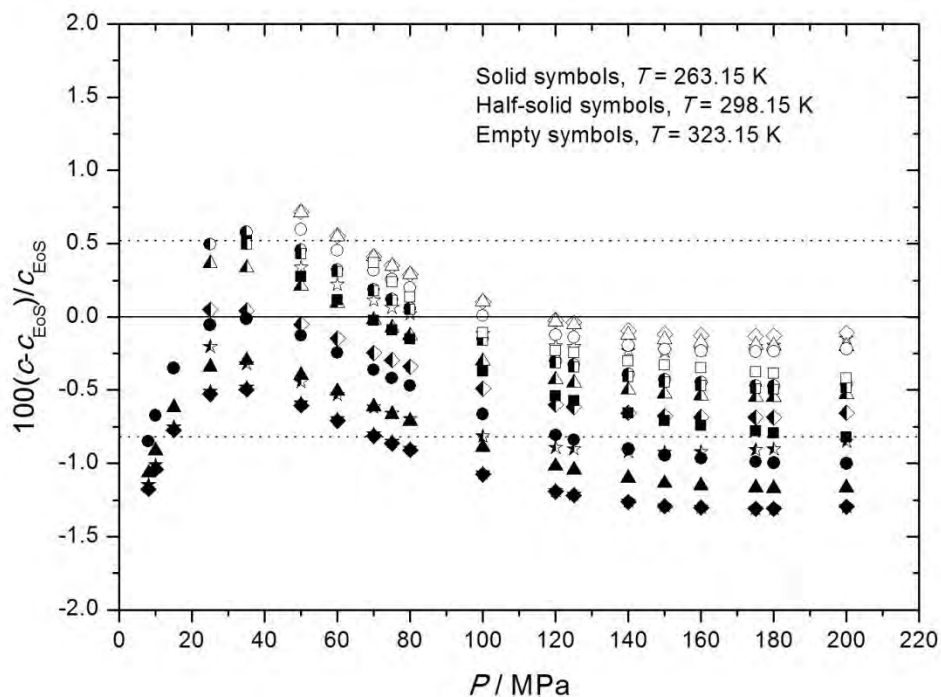


Figure 9. Correlation of the speed of sound calculated with equation (7), c_{fit} , as a function of the CO₂ mole fraction, x_{CO_2} , for the CO₂+CH₃OH mixtures at the three studied temperatures and at several pressures (equation 8, Table 9). ■, $P = 50$ MPa; ▲, $P = 100$ MPa; ◆, $P = 150$ MPa; ★, $P = 200$ MPa. Solid symbols, $T = 263.15$ K; half-solid symbols, $T = 298.15$ K; empty symbols, $T = 323.15$ K.

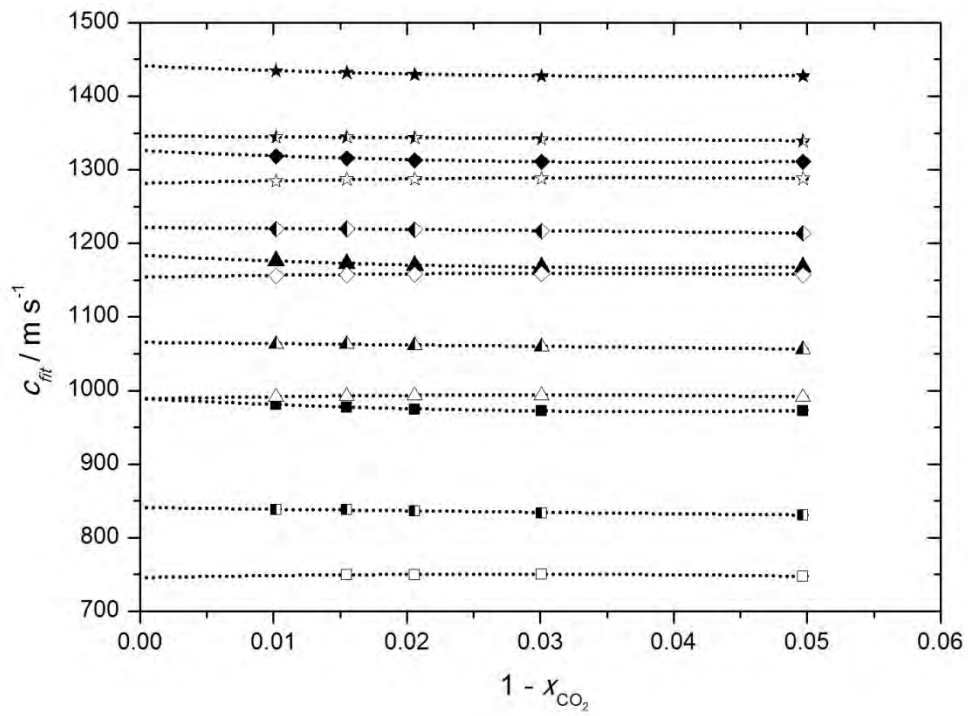
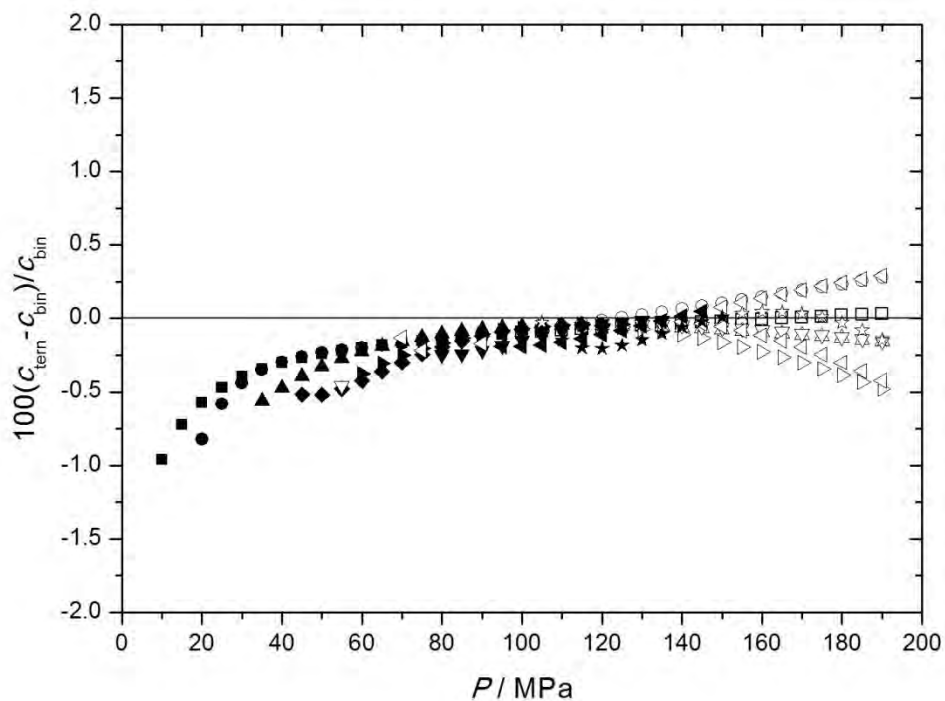


Figure 10. Relative deviations between the $P - c - T$ data in this work for the binary (c_{bin}) $\text{CO}_2 + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8969, x_{\text{SO}_2} = 0.1031$) and the ternary (c_{ter}) $\text{CO}_2 + \text{CH}_3\text{OH} + \text{SO}_2$ ($x_{\text{CO}_2} = 0.8889, x_{\text{CH}_3\text{OH}} = 0.0080, x_{\text{SO}_2} = 0.1031$) mixtures at temperatures T and pressures P . ■, $T = 263.15$ K; ●, $T = 273.15$ K; ▲, $T = 293.15$ K; ◆, $T = 304.16$ K; ►, $T = 313.15$ K; ▼, $T = 333.15$ K; ◀, $T = 353.15$ K; ★, $T = 373.19$ K. Solid symbols, correlated data; empty symbols, extrapolated data (equation 7, Tables 7 and 8).



**High-pressure speed of sound in pure CO₂ and in CO₂ with SO₂ as an impurity
using methanol as a doping agent**

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SUPPLEMENTARY MATERIAL

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the $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ mixture with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, modeled as a binary mixture.	
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Table S1. Parameters used in the modeling of the studied systems with the PC-SAFT EoS.

CO ₂ +CH ₃ OH and CO ₂ +CH ₃ OH+SO ₂ systems			
Pure compound parameters	CO ₂ ^a	CH ₃ OH ^a	SO ₂ ^b
m/M (mol/g)	0.04834	0.05273	0.04466
σ (Å)	2.8251	3.3264	2.6826
ε (K)	163.76	175.20	205.35
$\kappa^{A_i B_i}$	0.035176	0.035176	
$\varepsilon^{A_i B_i}$ (K)	0	2899.5	
Association scheme	2C	2B	
CO ₂ +SO ₂ system			
Pure compound parameters	CO ₂ ^b		SO ₂ ^b
m/M (mol/g)	0.04710		0.04466
σ (Å)	2.7852		2.6826
ε (K)	169.21		205.35
Binary interaction parameter CO ₂ - CH ₃ OH ^a : $k_{ij} = -0.323 + 2.88 \times 10^{-4} T$			
Binary interaction parameter CO ₂ - SO ₂ ^c : $k_{ij} = 0.03$			
Binary interaction parameter SO ₂ - CH ₃ OH ^d : $k_{ij} = 0$			

^a Gil, L., Blanco, S., Rivas, C., Laga, E., Fernández, J., Artal, M., Velasco, I., 2012. Experimental determination of the critical loci for {*n*-C₆H₁₄ or CO₂ + alkan-1-ol} mixtures. Evaluation of their critical and subcritical behavior using PC-SAFT EoS. The Journal of Supercritical Fluids 71, 26-44. <http://dx.doi.org/10.1016/j.supflu.2012.07.008>.

^b Gross, J., Sadowski, G., 2001. Perturbed-Chain SAFT: An equation of state based on a perturbation theory for chain molecules. Industrial & Engineering Chemical Research 40, 1244-1260. <http://dx.doi.org/10.1021/ie0003887>.

^c Diamantonis, N.I., Boulougouris, G.C., Mansoor, E., Tsangaris, D.M., Economou, I.G., 2013. Evaluation of cubic, SAFT, and PC-SAFT equations of state for the vapor-liquid equilibrium modeling of CO₂ mixtures with other gases. Industrial & Engineering Chemistry Research 52, 3933-3942. <http://dx.doi.org/10.1021/ie303248q>.

^d This work, $T = 263.15$ - 313.15 K.

Figure S1. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.8005$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

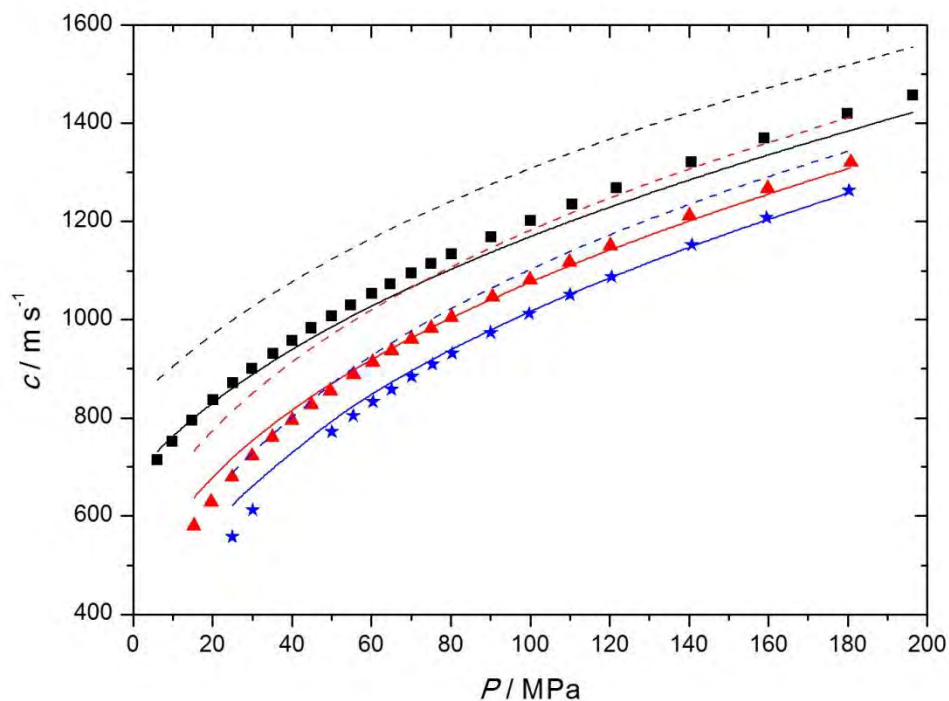


Figure S2. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9025$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

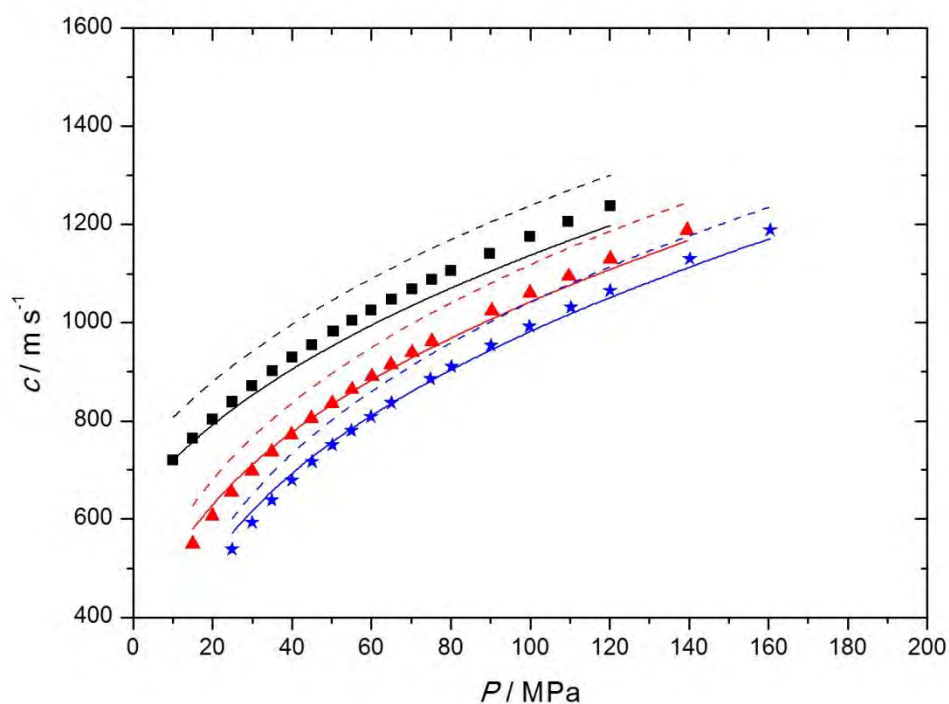


Figure S3. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9700$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K (Rivas et al. 2016); \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

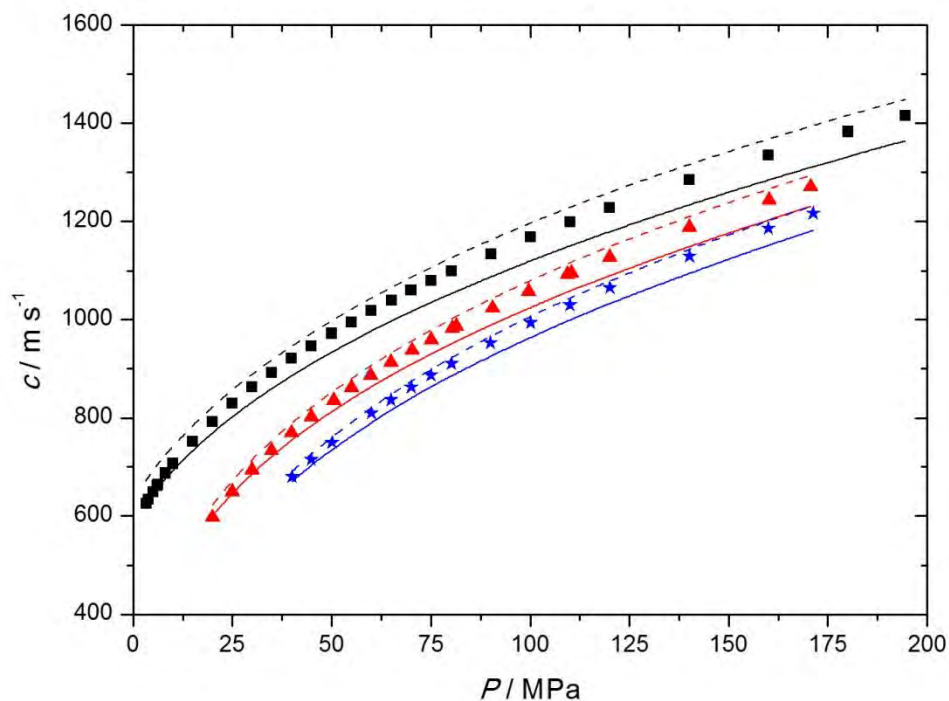


Figure S4. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9794$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

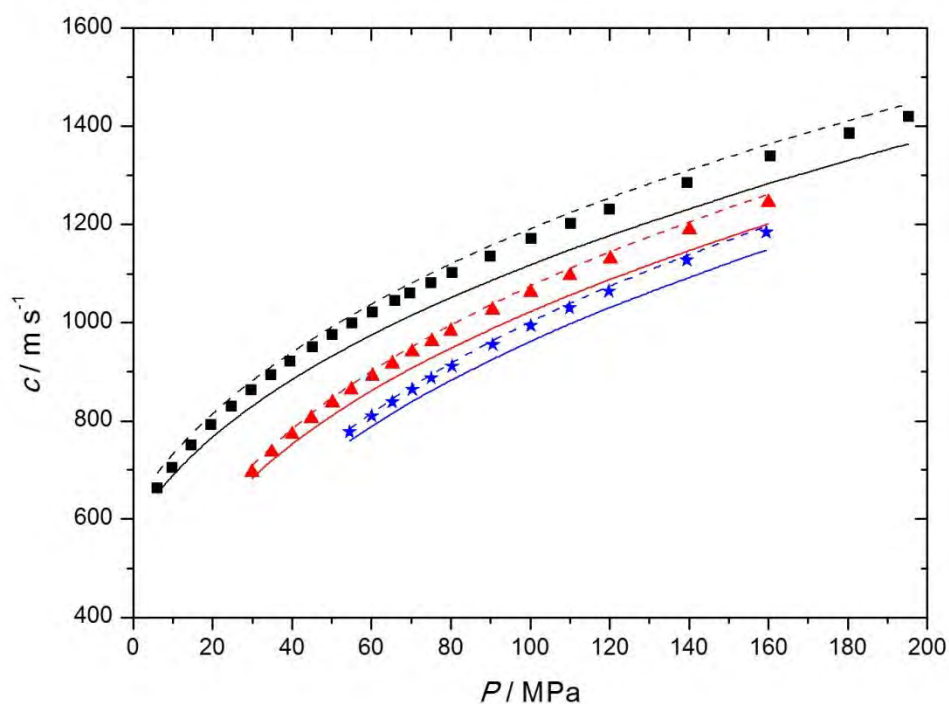


Figure S5. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9845$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

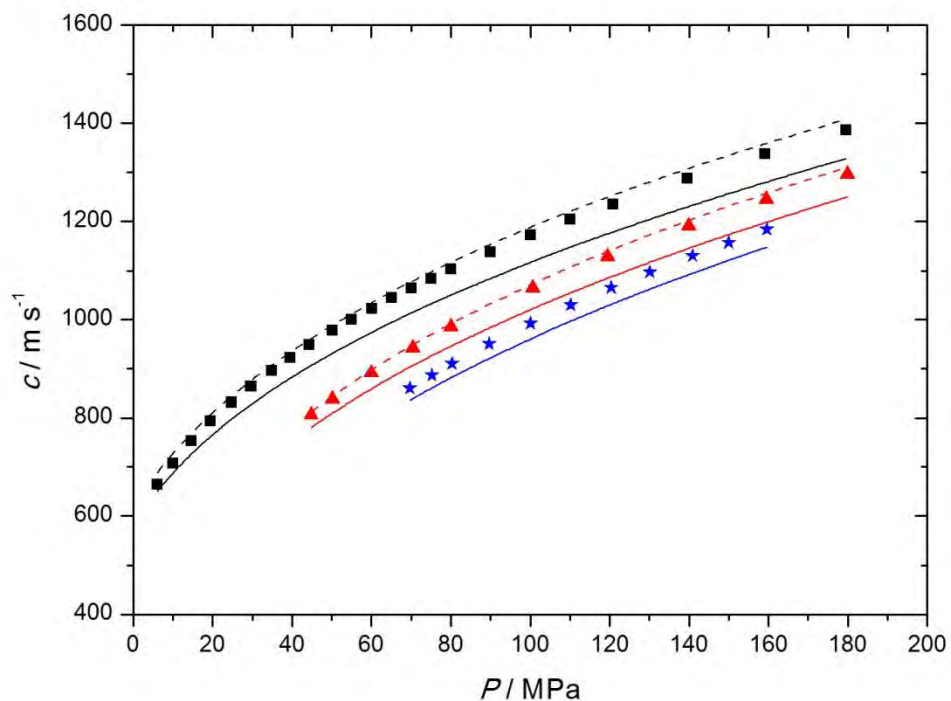


Figure S6. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}$ with $x_{\text{CO}_2} = 0.9898$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 298.15$ K; \star , $T = 323.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software.

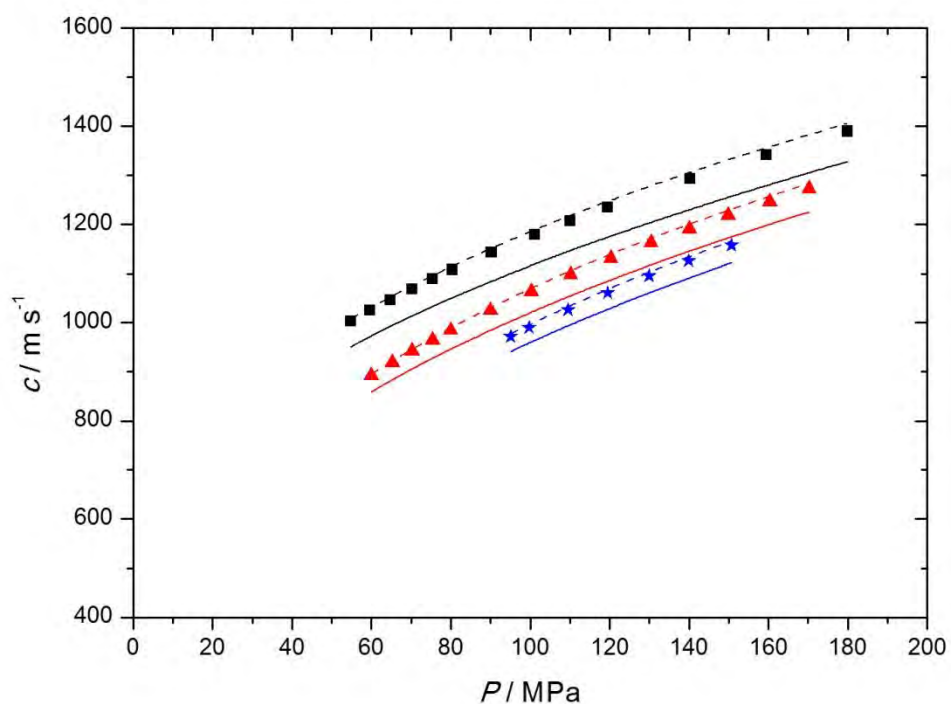


Figure S7. Relative deviations between the experimental speed of sound in this work in the CO₂+CH₃OH mixtures, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at $T = 263.15$ K.

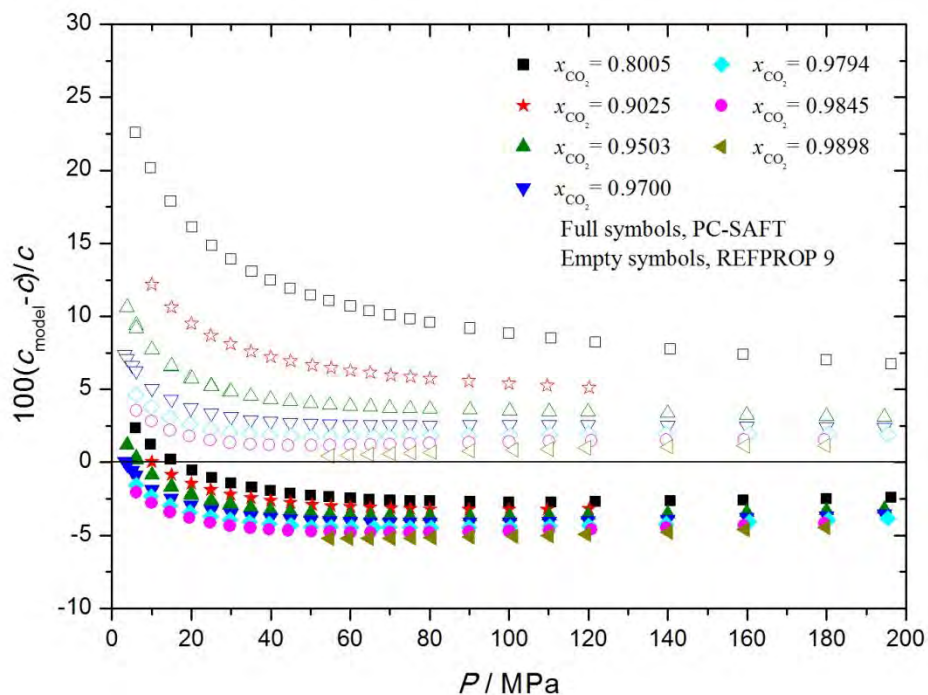


Figure S8. Relative deviations between the experimental speed of sound in this work in the CO₂+CH₃OH mixtures, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at $T = 298.15$ K.

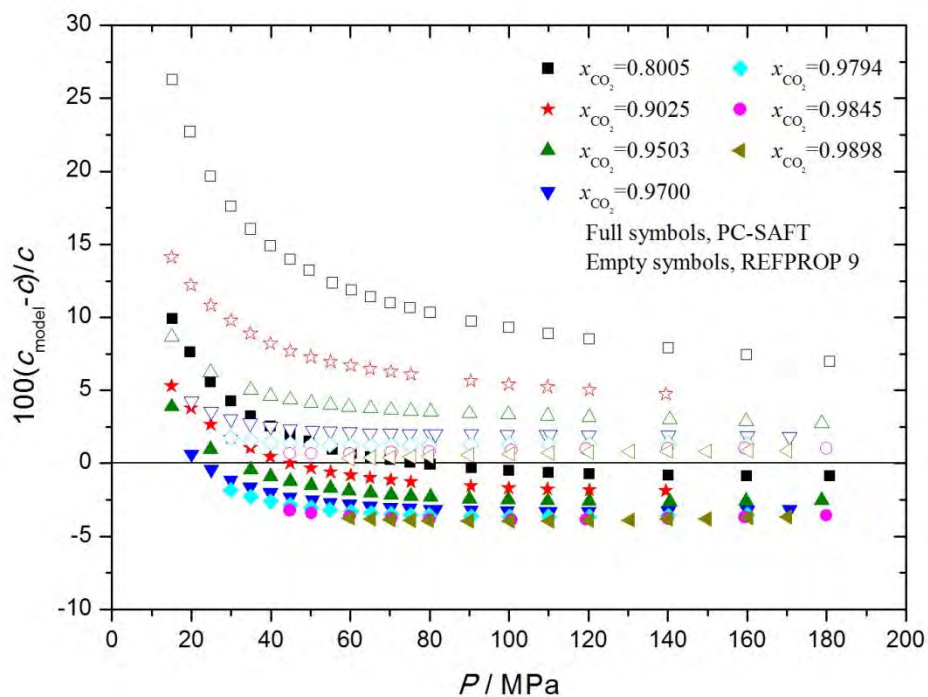


Figure S9. Relative deviations between the experimental speed of sound in this work in the $\text{CO}_2+\text{CH}_3\text{OH}$ mixtures, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at $T = 323.15$ K.

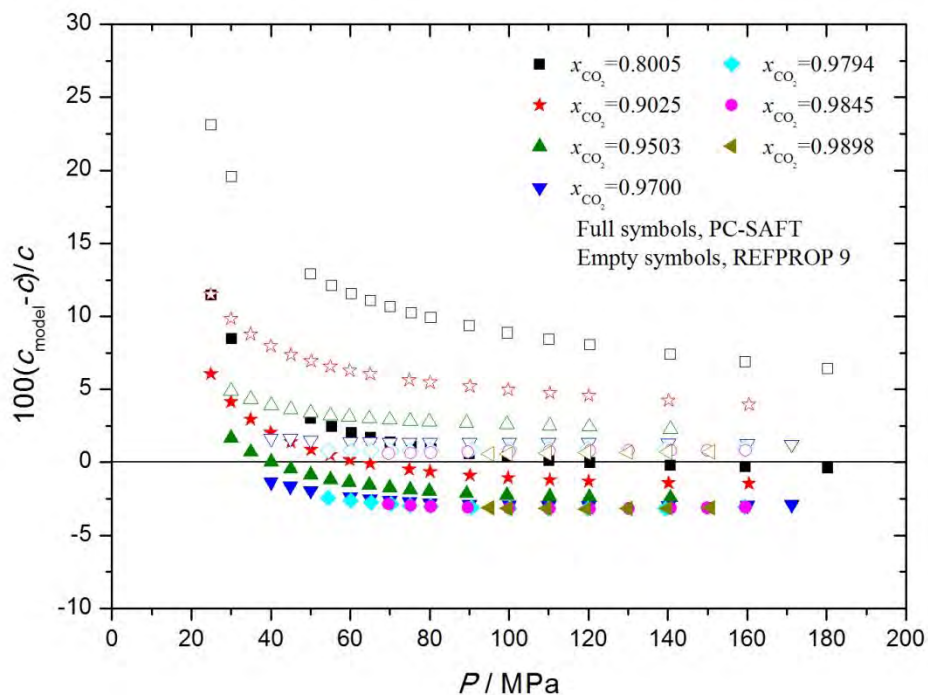


Figure S10. Relative deviations between the experimental speed of sound in this work in the CO_2+SO_2 mixture with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at temperatures T .

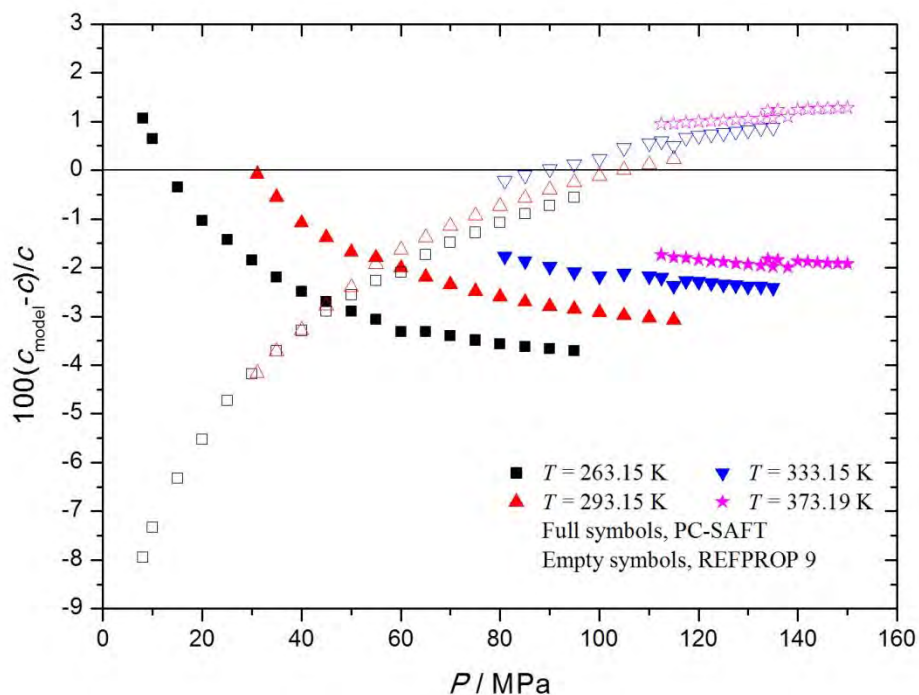


Figure S11. Speed of sound, c , in $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$ at temperatures T and pressures P . Symbols, experimental points: \blacksquare , $T = 263.15$ K; \blacktriangle , $T = 293.15$ K; \blacktriangledown , $T = 333.15$ K; \blackstar , $T = 373.15$ K. Solid lines, PC-SAFT EoS; dashed lines, REFPROP 9 software; system modeled as a ternary mixture.

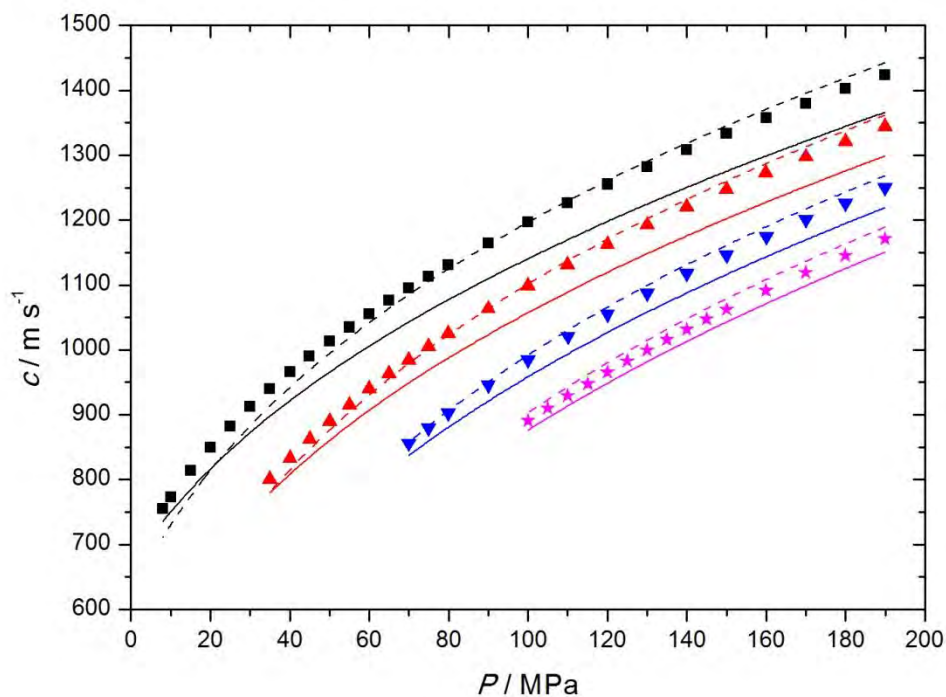


Figure S12. Relative deviations between the experimental speed of sound in this work in the $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ mixture with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at temperatures T . The system was modeled as a ternary mixture.

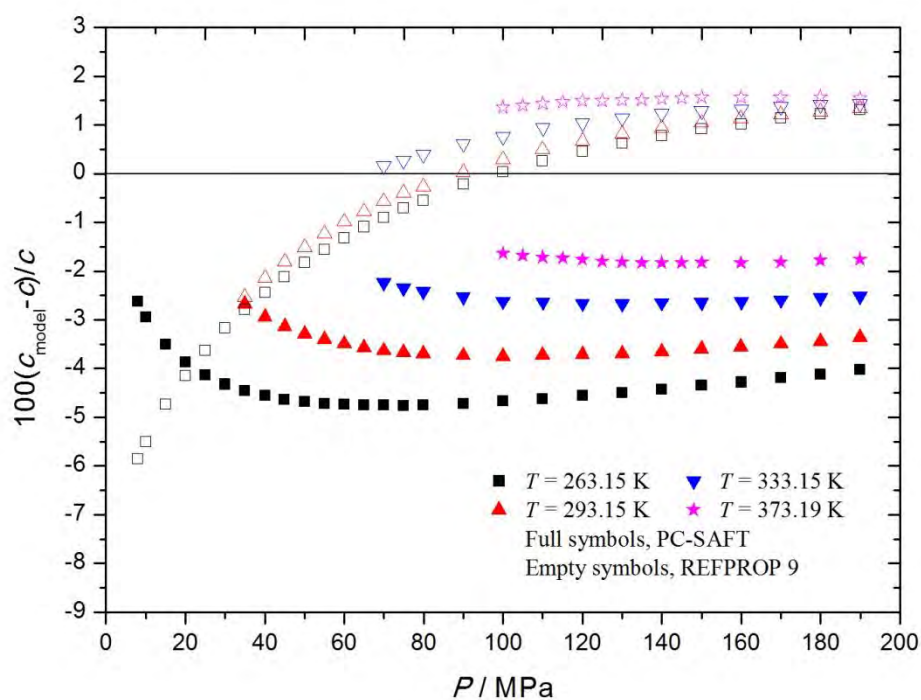


Figure S13. Relative deviations between the experimental speed of sound in the present work in the $\text{CO}_2+\text{CH}_3\text{OH}+\text{SO}_2$ mixture with $x_{\text{CO}_2} = 0.8889$, $x_{\text{CH}_3\text{OH}} = 0.0080$ and $x_{\text{SO}_2} = 0.1031$, c , and the values calculated using the PC-SAFT EoS and the REFPROP 9 software, c_{model} , at temperatures T . The system was modeled as a binary mixture with $x_{\text{CO}_2} = 0.8969$ and $x_{\text{SO}_2} = 0.1031$.

