

### Información del Plan Docente

Academic Year 2017/18

Faculty / School 100 - Facultad de Ciencias

**Degree** 453 - Degree in Mathematics

**ECTS** 6.0 **Year** 2

Semester Second semester

Subject Type Basic Education

Module ---

- 1.General information
- 1.1.Introduction
- 1.2. Recommendations to take this course
- 1.3. Context and importance of this course in the degree
- 1.4. Activities and key dates
- 2.Learning goals
- 2.1.Learning goals
- 2.2.Importance of learning goals
- 3. Aims of the course and competences
- 3.1.Aims of the course
- 3.2.Competences
- 4.Assessment (1st and 2nd call)
- 4.1. Assessment tasks (description of tasks, marking system and assessment criteria)
- 5. Methodology, learning tasks, syllabus and resources
- 5.1.Methodological overview

The learning process will be mainly based on:

-Lectures on the theoretical topics listed in Section 5.3. The explanations will be illustrated by means of a variety of examples and real problems, trying to motivate the student's participation. Computer presentations will be used. Such



lectures will represent, at most, the 50% of the learning activities.

- -Practical classes in which different exercises and questions will be solved in detail. The students will have in advance the whole collection of such exercises, in order to facilitate their homework. These practical sessions will represent, at least, the 40% of the learning activities.
- -Practical sessions in computer labs, where the students will learn to use computer tools in order to solve exercises from a numerical viewpoint. They will represent, at least, the 10% of the learning activities.
- -Individual tutorial sessions to discuss issues concerning the difficulties in the learning process, to correct the way of working, to monitorize the practical work assigned to each student,....

General information about the program, theoretical notes, collection of exercises, complementary material, references,...will be at the student's disposal in the Moodle page of the Zaragoza University.

### 5.2.Learning tasks

In accordance with Section 5.2, the main learning activities will be the following:

- -Two hours per week of theoretical lectures, addressed to all of the students in the course.
- -Two hours per week of practical sessions, including those in computer labs. To carry out these activities, the students will be splitted into two groups.
- -Other learning activities: individual tutorials, personal study and homework, works in groups,...

### 5.3.Syllabus

- 1. DATA ANALYSIS
- 1.1 Introduction: population and sample.
- 1.2 Relative frequencies and graphic representations.
- 1.3 Mean and standard deviation. Median and quantiles. Symmetry and kurtosis.
- 1.4 Outliers. Transformation of variables.
- 1.5 Two-dimensional data: joint, marginal and conditional distributions.
- 1.6 Moments. Covariance matrix and Pearson's correlation coefficient.



1.7 The simplest linear model. Linear regression. Residuals analysis.
2. INTRODUCTION TO PROBABILITY
2.1 Sample space, events and algebras of events.
2.2 Axioms of probability. Consequences.
2.3 Classical probability. Combinatorics.
2.4 Finite, discrete, and geometric models. Examples.
2.5 Conditional probability and independence.
2.6 Total probability formula. Bayes formula.
3. DISCRETE RANDOM VARIABLES
3.1 Introductory examples. Probability laws and distribution functions.
3.2 The most usual distributions: uniform, Bernoulli and binomial, hypergeometric, geometric, negative binomial, and Poisson distributions.
3.3 Mathematical expectations. The expectation of a function of a discrete random variable.
3.4 Moments and central moments. Computations.
3.5 Moments and Chebyshev`s inequality.
3.6 Approximations: from the hypergeometric to the binomial, and from the binomial to the Poisson distributions.
4. ABSOLUTELY CONTINUOUS RANDOM VARIABLES



- 4.1 Introduction. Probability densities.
- 4.2 Distribution functions. Properties.
- 4.3 The most usual distributions: uniform, triangular, exponential, gamma, beta, Pareto, Cauchy, and normal distributions.
- 4.4 Transformations of absolutely continuous random variables. Change of variables.
- 4.5 Moments and central moments. Computations.
- 4.6 Moments and Chebyshev's inequality.
- 4.7 The normal distribution: specific analysis and perspectives.
- 4.8 General random variables. Mixed random variables.

### 5.4. Course planning and calendar

The schedule of theoretical lectures and practical sessions will be previously announced in the web page of the faculty, as well as in the web page of the course.

A mid-term exam will be done. The exam date will be previously announced in the web page of the course.

## 5.5.Bibliography and recommended resources

References

Bartoszynski, Robert. Probability and statistical inference / Robert Bartoszynski, Magdalena Niewiadomska-Bugaj New York [etc.]: John Wiley and Sons, cop. 1996

Chung, Kai Lai. Elementary probability theory : with stochastic processes and an introduction to mathematical finance / Kai Lai Chung, Farid AitSahlia . - 4th ed. New York : Springer cop. 2003

Grimmett, Geoffrey. Probability and random processes / Geoffrey Grimmett and David Stirzaker . - 3rd. ed., repr. with corr. Oxford : Oxford University Press, 2004

Lasala, Pilar. Introducción al cálculo de probabilidades / Pilar Lasala Calleja Zaragoza : Prensas Universitarias de Zaragoza, 1996



Lasala, Pilar. Problemas resueltos de cálculo de probabilidades / Pilar Lasal Calleja Zaragoza : Prensas Universitarias de Zaragoza, 1996

Uña Juárez, Isaías. Lecciones de cálculo de probabilidades : curso teórico- práctico / Isaías Uña Juárez, Venancio Tomeo Perucha, Jesús San Martín Moreno Madrid [etc.] : Thomson, D.L. 2003

Uña, I.. Cálculo de Probabilidades. Garceta. 2010.

Vélez Ibarrola, Ricardo. Cálculo de probabilidades I / Ricardo Vélez Ibarrola, Víctor Hernández Morales . - [1a.ed.] Madrid : UNED, 1995

- Lecture notes on the course. Available online at the Moodle page of the Zaragoza University.