

Anexos

A. Producción de pares en DSR

In[*]:= **Solve**[**Refine**[$e^2 - p^2 + \alpha 1 / M * e^3 + \alpha 2 / M * e * p^2 - m^2$, $e \in \text{Reals} \ \&\& \ e > 0 \ \&\& \ p > 0$] == 0, e]
[resue·· [refina [números reales

$$\text{Out[*]} = \left\{ \left\{ e \rightarrow -\frac{M}{3 \alpha 1} - \left(2^{1/3} \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right) \right) / \left(3 \alpha 1 \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right) + \frac{1}{3 \times 2^{1/3} \alpha 1} \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right\}, \right. \\ \left\{ e \rightarrow -\frac{M}{3 \alpha 1} + \left(\left(1 + i \sqrt{3} \right) \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right) \right) / \left(3 \times 2^{2/3} \alpha 1 \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right) - \frac{1}{6 \times 2^{1/3} \alpha 1} \left(1 - i \sqrt{3} \right) \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right\}, \right. \\ \left\{ e \rightarrow -\frac{M}{3 \alpha 1} + \left(\left(1 - i \sqrt{3} \right) \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right) \right) / \left(3 \times 2^{2/3} \alpha 1 \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right) - \frac{1}{6 \times 2^{1/3} \alpha 1} \left(1 + i \sqrt{3} \right) \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 + \sqrt{4 \left(-M^2 + 3 p^2 \alpha 1 \alpha 2 \right)^3 + \left(-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 \right)^2} \right)^{1/3} \right\} \right\}$$

In[*]:= **m = a * e;**

```

In[*]:= Refine[Normal[
  refine normal
  Series[- $\frac{M}{3 \alpha 1} - (2^{1/3} (-M^2 + 3 p^2 \alpha 1 \alpha 2)) / (3 \alpha 1 (-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 +$ 
  serie
 $\sqrt{4 (-M^2 + 3 p^2 \alpha 1 \alpha 2)^3 + (-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2)^2})^{1/3} +$ 
 $\frac{1}{3 \times 2^{1/3} \alpha 1} (-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2 +$ 
 $\sqrt{4 (-M^2 + 3 p^2 \alpha 1 \alpha 2)^3 + (-2 M^3 + 27 m^2 M \alpha 1^2 + 27 M p^2 \alpha 1^2 + 9 M p^2 \alpha 1 \alpha 2)^2})^{1/3},$ 
  {M, Infinity, 1}, {ϵ, 0, 2}]]], p > 0 && a > 0]
  infinito

```

$$\begin{aligned}
\text{Out[*]} = & \frac{-(-1)^{1/3} \sqrt{3} p \sqrt{-M^4 \alpha 1^2} - (-1)^{2/3} \sqrt{3} p \sqrt{-M^4 \alpha 1^2}}{3 M^2 \alpha 1} + \\
& \frac{\left(-(-1)^{1/3} \sqrt{3} a^2 p \sqrt{-M^4 \alpha 1^2} - (-1)^{2/3} \sqrt{3} a^2 p \sqrt{-M^4 \alpha 1^2}\right) \epsilon^2}{6 M^2 p^2 \alpha 1} + \frac{1}{M} \\
& \left(\frac{1}{2} \left(-(-1)^{1/3} p^2 \alpha 1 + (-1)^{2/3} p^2 \alpha 1 - (-1)^{1/3} p^2 \alpha 2 + (-1)^{2/3} p^2 \alpha 2\right) + \right. \\
& \left. \frac{1}{2} \left(-(-1)^{1/3} a^2 \alpha 1 + (-1)^{2/3} a^2 \alpha 1\right) \epsilon^2\right)
\end{aligned}$$

In[*]:= ϵ = 1;

```

In[*]:= Simplify[
  simplifica
 $\frac{-(-1)^{1/3} \sqrt{3} p \sqrt{-M^4 \alpha 1^2} - (-1)^{2/3} \sqrt{3} p \sqrt{-M^4 \alpha 1^2}}{3 M^2 \alpha 1} +$ 
 $\frac{\left(-(-1)^{1/3} \sqrt{3} a^2 p \sqrt{-M^4 \alpha 1^2} - (-1)^{2/3} \sqrt{3} a^2 p \sqrt{-M^4 \alpha 1^2}\right) \epsilon^2}{6 M^2 p^2 \alpha 1} + \frac{1}{M}$ 
 $\left(\frac{1}{2} \left(-(-1)^{1/3} p^2 \alpha 1 + (-1)^{2/3} p^2 \alpha 1 - (-1)^{1/3} p^2 \alpha 2 + (-1)^{2/3} p^2 \alpha 2\right) + \right.$ 
 $\left. \frac{1}{2} \left(-(-1)^{1/3} a^2 \alpha 1 + (-1)^{2/3} a^2 \alpha 1\right) \epsilon^2\right)]$ 

```

$$\text{Out[*]} = \frac{a^2 \left(-3 M p \alpha 1^2 - 3 i \sqrt{-M^4 \alpha 1^2}\right) - 3 p^2 \left(2 i \sqrt{-M^4 \alpha 1^2} + M p \alpha 1 (\alpha 1 + \alpha 2)\right)}{6 M^2 p \alpha 1}$$

```

In[*]:= Refine[
  refine
 $\frac{a^2 \left(-3 M p \alpha 1^2 - 3 i \sqrt{-M^4 \alpha 1^2}\right) - 3 p^2 \left(2 i \sqrt{-M^4 \alpha 1^2} + M p \alpha 1 (\alpha 1 + \alpha 2)\right)}{6 M^2 p \alpha 1},$ 

```

M > 0 && α1 > 0 && α2 > 0]

$$\text{Out[*]} = \frac{a^2 \left(3 M^2 \alpha 1 - 3 M p \alpha 1^2\right) - 3 p^2 \left(-2 M^2 \alpha 1 + M p \alpha 1 (\alpha 1 + \alpha 2)\right)}{6 M^2 p \alpha 1}$$

```

In[*]:= Simplify[
  simplifica
 $\frac{a^2 \left(3 M^2 \alpha 1 - 3 M p \alpha 1^2\right) - 3 p^2 \left(-2 M^2 \alpha 1 + M p \alpha 1 (\alpha 1 + \alpha 2)\right)}{6 M^2 p \alpha 1}]$ 

```

$$\text{Out[*]} = \frac{2 M p^2 + a^2 (M - p \alpha 1) - p^3 (\alpha 1 + \alpha 2)}{2 M p}$$

Esta es la expresión de la energía E (p).

```
In[ ]:= e[p_, m_] := (2 * M * p^2 + M * m^2 - p^3 * (α1 + α2)) / (2 * M * p);
```

Ecuación de conservación del momento para obtener p (el momento del electrón/positrón) en función de k (momento del fotón).

```
In[ ]:= Clear[ε];
borra
```

```
In[ ]:= a = m * ε; c = ω * ε;
```

Lado izquierdo de la ecuación.

```
In[ ]:= Refine[Normal[Series[k - c - γ1 * e[k, 0] * c / M + γ2 * k * c / M, {M, Infinity, 0}], {ε, 0, 2}]],
refina normal serie infinito
me > 0 && k > 0 && ω > 0]
```

```
Out[ ]:= k - ε ω
```

Lado derecho de la ecuación.

```
In[ ]:= Refine[Normal[Series[2 * p + (γ1 + γ2) * e[p, a] * p / M, {M, Infinity, 1}], {ε, 0, 2}]],
refina normal serie infinito
me > 0 && k > 0 && ω > 0]
```

```
Out[ ]:= 2 p + \frac{p^2 (\gamma_1 + \gamma_2) + \frac{1}{2} m \epsilon^2 (\gamma_1 + \gamma_2) \epsilon^2}{M}
```

```
In[ ]:= Solve[k - ω == 2 * p + p^2 * (γ1 + γ2) / M, p]
resuelve
```

```
Out[ ]:= {{p -> \frac{-1 - \frac{\sqrt{M+k \gamma_1+k \gamma_2-\gamma_1 \omega-\gamma_2 \omega}}{\sqrt{M}}}{\frac{\gamma_1}{M} + \frac{\gamma_2}{M}}}, {p -> \frac{-1 + \frac{\sqrt{M+k \gamma_1+k \gamma_2-\gamma_1 \omega-\gamma_2 \omega}}{\sqrt{M}}}{\frac{\gamma_1}{M} + \frac{\gamma_2}{M}}}}
```

Elegimos la segunda que es la positiva.

```
In[ ]:= Refine[Normal[Series[\frac{-1 + \frac{\sqrt{M+k \gamma_1+k \gamma_2-\gamma_1 \omega-\gamma_2 \omega}}{\sqrt{M}}}{\frac{\gamma_1}{M} + \frac{\gamma_2}{M}}, {M, Infinity, 1}], {ε, 0, 2}]],
refina normal serie infinito
```

```
me > 0 && k > 0 && ω > 0]
```

```
Out[ ]:= \frac{k - \omega}{2} - \frac{(\gamma_1 + \gamma_2) (k - \omega)^2}{8 M}
```

```
In[ ]:= mome = (k - c) / 2 - k^2 * (γ1 + γ2) / (8 * M);
```

Ecuación de conservación de la energía.

```

In[ ]:= Refine[Normal[Series[e[k, 0] + c, {M, Infinity, 1}, {ϵ, 0, 0}], me > 0 && k > 0 && ω > 0] -
  Refine[Normal[Series[e[k, 0] + c, {M, Infinity, 0}, {ϵ, 0, 0}], me > 0 && k > 0 && ω > 0] +
  Refine[Normal[Series[e[k, 0] + c, {M, Infinity, 0}, {ϵ, 0, 2}], me > 0 && k > 0 && ω > 0] ==
  Refine[Normal[Series[2 * e[mome, a] + β1 * (e[mome, a])^2 / M + β2 * mome^2 / M,
    {M, Infinity, 1}, {ϵ, 0, 0}], me > 0 && k > 0 && ω > 0] -
  Refine[Normal[Series[2 * e[mome, a] + β1 * (e[mome, a])^2 / M + β2 * mome^2 / M,
    {M, Infinity, 0}, {ϵ, 0, 0}], me > 0 && k > 0 && ω > 0] +
  Refine[Normal[Series[2 * e[mome, a] + β1 * (e[mome, a])^2 / M + β2 * mome^2 / M,
    {M, Infinity, 0}, {ϵ, 0, 2}], me > 0 && k > 0 && ω > 0]

```

$$\text{Out[]} = k - \frac{k^2 (\alpha_1 + \alpha_2)}{2 M} + \epsilon \omega = k + \frac{-k^2 \alpha_1 - k^2 \alpha_2 + k^2 \beta_1 + k^2 \beta_2 - k^2 \gamma_1 - k^2 \gamma_2}{4 M} + \frac{2 m e^2 \epsilon^2}{k} - \epsilon \omega$$

In[]:= $\epsilon = 1$;

$$\text{In[]} = \text{Simplify}\left[k - \frac{k^2 (\alpha_1 + \alpha_2)}{2 M} + \epsilon \omega = k + \frac{-k^2 \alpha_1 - k^2 \alpha_2 + k^2 \beta_1 + k^2 \beta_2 - k^2 \gamma_1 - k^2 \gamma_2}{4 M} + \frac{2 m e^2 \epsilon^2}{k} - \epsilon \omega\right]$$

$$\text{Out[]} = \frac{8 m e^2}{k} + \frac{k^2 (\alpha_1 + \alpha_2 + \beta_1 + \beta_2 - \gamma_1 - \gamma_2)}{M} = 8 \omega$$

B. Fotoproducción de piones en DSR

In[*]:= e[p_, m_] := (2 * M * p^2 + M * m^2 - p^3 * (α1 + α2)) / (2 * M * p);

In[*]:= a = mp * ε; b = mpi * ε; c = ω * ε;

In[*]:= momp = mompi * a / b;

In[*]:= Refine[Normal[Series[momp + mompi + γ1 * e[momp, a] * mompi / M + γ2 * momp * e[mompi, b] / M,
[refina [normal [serie
{M, Infinity, 1}, {ε, 0, 2}]]], mp > 0 && mpi > 0 && k > 0 && ω > 0]
[infinito

$$\text{Out[*]} = \text{momp} + \frac{\text{momp} \text{ mp}}{\text{mpi}} + \frac{\frac{\text{momp}^2 \text{ mp } \gamma_1 + \text{momp}^2 \text{ mp } \gamma_2}{\text{mpi}} + \frac{1}{2} (\text{mp mpi } \gamma_1 + \text{mp mpi } \gamma_2) \epsilon^2}{M}$$

In[*]:= ε = 1;

In[*]:= Simplify[momp + $\frac{\text{momp} \text{ mp}}{\text{mpi}} + \frac{\frac{\text{momp}^2 \text{ mp } \gamma_1 + \text{momp}^2 \text{ mp } \gamma_2}{\text{mpi}} + \frac{1}{2} (\text{mp mpi } \gamma_1 + \text{mp mpi } \gamma_2) \epsilon^2}{M}$]
[simplifica

$$\text{Out[*]} = \frac{2 M \text{momp} (\text{mp} + \text{mpi}) + \text{mp} (2 \text{momp}^2 + \text{mpi}^2) (\gamma_1 + \gamma_2)}{2 M \text{mpi}}$$

In[*]:= Solve[k - ω == $\frac{2 M \text{momp} (\text{mp} + \text{mpi}) + \text{mp} (2 \text{momp}^2) (\gamma_1 + \gamma_2)}{2 M \text{mpi}}$, mompi]
[resuelve

$$\text{Out[*]} = \left\{ \left\{ \text{momp} \rightarrow \frac{-1 - \frac{\text{mp}}{\text{mpi}} - \sqrt{\left(-1 - \frac{\text{mp}}{\text{mpi}}\right)^2 - 4 \left(-\frac{\text{mp } \gamma_1}{M \text{mpi}} - \frac{\text{mp } \gamma_2}{M \text{mpi}}\right) (k - \omega)}}{2 \left(\frac{\text{mp } \gamma_1}{M \text{mpi}} + \frac{\text{mp } \gamma_2}{M \text{mpi}}\right)} \right\}, \right. \\ \left. \left\{ \text{momp} \rightarrow \frac{-1 - \frac{\text{mp}}{\text{mpi}} + \sqrt{\left(-1 - \frac{\text{mp}}{\text{mpi}}\right)^2 - 4 \left(-\frac{\text{mp } \gamma_1}{M \text{mpi}} - \frac{\text{mp } \gamma_2}{M \text{mpi}}\right) (k - \omega)}}{2 \left(\frac{\text{mp } \gamma_1}{M \text{mpi}} + \frac{\text{mp } \gamma_2}{M \text{mpi}}\right)} \right\} \right\}$$

In[*]:= Clear[ε];
[borra

In[*]:= Refine[
[refina

Normal[Series[$\frac{-1 - \frac{a}{b} + \sqrt{\left(-1 - \frac{a}{b}\right)^2 - 4 \left(-\frac{a \gamma_1}{M b} - \frac{a \gamma_2}{M b}\right) (k - c)}}{2 \left(\frac{a \gamma_1}{M b} + \frac{a \gamma_2}{M b}\right)}$, {M, Infinity, 1}, {ε, 0, 2}]],
[normal [serie [infinito

mp > 0 && mpi > 0 && k > 0 && ω > 0]

$$\text{Out[*]} = \frac{k \text{mpi}}{\text{mp} + \text{mpi}} + \frac{M \text{mpi} \left(-1 - \frac{\text{mp}}{\text{mpi}} + \frac{\text{mp} + \text{mpi}}{\text{mpi}}\right)}{2 \text{mp} (\gamma_1 + \gamma_2)} - \frac{\text{mpi } \epsilon \omega}{\text{mp} + \text{mpi}} + \\ - \frac{k^2 \text{mp mpi}^2 (\gamma_1 + \gamma_2)}{(\text{mp} + \text{mpi})^3} + \frac{2 k \text{mp mpi}^2 (\gamma_1 + \gamma_2) \epsilon \omega}{(\text{mp} + \text{mpi})^3} - \frac{\text{mp mpi}^2 (\gamma_1 + \gamma_2) \epsilon^2 \omega^2}{(\text{mp} + \text{mpi})^3} \\ M$$

In[*]:= ε = 1;

$$\begin{aligned}
\text{In}[*]:= & \text{Simplify}\left[\frac{k \text{ mpi}}{mp + mpi} + \frac{M \text{ mpi} \left(-1 - \frac{mp}{mpi} + \frac{mp+mpi}{mpi}\right)}{2 mp (\gamma_1 + \gamma_2)} - \right. \\
& \left. \frac{mpi \epsilon \omega}{mp + mpi} + \frac{-\frac{k^2 mp \text{ mpi}^2 (\gamma_1 + \gamma_2)}{(mp+mpi)^3} + \frac{2 k mp \text{ mpi}^2 (\gamma_1 + \gamma_2) \epsilon \omega}{(mp+mpi)^3} - \frac{mp \text{ mpi}^2 (\gamma_1 + \gamma_2) \epsilon^2 \omega^2}{(mp+mpi)^3}}{M} \right] \\
\text{Out}[*]= & \frac{mpi \left(M (mp + mpi)^2 - mp \text{ mpi} (\gamma_1 + \gamma_2) (k - \omega) \right) (k - \omega)}{M (mp + mpi)^3}
\end{aligned}$$

Definimos el momento del pion a partir del del fotón incidente.

$$\begin{aligned}
\text{In}[*]:= & \text{Clear}[\epsilon]; \\
& \text{borra} \\
\text{In}[*]:= & \text{momp} = (b * M * (a + b)^2 * (k - c) - a * b^2 * (\gamma_1 + \gamma_2) * k^2) / (M * (a + b)^3); \\
\text{In}[*]:= & \text{momp} = \text{momp} * a / b; \\
\text{In}[*]:= & \text{Refine}[\text{Normal}[\text{Series}[e[k, a] + c, \{M, \text{Infinity}, 1\}, \{\epsilon, 0, 0\}]], \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] - \\
& \text{Refine}[\text{Normal}[\text{Series}[e[k, a] + c, \{M, \text{Infinity}, 0\}, \{\epsilon, 0, 0\}]], \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] + \\
& \text{Refine}[\text{Normal}[\text{Series}[e[k, a] + c, \{M, \text{Infinity}, 0\}, \{\epsilon, 0, 2\}]], \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] == \\
& \text{Refine}[\text{Normal}[\text{Series}[e[\text{momp}, a] + e[\text{momp}i, b] + \beta_1 * e[\text{momp}, a] * e[\text{momp}i, b] / M + \\
& \text{refina} \quad \text{normal} \quad \text{serie} \\
& \beta_2 * \text{momp} * \text{momp}i / M, \{M, \text{Infinity}, 1\}, \{\epsilon, 0, 0\}]], mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] - \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& \text{Refine}[\text{Normal}[\text{Series}[e[\text{momp}, a] + e[\text{momp}i, b] + \beta_1 * e[\text{momp}, a] * e[\text{momp}i, b] / M + \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& \beta_2 * \text{momp} * \text{momp}i / M, \{M, \text{Infinity}, 0\}, \{\epsilon, 0, 0\}]], mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] + \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& \text{Refine}[\text{Normal}[\text{Series}[e[\text{momp}, a] + e[\text{momp}i, b] + \beta_1 * e[\text{momp}, a] * e[\text{momp}i, b] / M + \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
& \beta_2 * \text{momp} * \text{momp}i / M, \{M, \text{Infinity}, 0\}, \{\epsilon, 0, 2\}]], mp > 0 \&\& mpi > 0 \&\& k > 0 \&\& \omega > 0] \\
& \text{refina} \quad \text{normal} \quad \text{serie} \quad \text{infinito} \\
\text{Out}[*]= & k - \frac{k^2 (\alpha_1 + \alpha_2)}{2 M} + \frac{mp^2 \epsilon^2}{2 k} + \epsilon \omega == \\
& k + \frac{1}{2 M (mp + mpi)^2} \left(-k^2 mp^2 \alpha_1 - k^2 mpi^2 \alpha_1 - k^2 mp^2 \alpha_2 - k^2 mpi^2 \alpha_2 + 2 k^2 mp \text{ mpi} \beta_1 + \right. \\
& \left. 2 k^2 mp \text{ mpi} \beta_2 - 2 k^2 mp \text{ mpi} \gamma_1 - 2 k^2 mp \text{ mpi} \gamma_2 \right) + \frac{(mp^2 + 2 mp \text{ mpi} + mpi^2) \epsilon^2}{2 k} - \epsilon \omega \\
\text{In}[*]:= & \epsilon = 1;
\end{aligned}$$

In[*]:= **Simplify** $\left[k - \frac{k^2 (\alpha_1 + \alpha_2)}{2 M} + \frac{m p^2 \epsilon^2}{2 k} + \epsilon \omega\right] ==$
 [simplifica

$$k + \frac{1}{2 M (m p + m p i)^2} \left(-k^2 m p^2 \alpha_1 - k^2 m p i^2 \alpha_1 - k^2 m p^2 \alpha_2 - k^2 m p i^2 \alpha_2 + 2 k^2 m p m p i \beta_1 + \right. \\ \left. 2 k^2 m p m p i \beta_2 - 2 k^2 m p m p i \gamma_1 - 2 k^2 m p m p i \gamma_2 \right) + \frac{(m p^2 + 2 m p m p i + m p i^2) \epsilon^2}{2 k} - \epsilon \omega \Big] \\ Out[*]= \frac{2 k^2 m p m p i (\alpha_1 + \alpha_2 + \beta_1 + \beta_2 - \gamma_1 - \gamma_2)}{M (m p + m p i)} + \frac{(m p + m p i) (2 m p m p i + m p i^2 - 4 k \omega)}{k} == 0$$